







### **Topics Covered**

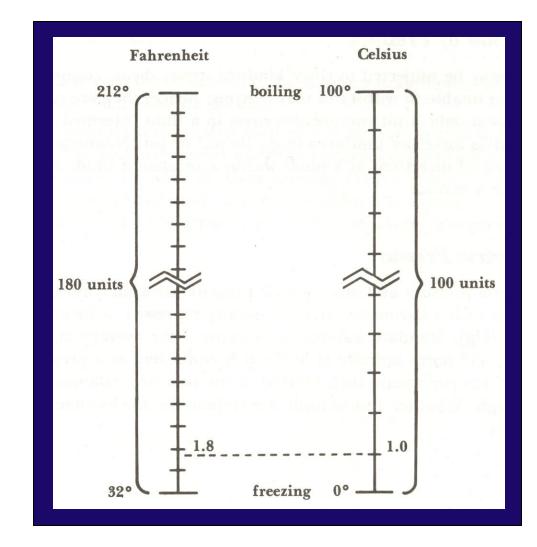




- Gas temperature
- Gas pressure
- Molecular weight and the mole
- Equation of state
- Viscosity
- Reynolds Number



#### **Gas Temperature**

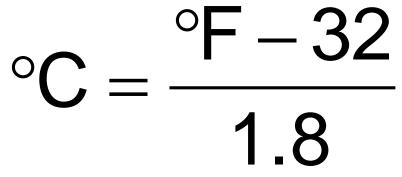




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#### **Conversion Equations**

# °F = 1.8°C + 32



### **Absolute Temperature**





#### Kelvin

#### $K = {}^{\circ}C + 273$



#### $^{\circ}R = ^{\circ}F + 460$

### **Standard Temperature**



Group	T <sub>std</sub>
USEPA (General)	68°F (20°C)
USEPA (Air monitoring)	77°F (25°C)
Industrial hygiene	70°F (21.1°C)
Combustion	60°F (15.6°C)
Science	32°F (0°C)

#### Example 1-1



The gas temperature in the stack of a wet scrubber system is 130°F. What is the absolute temperature in Rankine and Kelvin?

Absolute Temp. °R =  $460^{\circ}$ R +  $130^{\circ}$ F =  $590^{\circ}$ R Absolute Temp. K =  $\frac{590^{\circ}$ R}{1.8} = 327.8K



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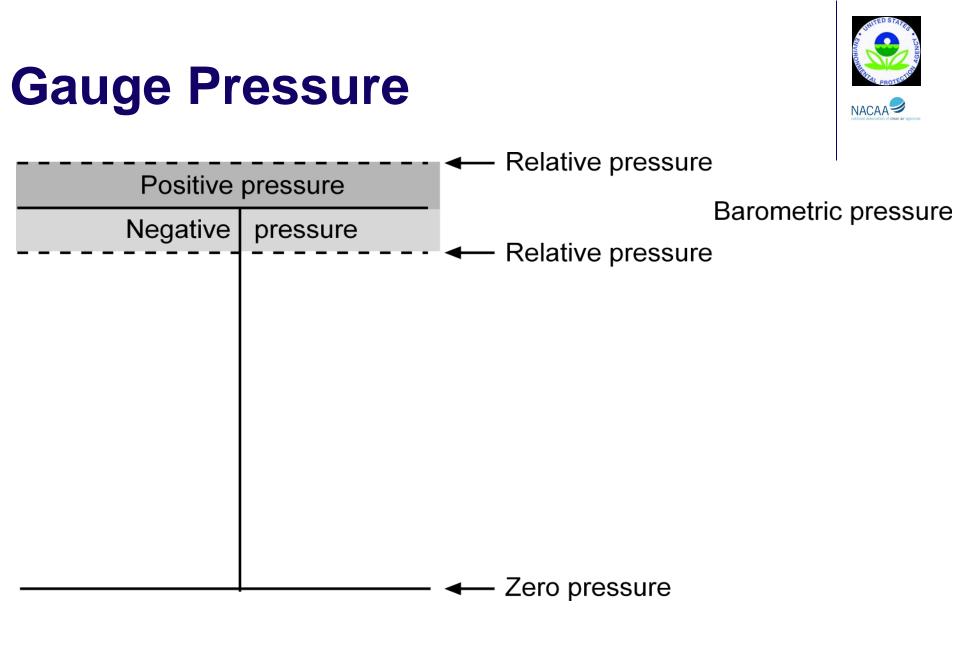
#### **Gas Pressure**

Barometric pressure
Gauge pressure
Absolute pressure

### **Standard Pressure**



Units	Value
Atmosphere (atm)	1
Pounds force per square inch (psi)	14.70
Inches of mercury (in Hg)	29.92
Millimeters of mercury (mm Hg)	760
Feet of water column (ft WC)	33.92
Inches of water column (in WC)	407
Kilopascals (kPa)	101.3
Millibars (mb)	1013









## $\mathsf{P}=\mathsf{P}_\mathsf{b}+\mathsf{P}_\mathsf{g}$

where

P = absolute pressure $P_b = barometric pressure$  $P_g = gauge pressure$ 

#### Example 1-2



An air pollution control device has an inlet static pressure of -25 in WC.

What is the absolute static pressure at the inlet of the air pollution control device if the barometric pressure at the time is 29.85 in Hg?

Convert the barometric pressure units to inWC :

$$P_{b} = 29.85 \text{ in Hg} \left( \frac{407 \text{ in WC}}{29.92 \text{ in Hg}} \right) = 406 \text{ in WC}$$

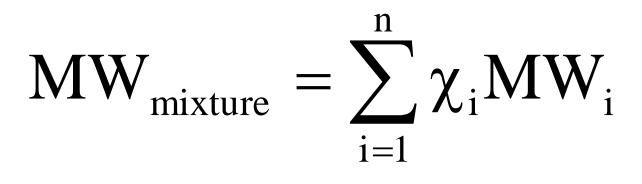
Add the barometric and gauge (static) pressures :

P = 406 in WC + (-25 in WC) = 381 in WC

#### **Molecular Weight**



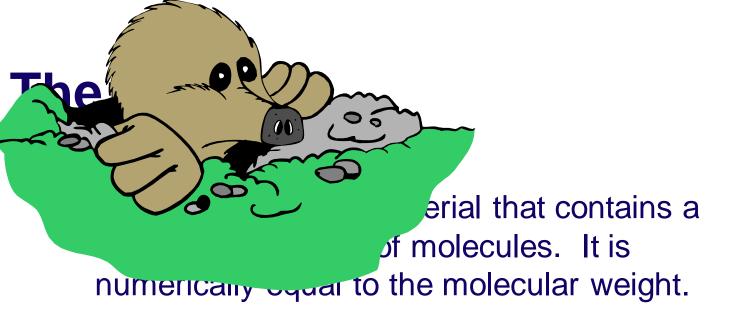
Molecular weight is the sum of the atomic weights of all atoms in a molecule



 $\chi_i$  = mole fraction of component I

MW<sub>i</sub> = molecular weight of component i





The gram-mole is the mass of material that contains Avogadro's number of molecules.

It measures the amount of substance of a system and is defined as the amount of substance that contains as many elementary entities as there are atoms in exactly 0.012 kilogram of carbon-12. This quantity is known as Avogadro's number and is approximately 6.0221415 × 10<sup>23</sup> (2002 CODATA value).

## UNITED STATES



#### **Equation of State**

The ideal gas law:

PV = nRT

- P = absolute pressure
- V = gas volume
- n = number of moles
- R = constant
- T = absolute temperature

#### Values for R



10.73 psia-ft<sup>3</sup>/lb-mole-°R 0.73 atm-ft<sup>3</sup>/lb-mole-°R 82.06 atm-cm<sup>3</sup>/g-mole-K 8.31 x 10<sup>3</sup> kPa-m<sup>3</sup>/kg-mole-K

#### **Volume Correction**





# $\frac{PV}{T} = nR = CONSTANT (if n = CONSTANT)$

$$\frac{P_{1}V_{1}}{T_{1}} = \frac{P_{2}V_{2}}{T_{2}}$$
$$V_{1} = V_{2} \left(\frac{P_{2}}{P_{1}}\right) \left(\frac{T_{1}}{T_{2}}\right)$$

#### Example 1-3

A particulate control system consists of a hood, ductwork, fabric filter, fan, and stack. The total gas flow entering the fabric filter is 8,640 scfm. The gas temperature in the inlet duct is 320°F and the static pressure is -10 in WC. The barometric pressure is 28.30 in Hg.

If the inlet duct has inside dimensions of 3 feet by 4 feet, what is the velocity into the fabric filter?

Convert the static pressure to absolute pressure :

P = 28.30 in Hg 
$$\left(\frac{407 \text{ in WC}}{29.92 \text{ in Hg}}\right)$$
 + (-10 in WC) = 375 in WC

Scfm = standard cubic feet per minute

acfm = actual cubic feet per minute



#### And then...



Convert the gas temperature to absolute temperature :  $T_{actual} = 320^{\circ}F + 460^{\circ} = 780^{\circ}R$ 

Convert the inlet flow rate to actual conditions :

$$Q_{actual} = 8,640 \operatorname{scfm}\left(\frac{780^{\circ} R}{528^{\circ} R}\right)\left(\frac{407 \operatorname{in WC}}{375 \operatorname{in WC}}\right) = 13,853 \operatorname{acfm}$$

Calculate the velocity :

$$V = \frac{\frac{13,853 \text{ ft}^{3}}{\text{min}}}{3 \text{ ft} \cdot 4 \text{ ft}} = 1,154 \text{ ft}/\text{min}$$

#### **Molar Volume**





# $\frac{V}{n} = \frac{RT}{P}$

At 68°F and 1 atm (EPA Standard conditions):

$$=\frac{\left(0.73\frac{atm - ft^{3}}{lb - mole \cdot R}\right)(528 \circ R)}{1 atm} = 385.4\frac{ft^{3}}{lb - mole}$$

#### **Example 1-4**





What is the molar volume of an ideal gas at 200°F and 1 atm?

#### Solution...



At 200°F and 1 atm:

$$\frac{V}{n} = \frac{RT}{P} = \frac{\left(0.73 \frac{\operatorname{atm} \cdot \operatorname{ft}^{3}}{\operatorname{lb} - \operatorname{mole}^{\circ} R}\right)}{\operatorname{1atm}} = 481.8 \operatorname{ft}^{3}/\operatorname{lb} \cdot \operatorname{mole}$$

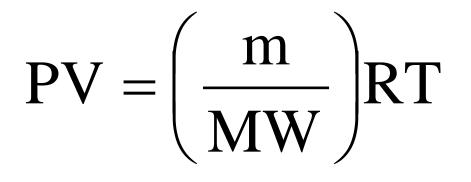
or

$$\frac{V}{n} = 385.4 \left(\frac{660^{\circ}R}{528^{\circ}R}\right) = 481.8 \frac{ft^3}{lb} \cdot \text{mole}$$



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### **Gas Density**



 $\rho = \frac{m}{V} = \frac{P \cdot MW}{RT}$ 

#### Example



Calculate the average molecular weight of air and the density of air at EPA standard conditions. Consider air to be composed of 21 mole% oxygen and 79 mole% nitrogen.

$$MW_{air} = 0.21 \left( \frac{32g}{mole} + 0.79(28g){mole} \right) = \frac{29g}{mole}$$

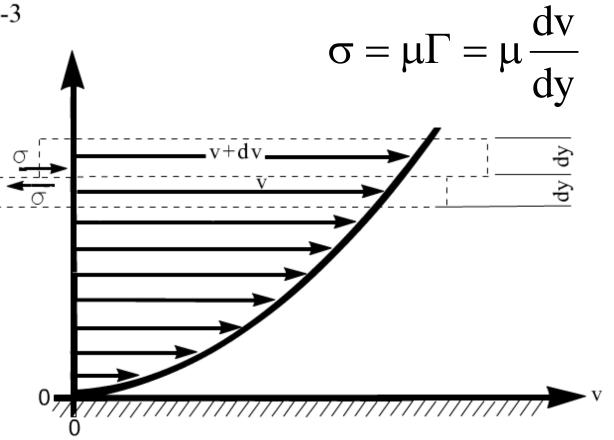
MW = 29 g/mole

Density =  $0.0075 \text{ lb/ft}^3$ 



### Viscosity

Figure 1-3



Shearing stress in a moving fluid





Intermolecular Cohesive

Forces

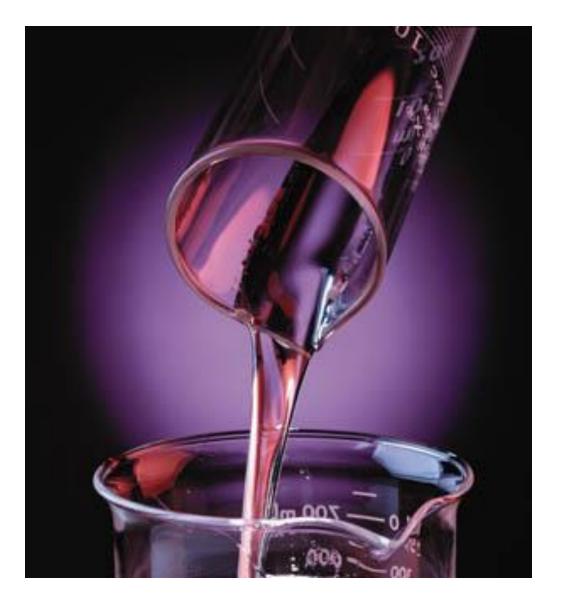
Momentum

Viscosity

Transfer

**Between the** 

Layers of Fluid







#### Heated Liquid = Lower Viscosity





Intermolecular Cohesive

Forces

Momentum

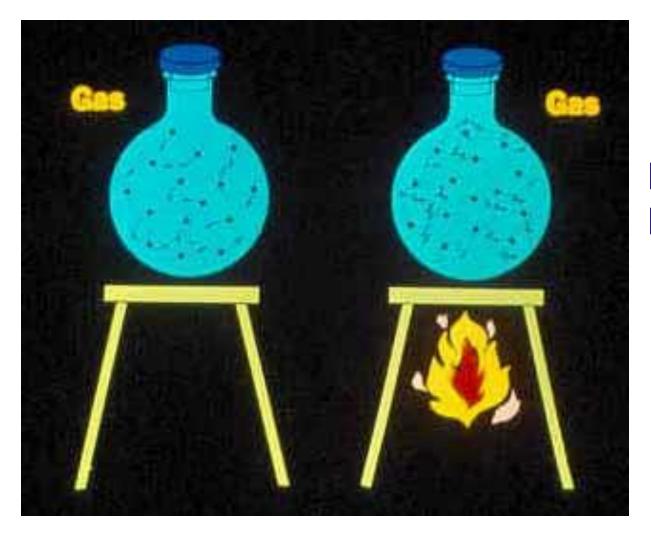
Viscosity

Transfer

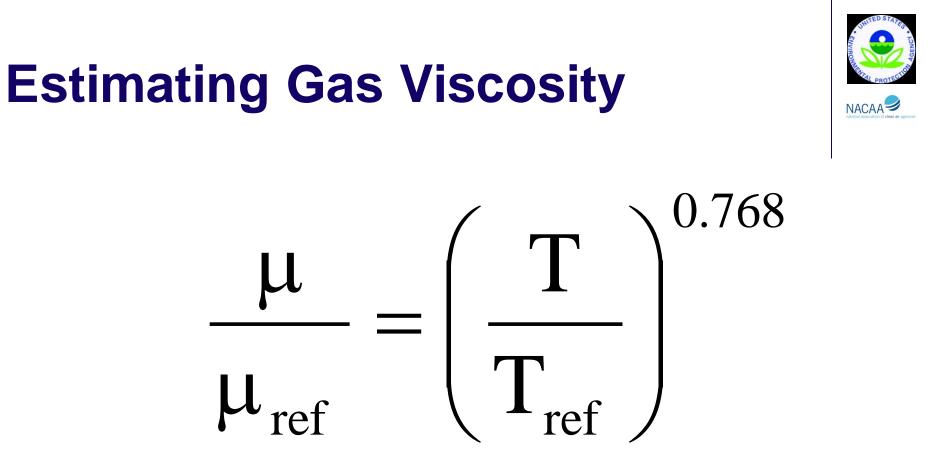
**Between the** 

Layers of Fluid





#### Heated Gas = Higher Viscosity



Viscosity of air at 68°F is 1.21 x 10<sup>-5</sup> lb<sub>m</sub>/ft-sec



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#### **Kinematic Viscosity**

# $v = \frac{\mu}{\rho}$

where

- v = kinematic viscosity
- $\mu$  = absolute viscosity
- $\rho = \text{density}$



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# $Re = \frac{Lv\rho}{\mu}$

where

Re = Reynolds Number

- = characteristic system dimension
- v = fluid velocity
- $\rho$  = fluid density
- $\mu$  = fluid viscosity

#### **Flow Reynolds Number**





# $Re = \frac{Dv\rho}{Dv}$

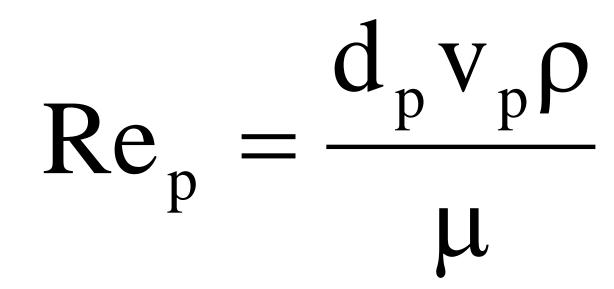
Where for a circular duct

D = duct diameter



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#### **Particle Reynolds Number**



#### Where

- $d_p$  = particle diameter
- $v_p$  = relative particle to gas velocity

Most particle motion in air pollution control devices occurs in the Stokes and Transitional Regions

### **Flow Regime**

Three flow regimes:

Rep < 1</th>laminar or Stokes flow1 < Rep < 1000</td>transition flowRep > 1000turbulent flow



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#### Example 1-5



Calculate the Particle Reynolds Number for a  $2\mu$ m diameter particle moving through 10°C still air at a velocity of 6 m/sec.

From Appendix B, the density of air at 20°C is 1.20 x 10-3 g/cm3 and the viscosity is 1.80 x 10-4 g/cm(sec)

Estimate the gas density at 10°C.

$$\rho = 1.20 \times 10^{-3} \left( \frac{293 \text{K}}{283 \text{K}} \right) = 1.24 \times 10^{-3} \frac{\text{g}}{\text{cm}^3}$$

Estimate the gas vicosity at 10°C.

$$\mu = 1.80 \times 10^{-4} \left(\frac{293 \text{K}}{283 \text{K}}\right)^{0.768} = 1.75 \times 10^{-4} \text{ g/cm} \cdot \text{sec}$$

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#### And then...

CalculateParticleReynolds Number :

$$\operatorname{Re}_{p} = \frac{d_{p}v_{p}\rho}{\mu} = \frac{(2x10^{-4} \operatorname{cm})\left(6x10^{2} \operatorname{cm}/\operatorname{sec}\right)\left(1.24x10^{-3} \frac{g}{\operatorname{cm}^{3}}\right)}{1.75x10^{-4} \frac{g}{\operatorname{cm} \cdot \operatorname{sec}}}$$

## Example 1-6

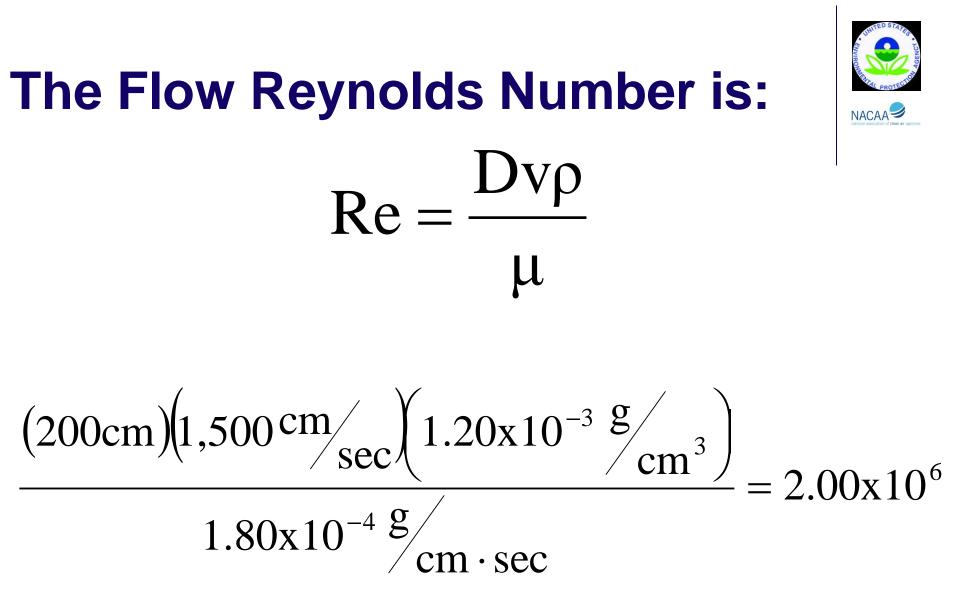


Calculate the Particle Reynolds Number for a gas stream moving through a 200 cm diameter duct at a velocity of 1,500 cm/sec.

•Assume that the particles are moving at the same velocity as the gas stream and are not settling due to gravity.

•Assume a gas temperature of 20°C and standard pressure.

Since there is no difference in velocity between the gas stream and the particle, the Particle Reynolds Number is zero.



#### Example 1-7:

The mol fraction of water in the stack gas from a combustion process contains 14 mol% water vapor. What is the dew point temperature if the total pressure is 1 atm? The Antoine constants for water are:

## A = 8.10765 B = 1750.286 C = 235.000 Solution:

At the dew point temperature:

 $P^* = Pi = yiP = 0.14(1) = 0.14$  atm or 106.4 mmHg

From the Antoine equation:

$$\log_{10} 106.4 = 8.10765 - \frac{1750.286}{T + 235.000}$$

Solve for T to obtain:  $T = 53^{\circ}C$ 



## **Review Questions:**



- 1. How does the particle Reynolds number change when the gas temperature is increased? (see page 10)
  - Increases
  - Decreases



Remains unchanged

But it is fairly complicated...

An increase in T means an increase in viscosity, also a decrease in density, and an increase in velocity.

## **Review Questions:**



2. How does the gas viscosity change as the temperature is increased? (see page 9)

Increases



- Decreases
- Remains unchanged

## **Review Problems**



1. The flows from Ducts A and B are combined into a single Duct C. The flow rate in Duct A is 5,000 scfm, the gas stream temperature is 350°F and the static pressure is -32 in WC. The flow rate in Duct B is 4,000 acfm, the gas stream temperature is 400°F and the static pressure is -35 in WC.

What is the flow rate in Duct C? Assume a barometric pressure of 29.15 in Hg. (see page 6)

## Solution #1



Calculate the absolute pressure in Duct B :

$$P = 29.15 \text{ in Hg} \left( \frac{407 \text{ in WC}}{29.92 \text{ in Hg}} \right) + (-35 \text{ in WC}) = 361.5 \text{ in WC}$$

Convert the flow in Duct B to standard conditions :

$$Q_{\rm B} = 4,000 \, {\rm acfm} \left(\frac{528^{\circ} {\rm R}}{860^{\circ} {\rm R}}\right) \left(\frac{361.5 \, {\rm in} \, {\rm WC}}{407 \, {\rm in} \, {\rm WC}}\right) = 2,181 \, {\rm scfm}$$

Combine flows :

$$Q_c = 5,000 \operatorname{scfm} + 2,181 \operatorname{scfm} = 7,181 \operatorname{scfm}$$

## **Review Problems**



- Calculate the Particle Reynolds Numbers for the following particles. Assume a gas temperature of 20°C and a pressure of 1 atm. (see page 10)
- In the particle moving at 1 ft/sec relative to the gas stream
- In the particle moving at 10 ft/sec relative to the gas stream
- In the second particle moving at 1 ft/sec relative to the gas stream
- In the formation of the second stream
  100 μm particle moving at 10 ft/sec relative to the gas stream

## Solution #2 (a & b)



a. 10  $\mu m$  particle moving at 1 ft/sec relative to the gas stream

$$\operatorname{Re}_{p} = \frac{d_{p}v_{p}\rho}{\mu} = \frac{\left(10x10^{-4} cm\right)\left[\left(1.0 \frac{ft}{\operatorname{sec}}\right)\left(30.48 \frac{cm}{ft}\right)\right]\left(1.20x10^{-3} \frac{g}{cm^{3}}\right)}{1.80x10^{-4} \frac{g}{cm \cdot \operatorname{sec}}} = 0.203$$

b. 10  $\mu m$  particle moving at 10 ft/sec relative to the gas stream

$$\operatorname{Re}_{p} = \frac{d_{p}v_{p}\rho}{\mu} = \frac{\left(10x10^{-4} cm\right)\left[\left(10.0 \frac{ft}{\operatorname{sec}}\right)\left(30.48 \frac{cm}{ft}\right)\right]\left(1.20x10^{-3} \frac{g}{\operatorname{cm}^{3}}\right)}{1.80x10^{-4} \frac{g}{\operatorname{cm} \cdot \operatorname{sec}}} = 2.032$$

## Solution #2 (c & d)



c. 100  $\mu\text{m}$  particle moving at 1 ft/sec relative to the gas stream

$$\operatorname{Re}_{p} = \frac{d_{p}v_{p}\rho}{\mu} = \frac{\left(100x10^{-4} cm\right) \left[\left(1.0 \frac{ft}{\operatorname{sec}}\right) \left(30.48 \frac{cm}{ft}\right)\right] \left(1.20x10^{-3} \frac{g}{cm^{3}}\right)}{1.80x10^{-4} \frac{g}{cm \cdot \operatorname{sec}}} = 2.03$$

d. 100  $\mu\text{m}$  particle moving at 10 ft/sec relative to the gas stream

$$\operatorname{Re}_{p} = \frac{d_{p}v_{p}\rho}{\mu} = \frac{\left(100x10^{-4} cm\right)\left[\left(10.0 \frac{ft}{\operatorname{sec}}\right)\left(30.48 \frac{cm}{ft}\right)\right]\left(1.20x10^{-3} \frac{g}{cm^{3}}\right)}{1.80x10^{-4} \frac{g}{cm} \cdot \operatorname{sec}} = 20.3$$

## Chapter 2



## Particulate Matter Formation and Regulation

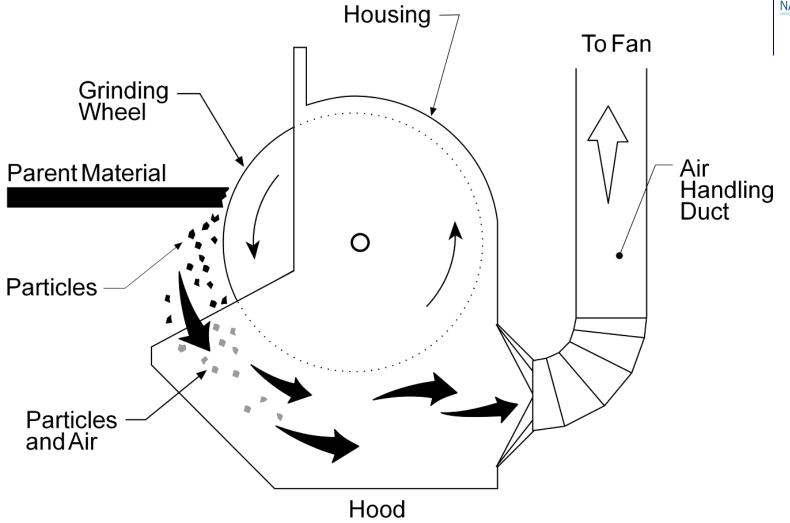
#### **Particle Formation Mechanisms**



- Physical attrition/mechanical dispersion
- Combustion particle burnout
- Homogeneous condensation
- Heterogeneous nucleation
- Droplet evaporation

## Grinding Wheel





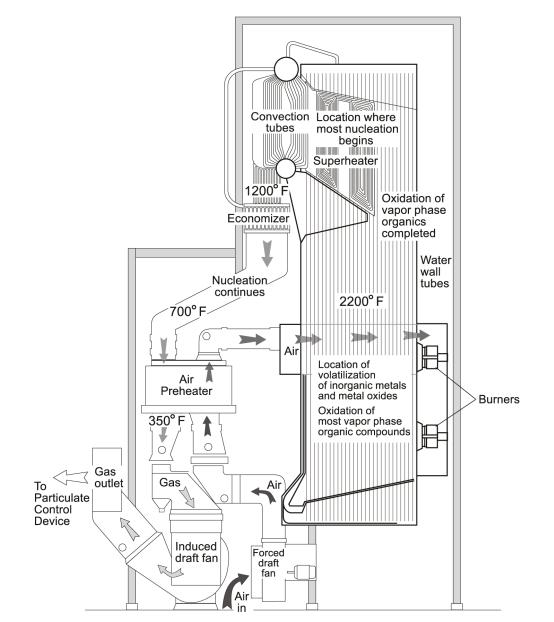
#### **Tertiary Crusher**





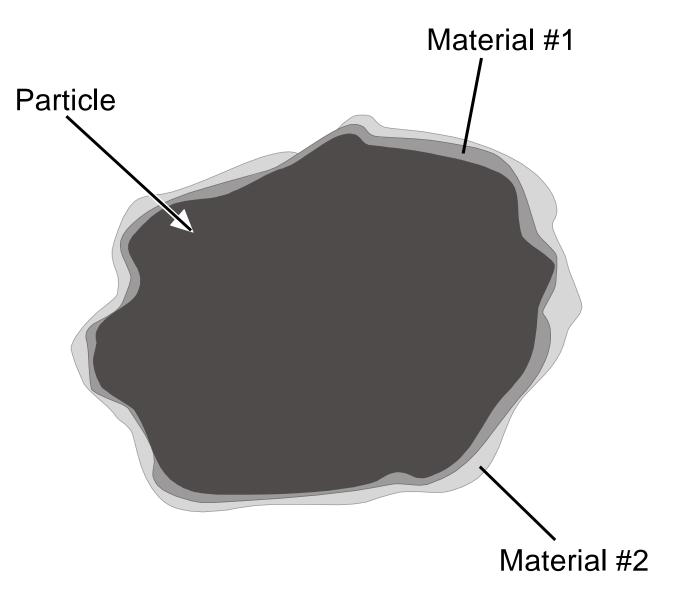


#### **Combustion Process**



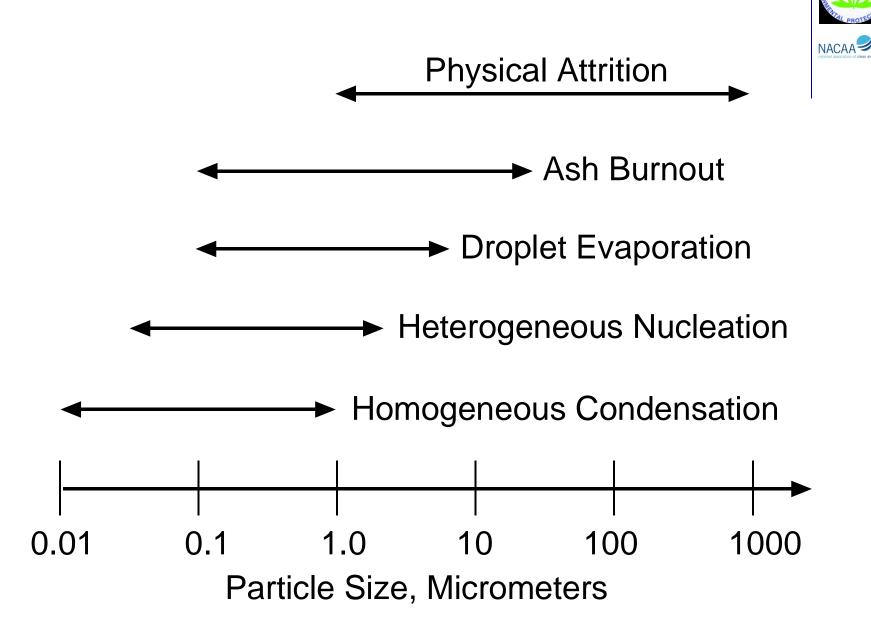


#### Heterogeneous Nucleation





#### Summary of Formation Mechanisms



#### Sources of Particulate Matter



Primary particulate matter
 Secondary particulate matter
 Condensation particles
 Reaction particles

# Particulate Matter Size Range Definitions

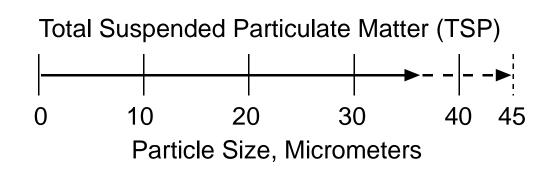


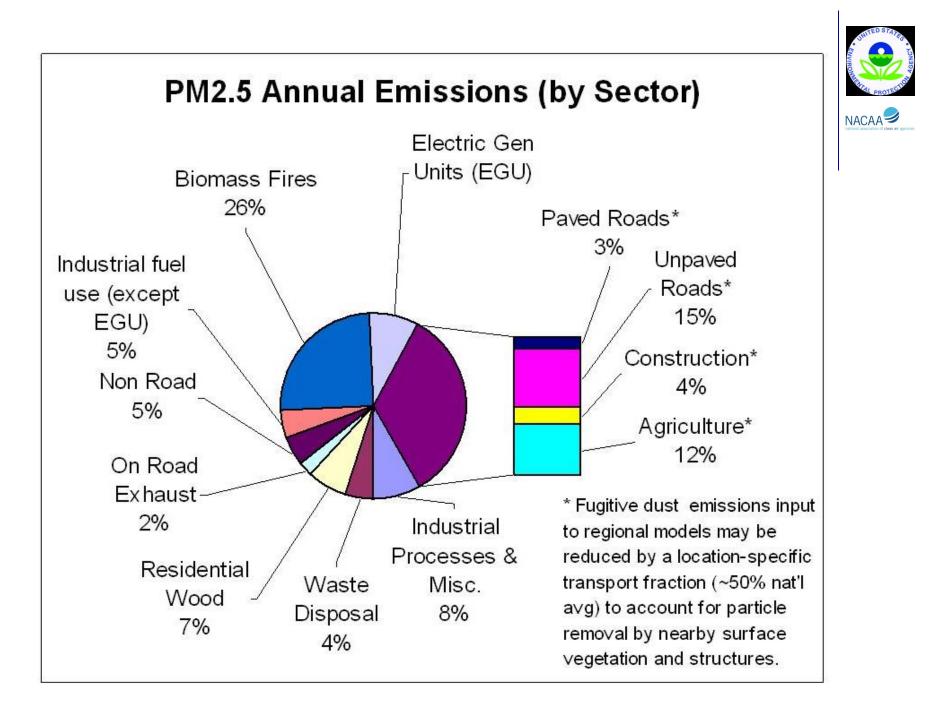
Note:

Actual particle size range included as TSP varied from 35 to 45 micrometers due to ambient monitor differences.

→ PM<sub>2.5</sub>

► PM<sub>10</sub>





#### Particulate Matter Regulation





#### **Particulate Matter Regulation**



## Before the Clean Air Act 1600s 1950s Clean Air Act Amendments of 1970 NAAQS SIPs NSPS

Summary of NAAQS for  $PM_{10}$  and  $PM_{2.5}$  (2006 revision of the 24-hour standard)

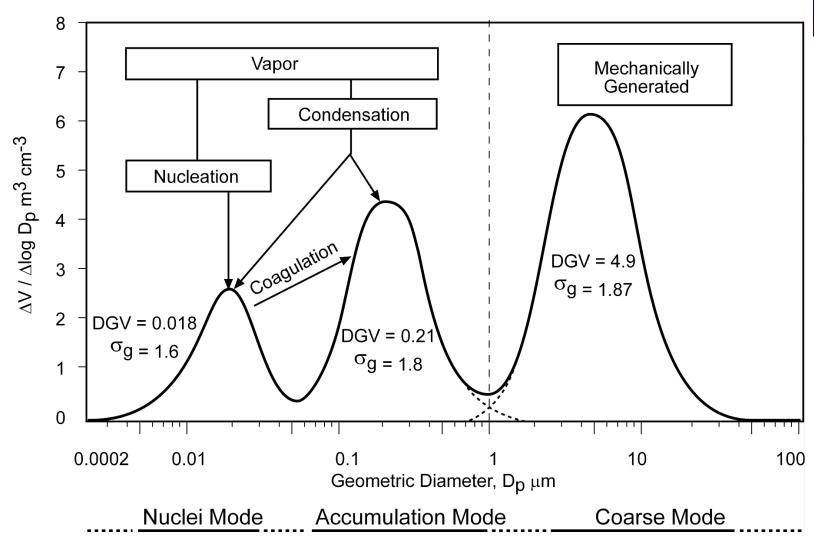


Pollutant	Health-based Standard	
	Type of Average	Concentration
<b>PM</b> <sub>10</sub>	Annual Arithmetic Mean	<b>50</b> μ <b>g/m</b> <sup>3</sup>
	24-hour <sup>a</sup>	<b>150</b> μ <b>g/m</b> <sup>3</sup>
<b>PM</b> <sub>2.5</sub>	Annual Arithmetic Mean	<b>15</b> μ <b>g/m<sup>3 b</sup></b>
	24-hour <sup>c</sup>	<b>35</b> μ <b>g/m</b> <sup>3</sup>

a) not to be exceeded more than once per year on average over a three year periodb) three-year average of the annual averagec) determined from the 98th percentile, averaged over three years

# Typical Ambient Particle Size Distribution





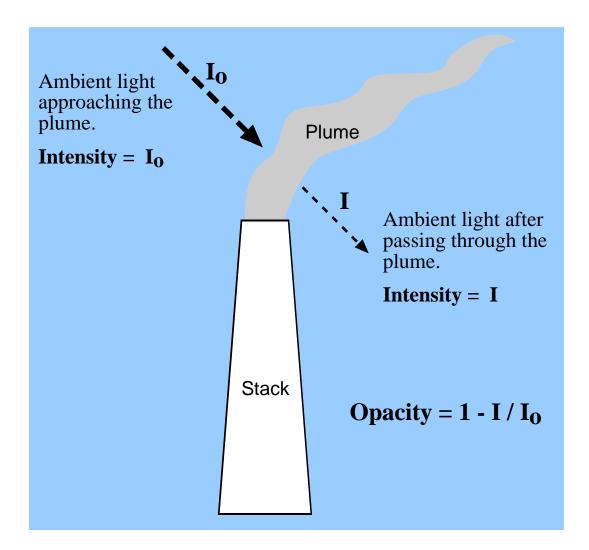
## State Implementation Plans

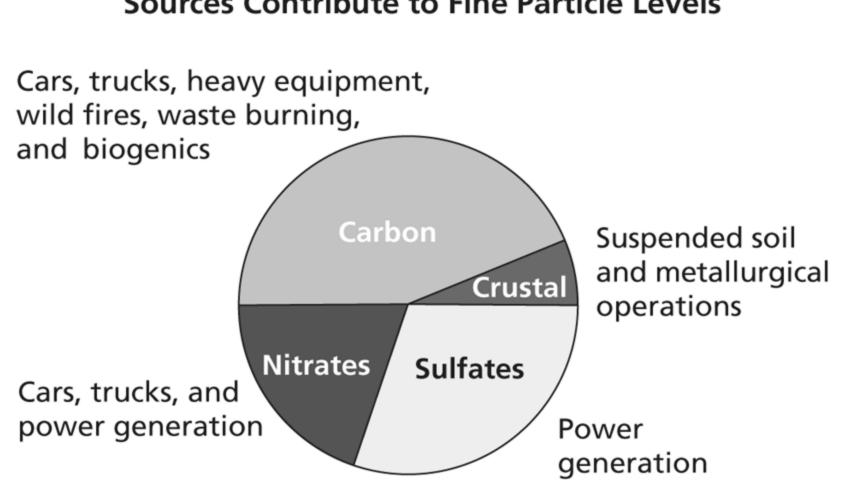


Fuel burning regulations
Process weight regulations
Opacity limitations

## **Plume Opacity**



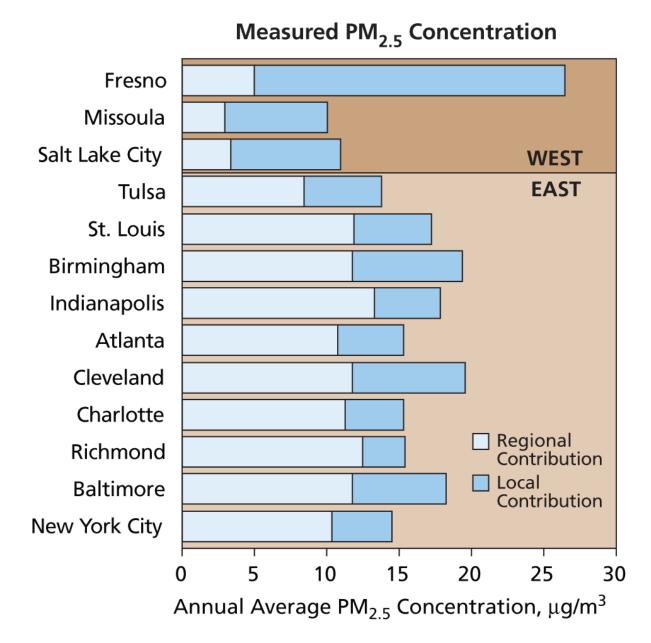




#### Where does it all come from?

Automobiles, Power Generation, and Other Sources Contribute to Fine Particle Levels







#### Clean Air Act Amendments of 1977



Case-by-Case Permit Reviews
PSD and BACT
NSR and LAER

## Standards for Hazardous Air Pollutants



Clean Air Act of 1970
 Clean Air Act of 1990

 189 hazardous pollutants

 NESHAPS vs NSPS/BACT/LAER
 MACT

Clean Air Act Amendments and Visibility

- Class I areas
- Regional Haze Rule
- BART
- Implementation plans
  - 2007
  - 10 year periodic plans



#### **Title V Operating Permits**

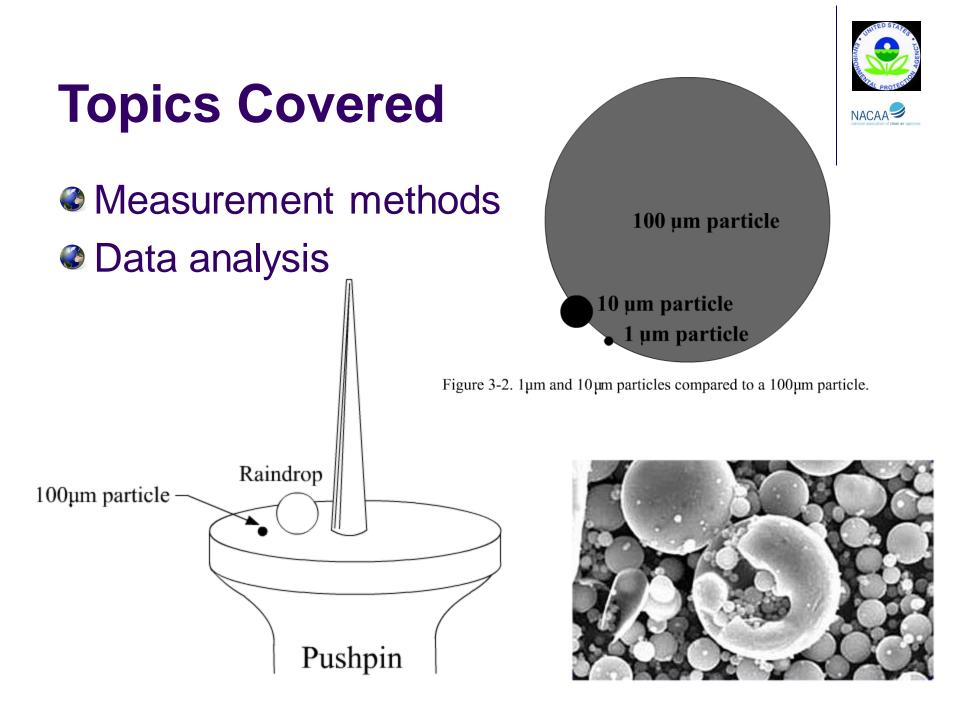


- What is Title V
- Title V and the public
- Title V requirements



## **Chapter 3**





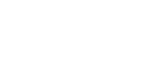
## Particle Size and Air Pollution Control

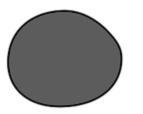


Table 3-1. Spherical Particle Diamete, Volume, and Surface Area			
Diameter ( m)	Volume (cm <sup>3</sup> )	Area (cm <sup>2</sup> )	
0.1	5.23 x 10 <sup>-16</sup>	3.14 x 10 <sup>-10</sup>	
1.0	5.23 x 10 <sup>-13</sup>	3.14 x 10 <sup>-8</sup>	
10.0	5.23 x 10 <sup>-10</sup>	3.14 x 10 <sup>-6</sup>	
100.0	5.23 x 10 <sup>-7</sup>	3.14 x 10 <sup>-4</sup>	
1,000.0	5.23 x 10 <sup>-4</sup>	3.14 x 10 <sup>-2</sup>	

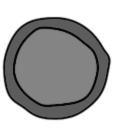


#### **Particle Size?**





Solid Sphere

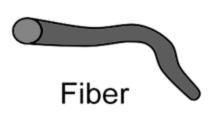


Hollow Sphere



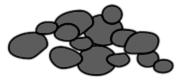
Solid Irregular

Flake





**Condensation Floc** 



Aggregate

#### **Aerodynamic Diameter**

The diameter of a sphere with a density of 1 g/cm<sup>3</sup> that has the same falling velocity in air as the actual particle

# $d_p = d_{\sqrt{\rho_p C_c}}$



### **Measurement Methods**

- Microscopy
- Optical counters
- Electrical aerosol analyzer
- Bahco analyzer
- Cascade impactors

## **Ideal Measuring Device**

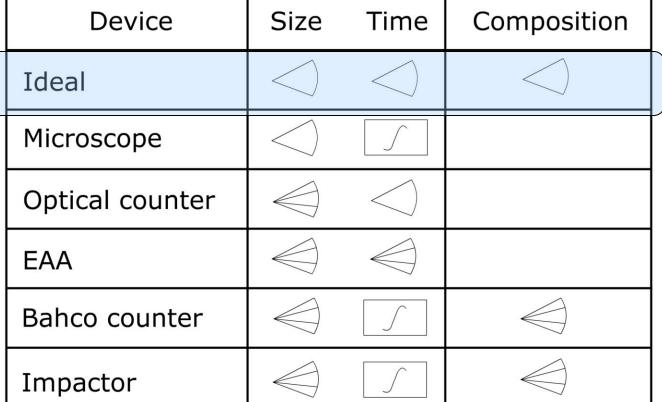


- Measure the exact size of each particle
- Determine the composition of each particle
- Report real-time data instantaneously

#### Figure 3-12. Comparison of particle sizing devices



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Single particle level



Discrete ranges



Intergrated averaging process

## Microscopy

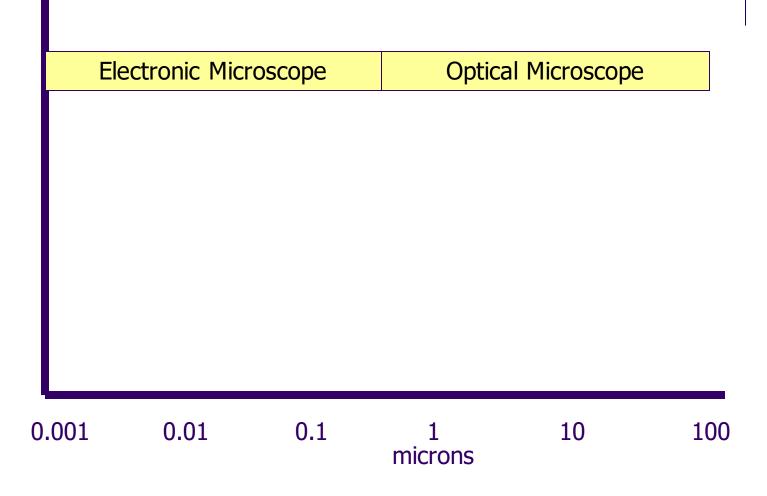


Polarized Light Microscopy

**Scanning Electron Microscopy** 

Energy Dispersive X-Ray Spectroscopy







#### Figure 3-12. Comparison of particle sizing devices

Device	Size	Time	Composition	
 Ideal	$\langle \rangle$	$\bigcirc$	$\langle$	
Microscope	$\langle \rangle$			
Optical counter		$\langle \rangle$		
EAA				
Bahco counter				
Impactor		$\int$		

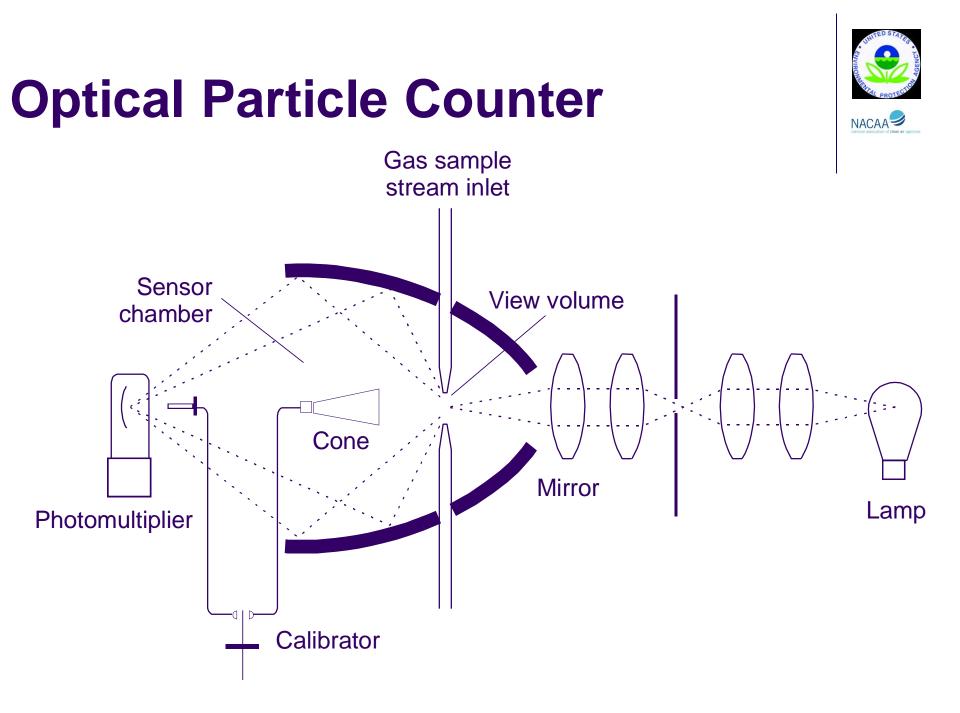


Single particle level

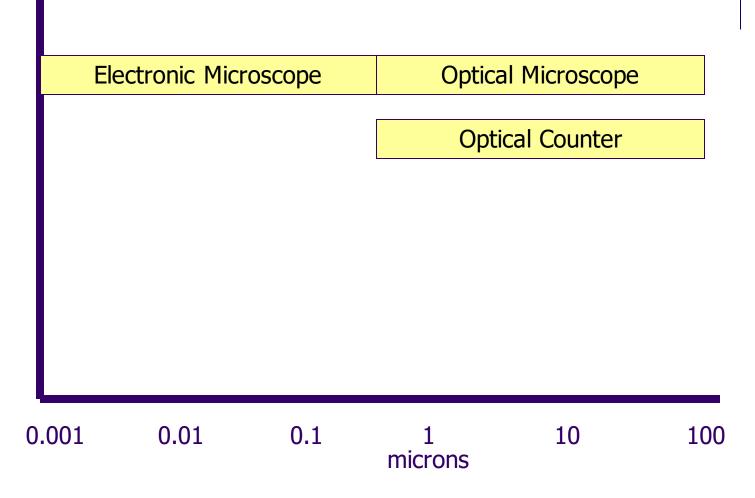


Discrete ranges

Intergrated averaging process









#### Figure 3-12. Comparison of particle sizing devices

Device	Size	Time	Composition	
Ideal	$\langle \rangle$	$\bigcirc$	$\langle$	
Microscope	$\langle \rangle$			
Optical counter		$\langle \rangle$		
EAA				
Bahco counter				
Impactor				



Single particle level

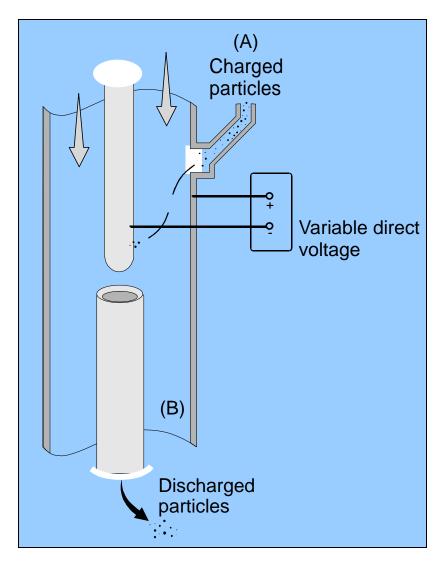
Discrete ranges

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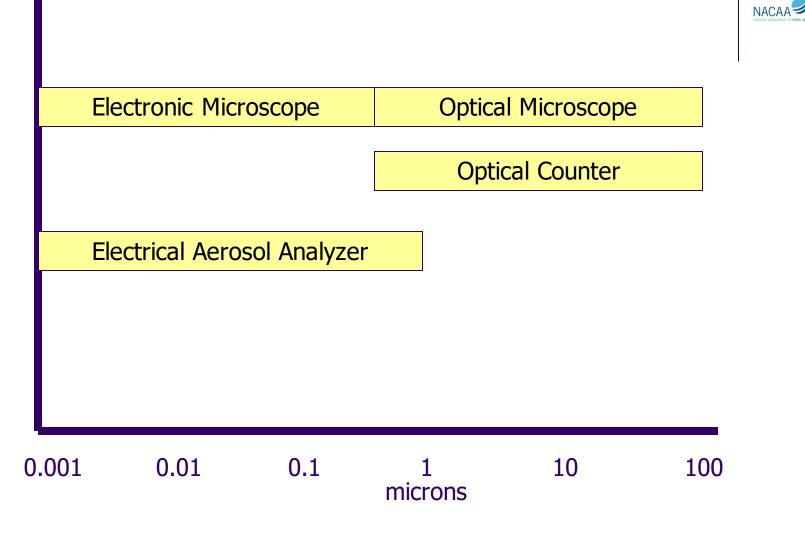
Intergrated averaging process



## **Electrical Aerosol Analyzer**

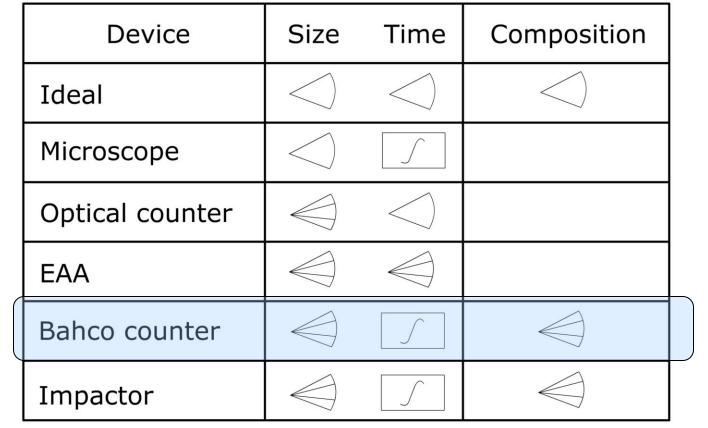






#### Figure 3-12. Comparison of particle sizing devices





NACAA

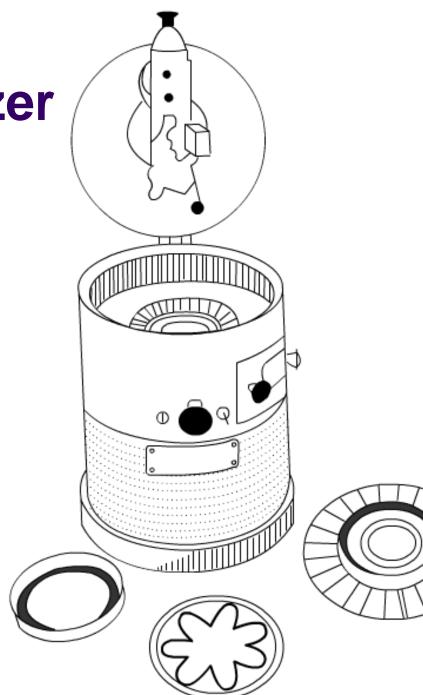


Single particle level

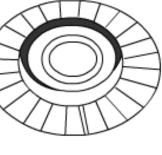
Discrete ranges

Intergrated averaging process

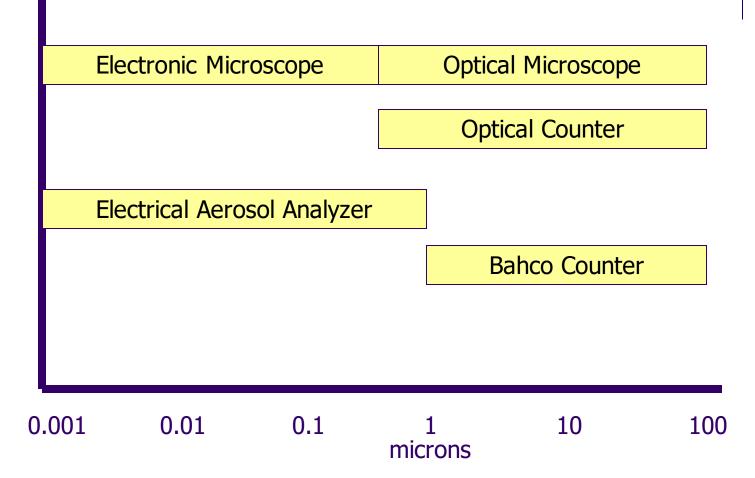
#### **Bahco Analyzer**













#### Figure 3-12. Comparison of particle sizing devices

Device	Size	Time	Composition
Ideal	$\langle \rangle$	$\langle \rangle$	$\langle \rangle$
Microscope	$\langle \rangle$		
Optical counter		$\langle \rangle$	
EAA			
Bahco counter			
Impactor			



Single particle level

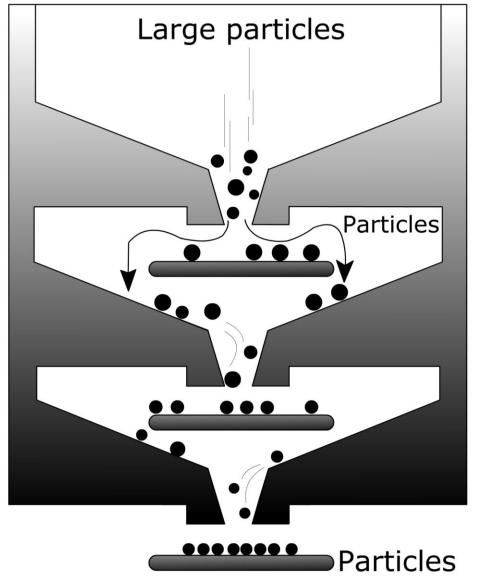
🗐 Disc

Discrete ranges

Intergrated averaging process

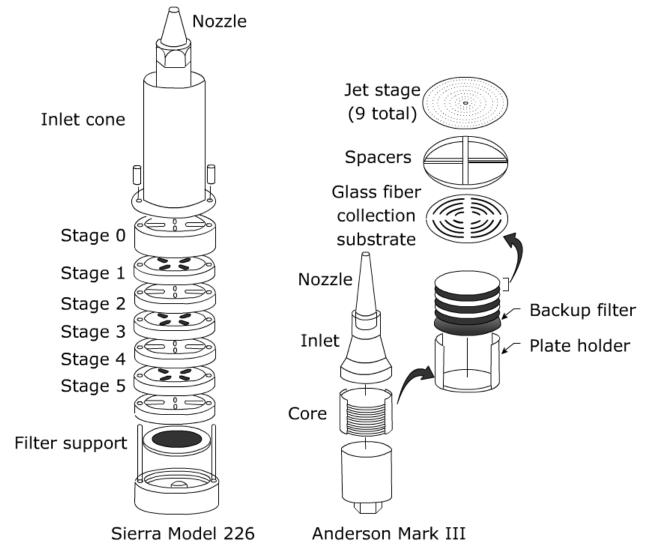


#### **Cascade Impactor**

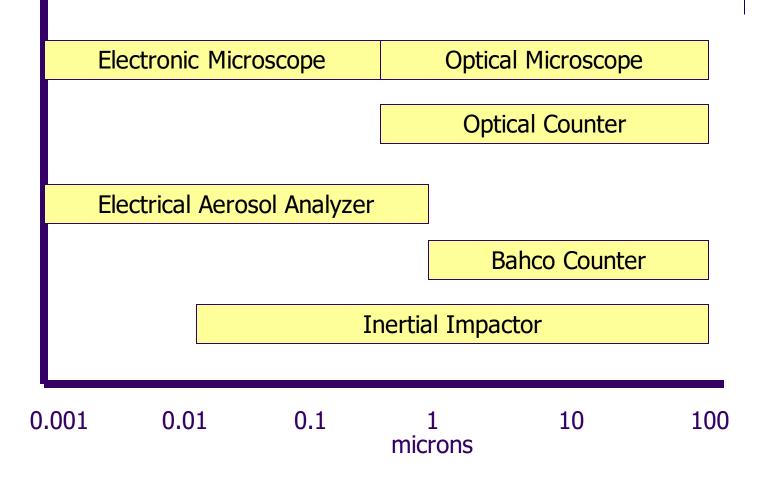


#### **Cascade Impactors**



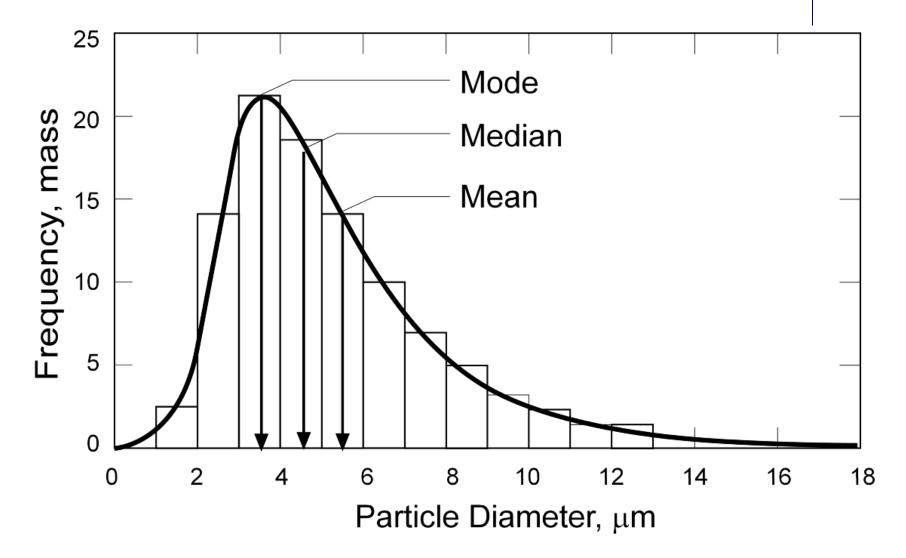






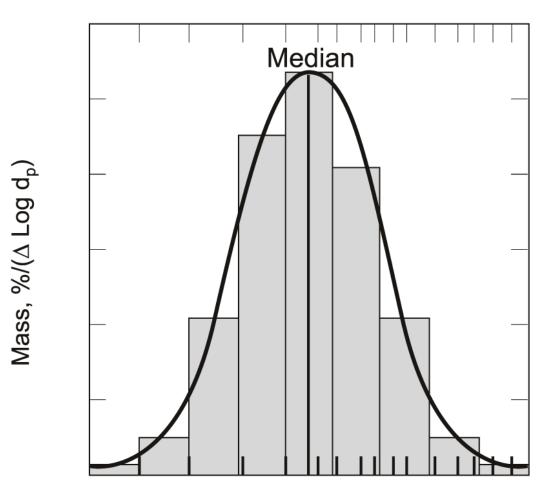


#### **Data Analysis**

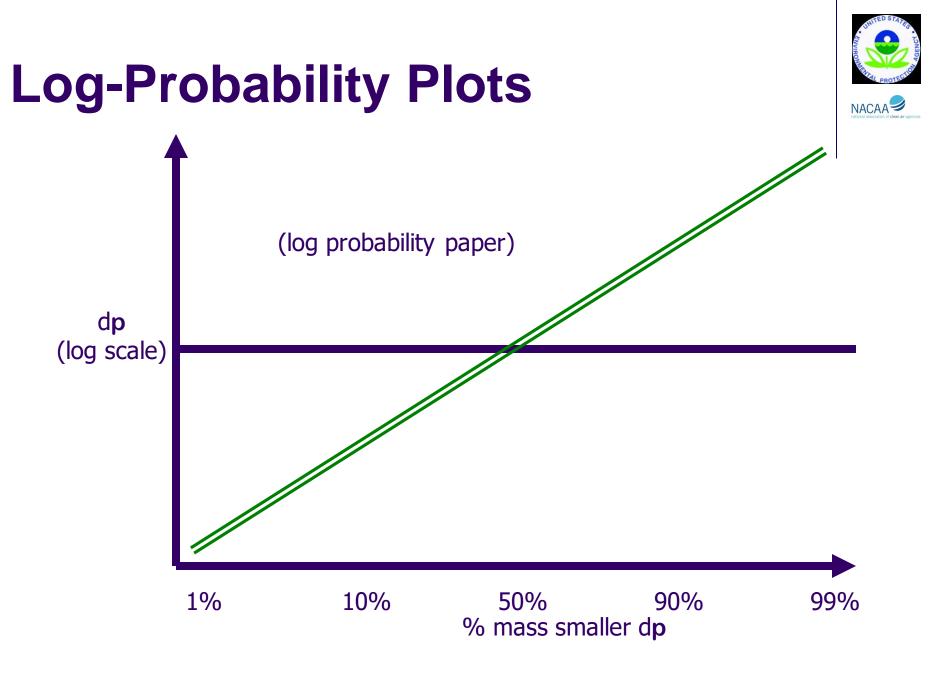




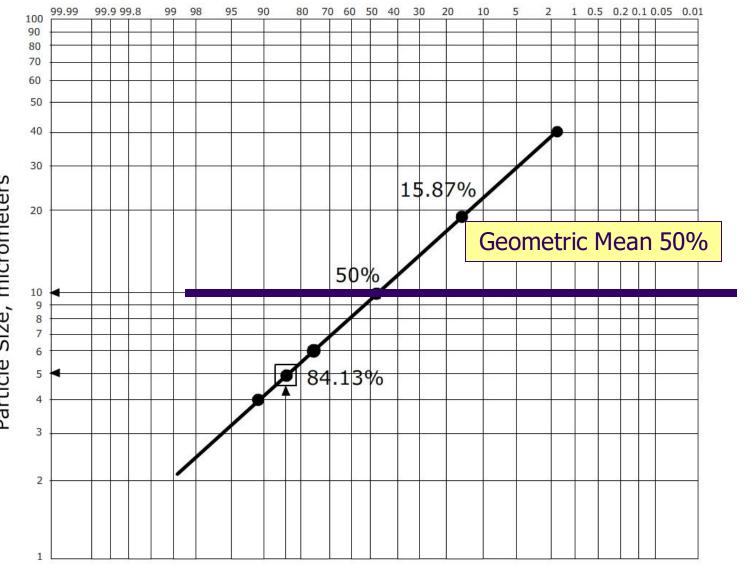
## **Log-Normal Distribution**



Particle Diameter,  $\mu m$ 



9.99	99	.9 99 	9.8	99	99 	8	95	9	<u>s</u>	30		0			40	30	) 2	20	10		2	1	7.5	0.2	2 0.	.10	.05	0.0	UNITED
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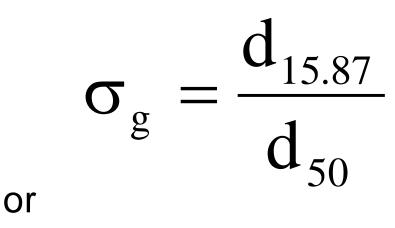


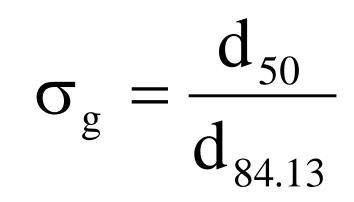
Cumulative % Smaller Than dp Max

Particle Size, micrometers



#### **Geometric Standard Deviation**





#### Example 3-1



Determine the mass mean diameter and the geometric standard deviation of the particle collection represented by the following distribution:

Size Range (gm)	Mass (mg)
<2	1.0
2 to 4	14.5
4 to 6	24.7
6 to 10	59.8
10 to 20	68.3
20 to 40	28.9
>40	2.8

## Solution...

Refer to the table. Determine the total
mass and calculate the percentage in each size range.

- 2. Starting with the size range for the smallest particles (<2 mm), subtract the percent mass in that range (0.50%) from 100.00 to determine the cumulative percent mass greater than 2 mm (99.50%).
- 3. For each subsequent size range, subtract the percent mass in that range from the cumulative percent mass of the previous size range to determine the cumulative percent mass less than d<sub>p</sub> max for that size range.

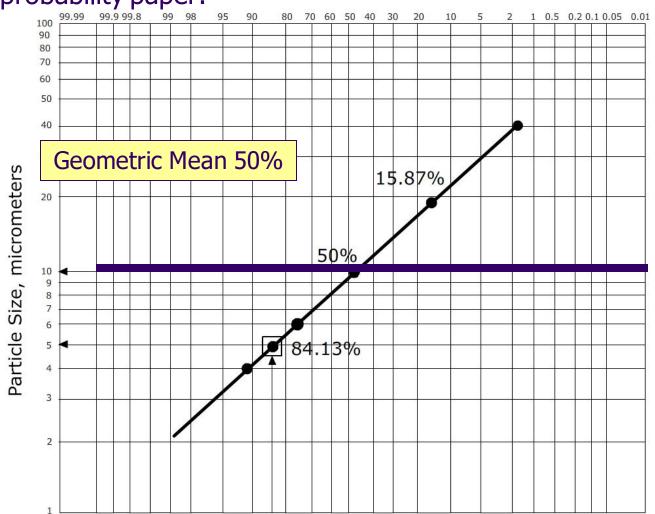
Example Particle Size Data									
Size Range (µm)	Mass (mg)	% Mass in Size Range	Cumulative % Mass Less Than dp max						
<2	1.0	0.50	99.50						
2 to 4	14.5	7.25	92.25						
4 to 6	24.7	12.35	79.90						
6 to 10	59.8	29.90	50.00						
10 to 20	68.3	34.15	15.85						
20 to 40	28.9	14.45	1.40						
>40	2.8	1.40							
TOTAL	200.0	100.0							

For example, for the 2-4  $\mu$ m size range, 99.50% - 7.25% = 92.25%, the cumulative percent mass less than 4 mm.



## And then...

Plot d<sub>p</sub>max versus Cumulative Percent Mass Smaller Than d<sub>p</sub>max on log-probability paper:

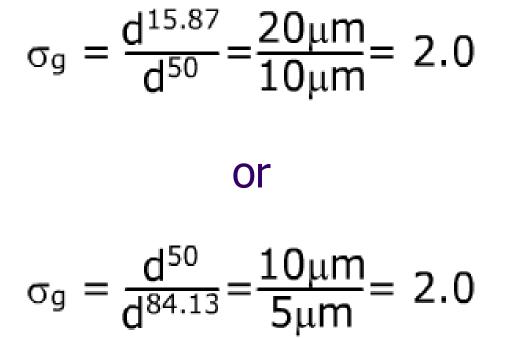


Cumulative % Smaller Than  $d_p$  Max





The mass mean particle diameter is found at the 50th percentile and is 10 mm. The geometric standard deviation is calculated from:





#### Finally...

#### **Review Questions**



1. Calculate the aerodynamic diameter of a spherical particle having a true diameter of 2  $\mu$ m and a density of 2.7 g/cm<sup>3</sup>.

#### Solution:

Assume that the Cunningham slip correction factor is 1.

$$d_p = d_{\sqrt{p_p C_c}} = 2\sqrt{(2.7)(1.0)} = 3.29 \mu m$$

#### **Review Questions**

- 2. Given the following distributions:
- Is either distribution lognormal?
- If yes, what is the geometric mass mean diameter and the geometric standard deviation?

Size Range (µm)	Sample A Mass (mg)	Sample B Mass (mg)
<0.6	25.50	8.50
0.6 to 1.0	33.15	11.05
1.0 to 1.2	17.85	7.65
1.2 to 3.0	102.00	40.80
3.0 to 8.0	63.75	15.30
8.0 to 10.0	5.10	1.69
>10.0	7.65	0.01





## Solution #2 (a)

Size Range (gm)	Mass (mg)	Percent Mass in Size Range	Cumulative Percent Mass Less Than d <sub>p</sub> max
<0.6	25.50	10	90
0.6 to 1.0	33.15	13	77
1.0 to 1.2	17.85	7	70
1.2 to 3.0	102.00	40	30
3.0 to 8.0	63.75	25	5
8.0 to 10.0	5.10	2	3
>10.0	7.65	3	
TOTAL	255.0	1 00 . 0	

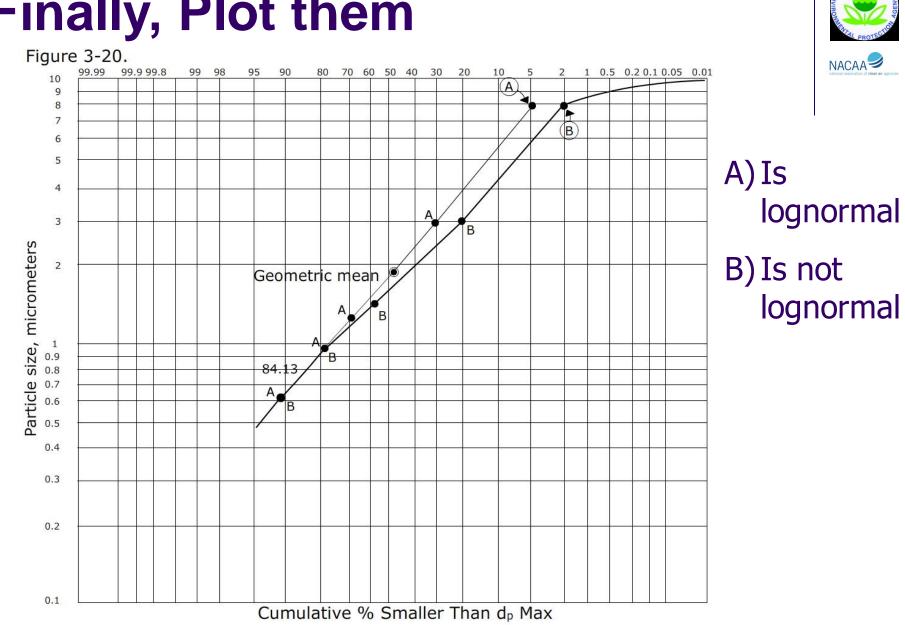
#### But wait there is more



## Solution #2 (b)

Size Range (gm)	Mass (mg)	Percent Mass in Size Range	Cumulative Percent Mass Less Than d <sub>p</sub> max
<0.6	8.50	10	90
0.6 to 1.0	11.05	13	77
1.0 to 1.2	7.65	9	68
1.2 to 3.0	40.80	48	20
3.0 to 8.0	15.30	18	2
8.0 to 10.0	1.69	1.99	0.01
>10.0	0.01	0.01	
TOTAL	85.0	100.0	

#### But wait there is more



### Finally, Plot them

But wait there is more





#### And finally...

The geometric mass mean diameter and the geometric standard deviations for Sample A are:

$$d_{50} = 1.9\,\mu m$$
  
$$\sigma_g = \frac{d_{50} = 1.9\,\mu m}{d_{50} = 0.8\,\mu m} = 2.4$$

# **Chapter 4**





# **Collection Mechanisms**



- Gravitational settling
- Centrifugal inertial force
- Inertial impaction
- Brownian motion
- Electrostatic attraction
- Thermophoresis
- Diffusiophoresis

#### **Particle Motion**



# $\Sigma F = m_{p}a_{p} = m_{p} \frac{dv_{p}}{dt}$

where

 $\Sigma F$  = sum of all forces acting on the particle (g-cm/sec<sup>2</sup>)

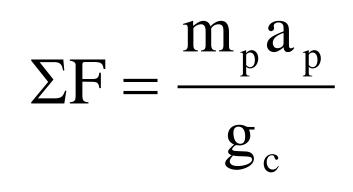
$$m_p = mass of the particle (g)$$

- $a_p$  = acceleration of the particle (cm/sec<sup>2</sup>)
- $v_p$  = velocity of the particle (cm/sec)
- t = time (sec)

cgs units given, but any consistent set of units is ok

### **English System Units**





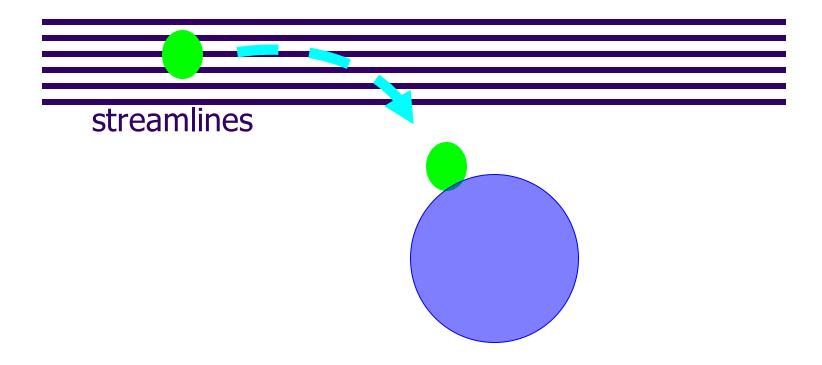
where

- $\Sigma F$  = sum of all forces acting on the particle (lb<sub>f</sub>)
- $m_p$  = mass of the particle ( $lb_m$ )
- $a_p$  = acceleration of the particle (ft/sec<sup>2</sup>)

$$g_{c} = 322 \frac{lb_{m}ft}{lb_{f}sec^{2}}$$

#### **Gravitational Settling**





#### **Forces on a Particle**



- Gravitational force
- Buoyant force
- Drag force

**Gravitational Force** 



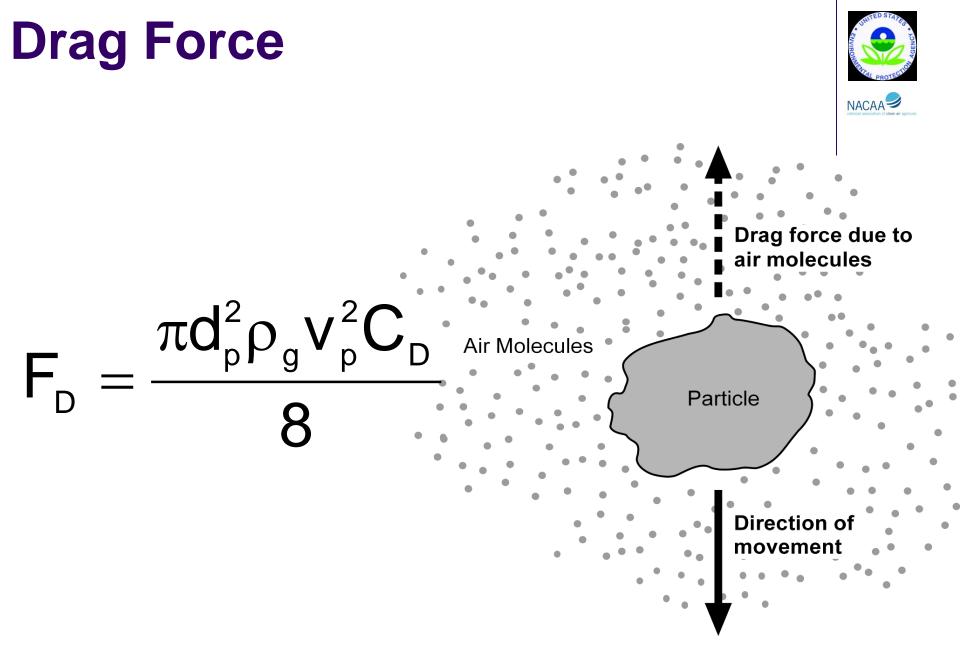
 $F_G = m_p g = \rho_p V_p g$  $V_p = \frac{\pi d_p^3}{\kappa}$  $= \frac{\pi d_p^3 \rho_p g}{2}$ F<sub>G</sub>





# $F_{\rm B} = m_{\rm g}g = \rho_{\rm g}V_{\rm p}g$

# $F_{\rm B} = \frac{\pi d_p^3 \rho_g g}{6}$

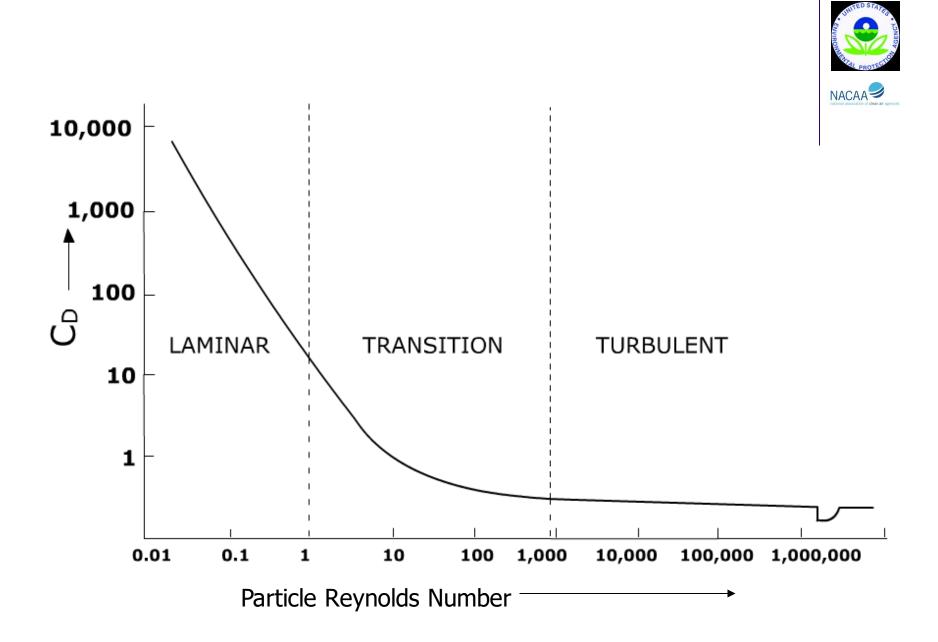






#### $C_{\mathsf{D}}$ is a function of the particle Reynolds number

 $\operatorname{Re}_{p} = \frac{d_{p}v_{p}\rho_{g}}{d_{p}v_{p}\rho_{g}}$ ′ g





Laminar (Re<sub>p</sub><1)</p>  $C_{D} = \frac{24}{Re_{p}}$ 

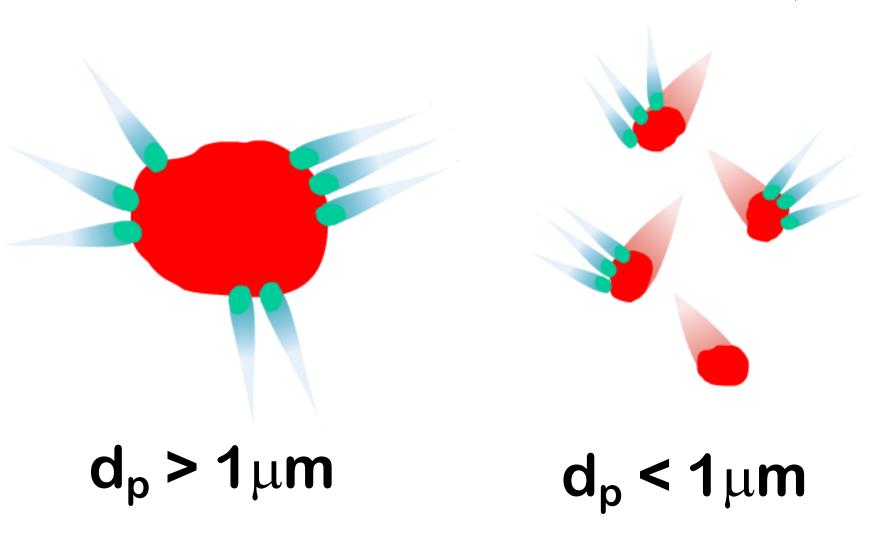
- Transition (1<Re<sub>p</sub><1,000)</p>
- $C_{\rm D} = \frac{18.5}{{\rm Re}_{\rm p}^{0.6}}$ • Turbulent (Re<sub>p</sub>>1,000)

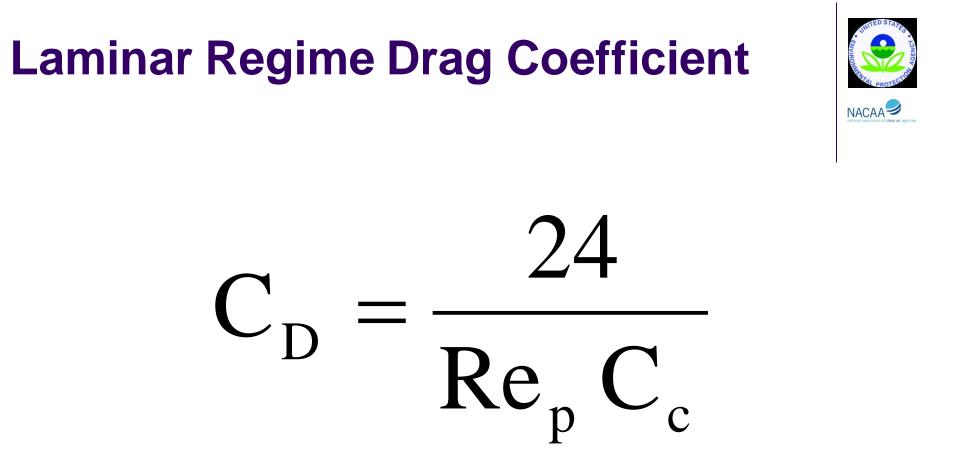
$$C_{\rm D} = 0.44$$

#### Laminar Regime

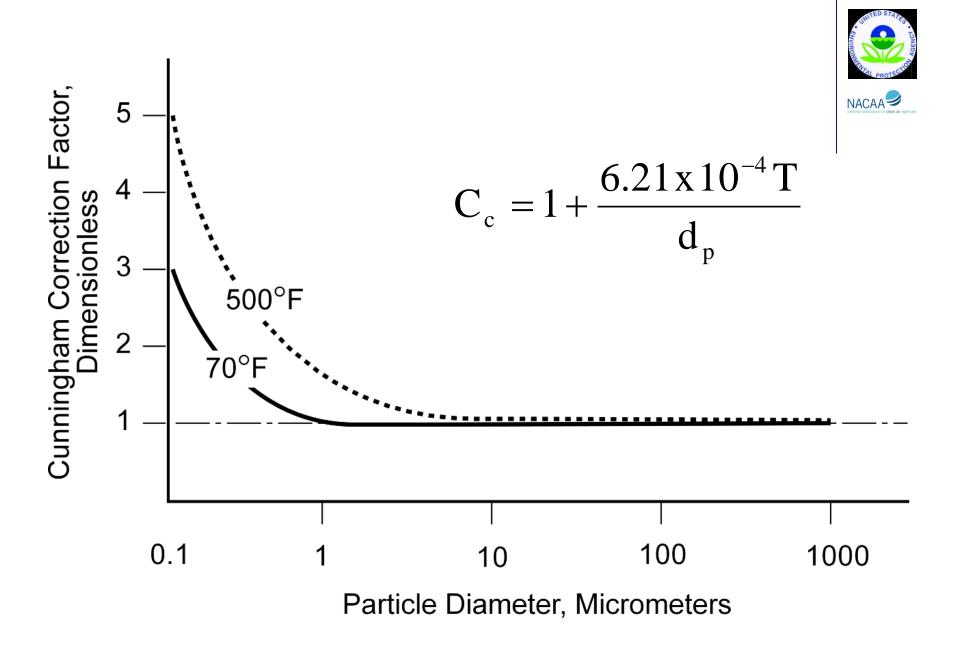








#### C<sub>c</sub> is the Cunningham slip correction factor







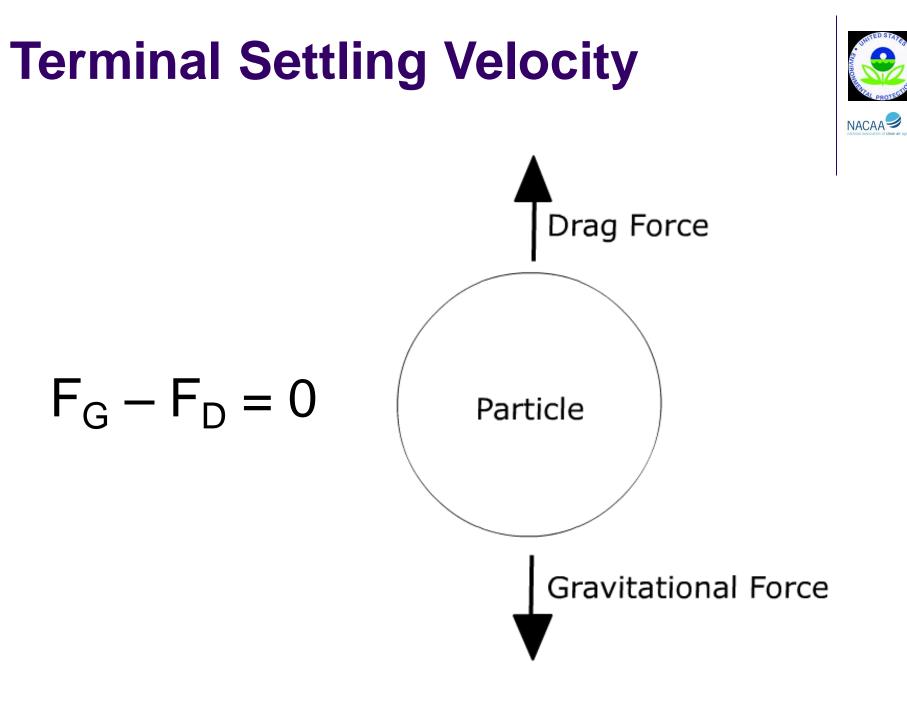
$$F_{\rm D} = \frac{3\pi\mu_{\rm g} v_{\rm p} d_{\rm p}}{C_{\rm c}}$$

Transition (1<Re<sub>p</sub><1,000)</p>

$$F_{\rm D} = 2.31\pi \left(d_{\rm p} v_{\rm p}\right)^{1.4} \mu_{\rm g}^{0.6} \rho_{\rm g}^{0.4}$$

Turbulent (Re<sub>p</sub>>1,000)

$$F_{\rm D} = 0.055\pi \left(d_{\rm p} v_{\rm p}\right)^2 \rho_{\rm g}$$



#### Terminal Settling Velocity Laminar Regime



 $v_{t} = \frac{g C_{c} \rho_{p} d_{p}^{2}}{18 \mu_{g}}$ 

# **Terminal Settling Velocity**

#### **Transition Regime**



# $v_{t} = \frac{0.153 g^{0.71} \rho_{p}^{0.71} d_{p}^{1.14}}{\mu_{g}^{0.43} \rho_{g}^{0.29}}$

#### Terminal Settling Velocity Turbulent Regime



# $v_{t} = 1.74 \left( \frac{g \rho_{p} d_{p}}{\rho_{g}} \right)^{0.5}$

# **Determination of Flow Regime**



$$\mathbf{K} = \mathbf{d}_{p} \left( \frac{g \rho_{p} \rho_{g}}{\mu_{g}^{2}} \right)^{0.33}$$

where

 $\begin{array}{l} g = \mbox{acceleration of particle due to gravity (980 cm/sec^2)} \\ \rho_p = \mbox{particle density (g/cm3)} \\ \mu_g = \mbox{gas viscosity (g/(cm \cdot sec))} \\ d_p = \mbox{physical particle diameter (cm)} \\ \rho_q = \mbox{gas density (g/cm^3)} \end{array}$ 

Don't get wrapped up in the units; any consistent set of units is ok.





Laminar region	K<2.62
Transitional region	2.62 <k<69.12< td=""></k<69.12<>
Turbulent region	K>69.12

Terminal Settling Velocities of Unit Density Spheres at 25°C		
Particle Size (µm)	Terminal Settling Velocity at 25°C (cm/sec)	<b>Flow Condition</b>
0.1	0.000087	Laminar
1.0	0.0035	Laminar
10.0	0.304	Laminar
50.0	7.5	Laminar
80.0	19.3	Laminar
100	31.2	Transitional
200	68.8	Transitional
1,000	430.7	Transitional
10,000	1,583	Turbulent
100,000	5,004	Turbulent

## Example 4-1

Calculate the terminal settling velocity in 20°C air of a 45  $\mu$ m diameter particle with a density of 1 g/cm<sup>3</sup>.



#### **Solution**

Calculate K to determine the flow region :

$$K = d_{\rho} \left(\frac{gp_{\rho}p_{g}}{\mu_{g}^{2}}\right)^{0.33} = 45 \times 10^{-4} \text{ cm} \left[\frac{\left(980 \text{ cm}/\text{sec}^{2}\right)\left(1.0 \frac{g}{\text{cm}^{3}}\right)\left(1.20 \times 10^{-3} \frac{g}{\text{cm}^{3}}\right)}{\left(1.80 \times 10^{-4} \frac{g}{\text{cm}^{3}} \times \text{sec}^{2}\right)^{2}}\right] = 1.35$$

Assume  $C_c = 1.0$ 

$$v_{t} = \frac{gC_{c}p_{\rho}}{18\mu8} = \frac{\left(980 \text{ cm/sec}^{2}\right) \cdot 0\left(1.0 \frac{g}{\text{cm}^{3}}\right) \left(45 \times 10^{-3} \frac{g}{\text{cm}^{3}}\right)^{2}}{18 \left(1.80 \times 10^{-4} \frac{g}{\text{cm}^{3}} \times \text{sec}\right)} = 6.13 \text{ cm/sec}$$



Calculate the terminal settling velocity in 20°C air of a 2  $\mu$ m diameter particle with a density of 1 g/cm<sup>3</sup>.

#### Solution

Calculate K to determine the flow region :

$$K = d_{\rho} \left(\frac{gp_{\rho}p_{g}}{\mu_{g}^{2}}\right)^{0.33} = 2x10^{-4} \text{ cm} \left[\frac{\left(980 \text{ cm}/\text{sec}^{2}\right)\left(1.0 \text{ g}/\text{cm}^{3}\right)\left(1.20x10^{-3} \text{ g}/\text{cm}^{3}\right)}{\left(1.80x10^{-4} \text{ g}/\text{cm} \cdot \text{sec}\right)^{2}}\right] = 0.06$$

$$C_c = 1 + \frac{6.21 \times 10^{-4} \text{T}}{d_p} = 1 + \frac{6.21 \times 10^{-4} (293 \text{K})}{2 \mu \text{m}} = 1.09$$

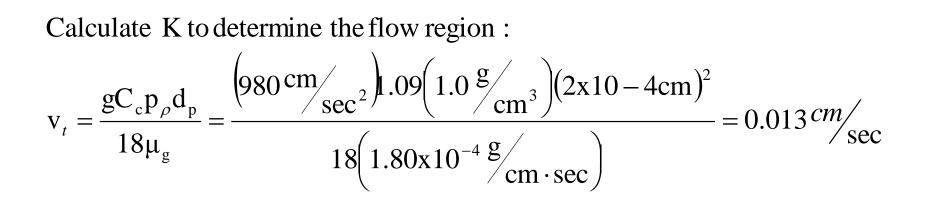




Calculate the terminal settling velocity in 20°C air of a 2  $\mu$ m diameter particle with a density of 1 g/cm<sup>3</sup>.

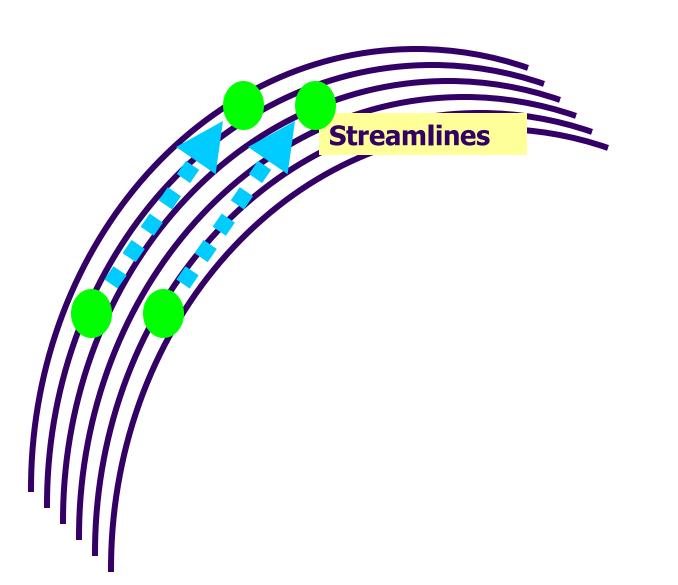


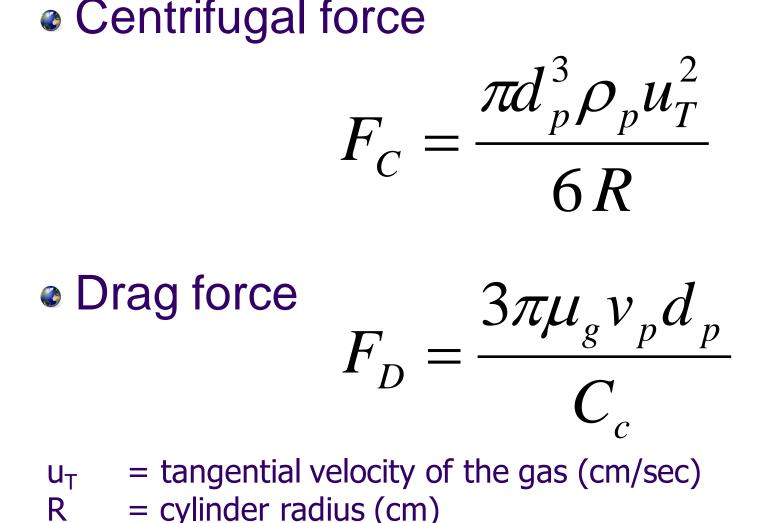
#### Then...



#### **Centrifugal Inertial Force**





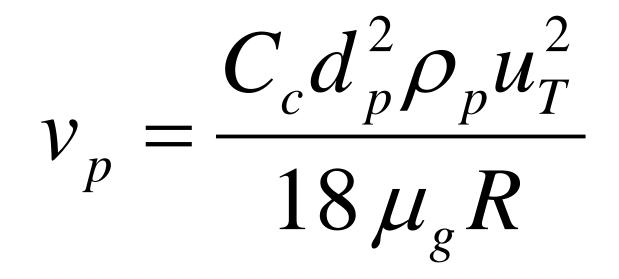


Forces on a Particle



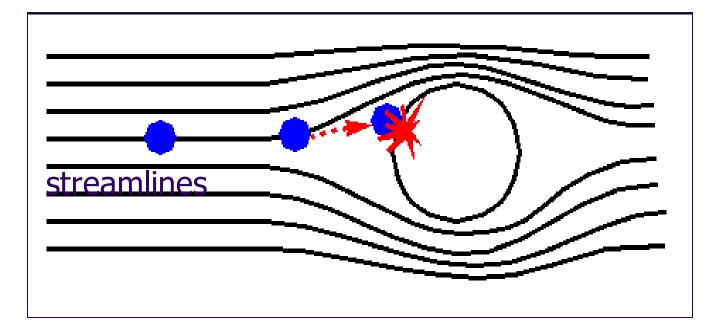
#### **Particle Radial Velocity**





# Particle Drag Force Inertial Force





## **Inertial Impaction Parameter**



 $C_c d_p^2 v_p \rho_p$  $\frac{18\,\mu_g D_c}{100}$ 

#### Where

C<sub>c</sub>

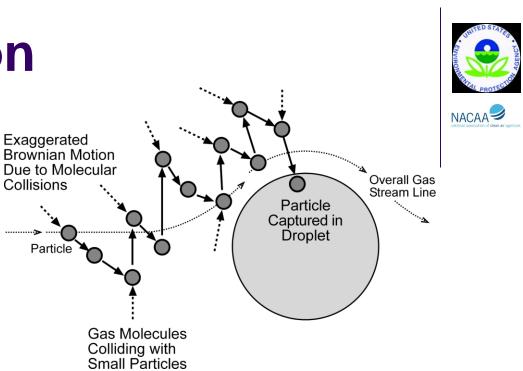
 $d_p$ 

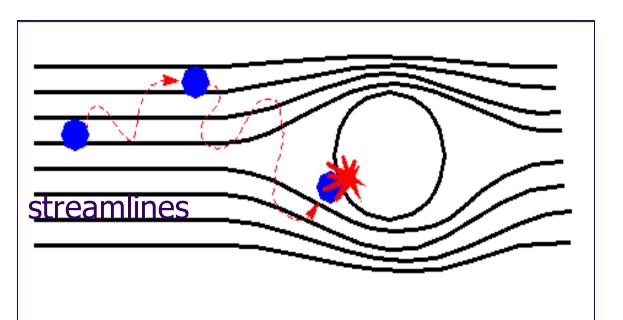
Vp

 $D_{c}$ 

- $\Psi_{I}$  = inertial impaction parameter (dimensionless)
  - = Cunningham slip correction factor (dimensionless)
  - = physical particle diameter (cm)
  - = difference in velocity between the particle and the target (cm/sec)
  - = diameter of collection target (cm)
- $\rho p$  = particle density (g/cm3)
- $\mu g = gas viscosity (g/(cm \cdot sec))$

## **Brownian Motion**





## **Diffusional Collection Parameter**



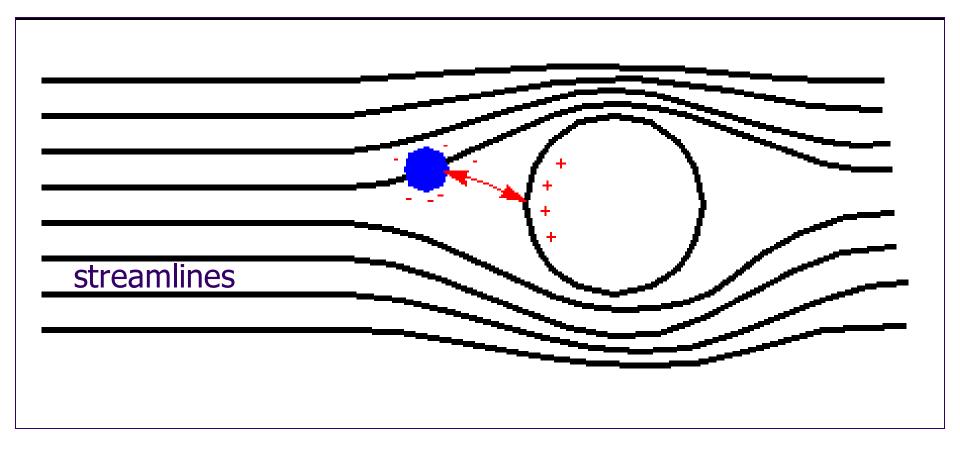
 $\psi_D = \frac{C_c kT}{3\pi\mu_g d_p D_c v_p}$ 

Where

- k = Boltzmann constant (g . cm2/sec2 . K)
- T = absolute temperature (K)
- C<sub>c</sub> = Cunningham slip correction factor (dimensionless)
- $\mu g = gas viscosity (g/cm .sec)$
- d<sub>p</sub> = physical particle diameter (cm)

#### **Electrostatic Attraction**





# **Charging Mechanisms**



• Field charging (large particles, >2µm)

$$n_{\rm f} = \left(\frac{3\epsilon}{\epsilon+2}\right) \left(\frac{Ed_{\rm p}^2}{4e}\right)$$

#### Where

- $n_d$  = number of charges deposited by diffusion charging
- $d_p$  = particle diameter (cm)
- k' = Boltzmann constant (k = 1.4 x 10-16g . cm<sup>2</sup>/sec<sup>2</sup> . K)
- T = absolute temperature (K)
- $c_i$  = ion velocity ( $c_i$  = 2.4 x 10<sup>4</sup> cm/sec)
- e = charge of an electron (e =  $4.8 \times 10^{-10}$  statcoulomb)
- t = time (sec)
- $N_i$  = ion concentration (number/cm<sup>3</sup>)

# **Charging Mechanisms**



Diffusion charging (small particles, <0.4µm)</li>

$$n_{d} = \frac{d_{p}kT}{2e^{2}} \ln \left(1 + \frac{\pi d_{p}c_{i}e^{2}N_{i}t}{2kT}\right)$$

#### Where

- $n_d$  = number of charges deposited by diffusion charging
- $d_p$  = particle diameter (cm)
- k' = Boltzmann constant (k = 1.4 x 10-16g . cm<sup>2</sup>/sec<sup>2</sup> . K)
- T = absolute temperature (K)
- $c_i$  = ion velocity ( $c_i$  = 2.4 x 10<sup>4</sup> cm/sec)
- e = charge of an electron (e =  $4.8 \times 10^{-10}$  statcoulomb)
- t = time (sec)
- $N_i$  = ion concentration (number/cm<sup>3</sup>)

#### **Forces on a Particle**



• Electrostatic force

## $F_E = neE$

• Drag force

$$F_{\rm D} = \frac{3\pi\mu_{\rm g} v_{\rm p} d_{\rm p}}{C_{\rm c}}$$



### **Particle Migration Velocity**

## $v_p = \omega = \frac{neEC_c}{3\pi\mu_g d_p}$

### Example 4-3



Determine the migration velocity of a 2  $\mu$ m unit-density particle carrying 800 units of charge in an electric field of 2kV/cm. Assume that the gas temperature is 20°C:

#### **Solution:**

To solve this problem, the following relationships are used:

 $\begin{array}{l} 300 \text{ volts} = 1 \text{ statvolt} \\ 1 \text{ statvolt} = 1 \text{ statcoulomb/cm} \\ 1 \text{ dyne} = 1 \text{ statcoulomb}^2/\text{cm}^2 = 1 \text{ g.cm/sec}^2 \\ C_{\text{C}} = 1.09 \text{ (as calculated in Example 4-2)} \end{array}$ 



## The electric field in centimeter-gram-second units is:

$$E = 2\frac{kV}{cm} = 2,000\frac{V}{cm}\left(\frac{statvolt}{300 \text{ volts}}\right) = 6.67\frac{statvolts}{cm} = 6.67\frac{statcoulombs}{cm^2}$$
$$\omega = \frac{neEC_c}{3\pi\mu_g d_p} = \frac{(800)(4.8\times10^{-10} \text{ statcoulombs})\left(6.67\frac{statcoulombs}{cm^2}\right)(1.09)}{3\pi\left(1.8\times10^{-4}\frac{g}{cm\cdot\text{sec}}\right)(2\times10^{-4}\text{cm})}$$



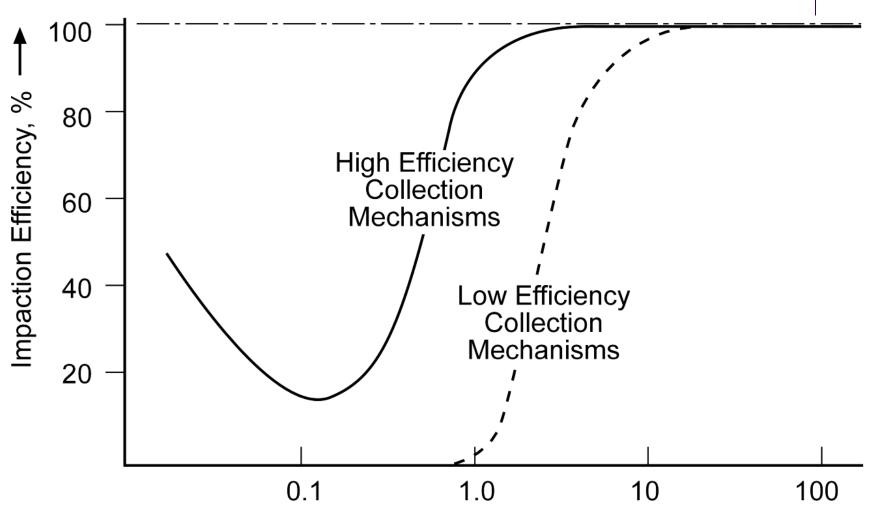


ThermophoresisDiffusiophoresis

## **Size-Efficiency Relationships**



NACAA



Particle Size, Micrometers —



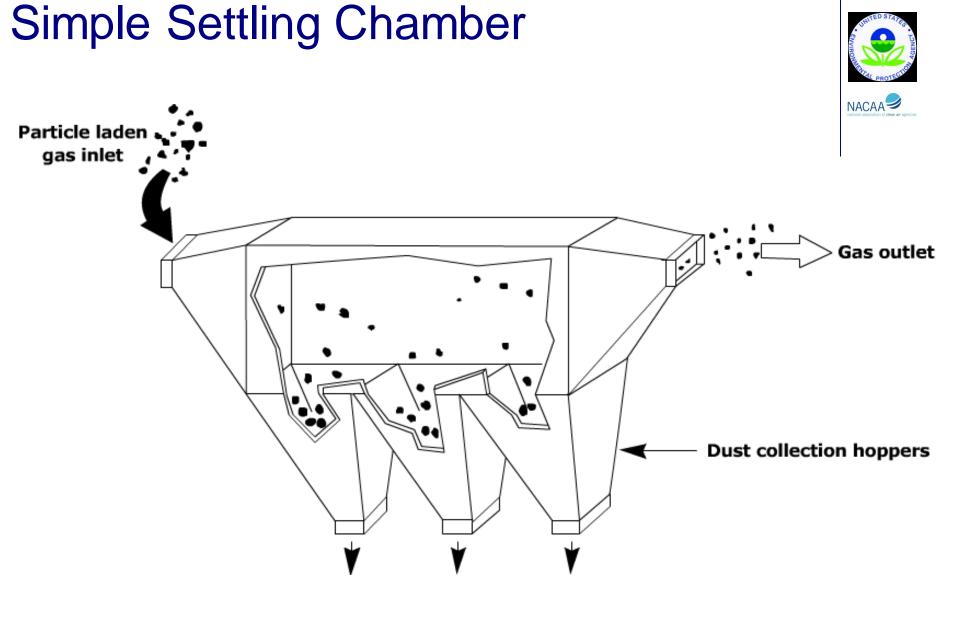




#### **Collection Mechanisms**

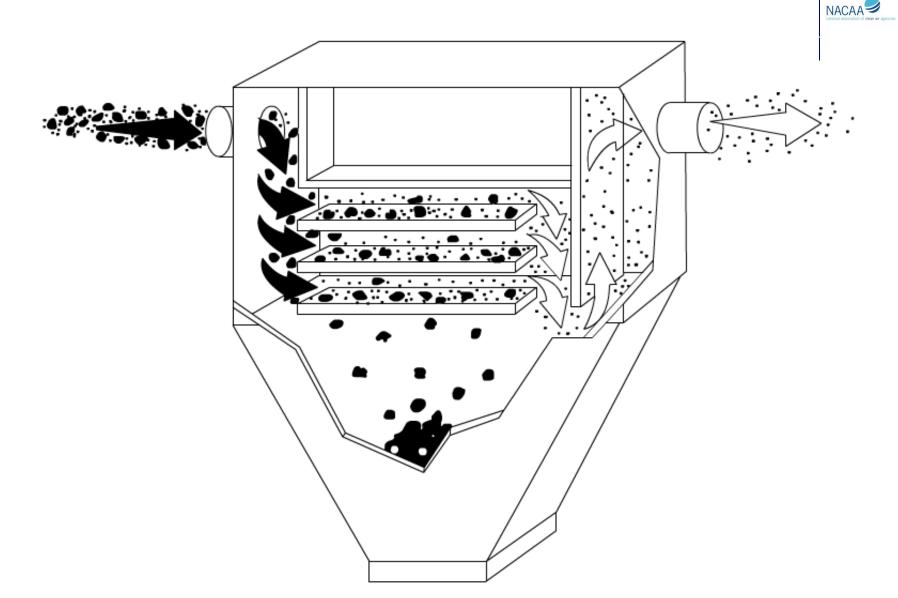


#### Gravitational settling



#### Multi-Tray Settling Chamber Howard

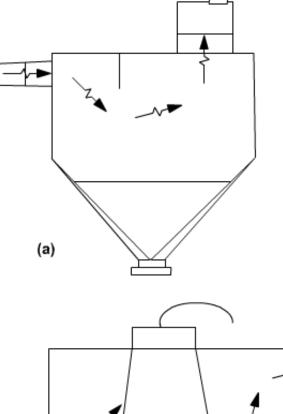


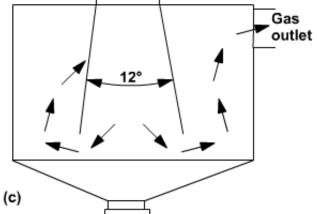


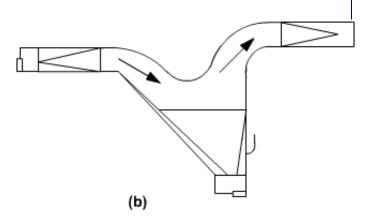
#### **Momentum Separators**

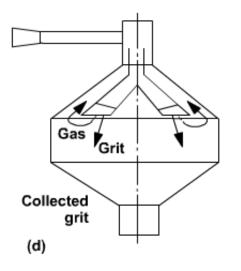


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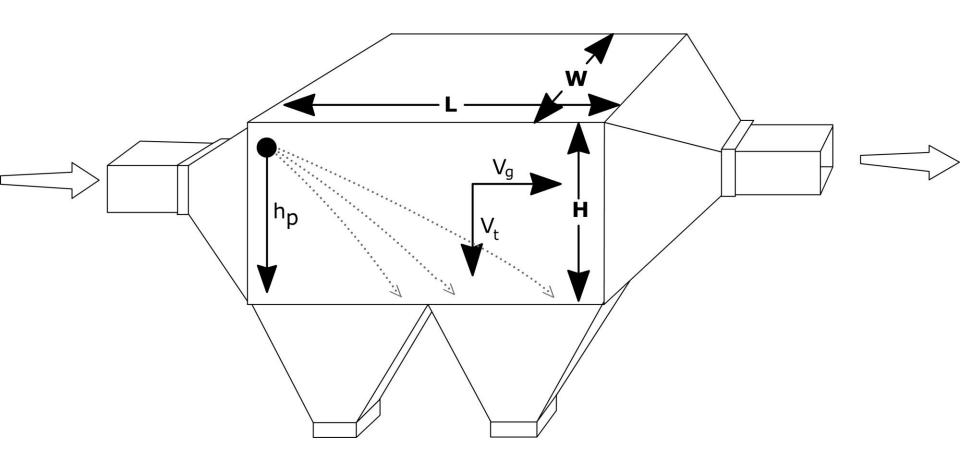






#### **Performance Evaluation**





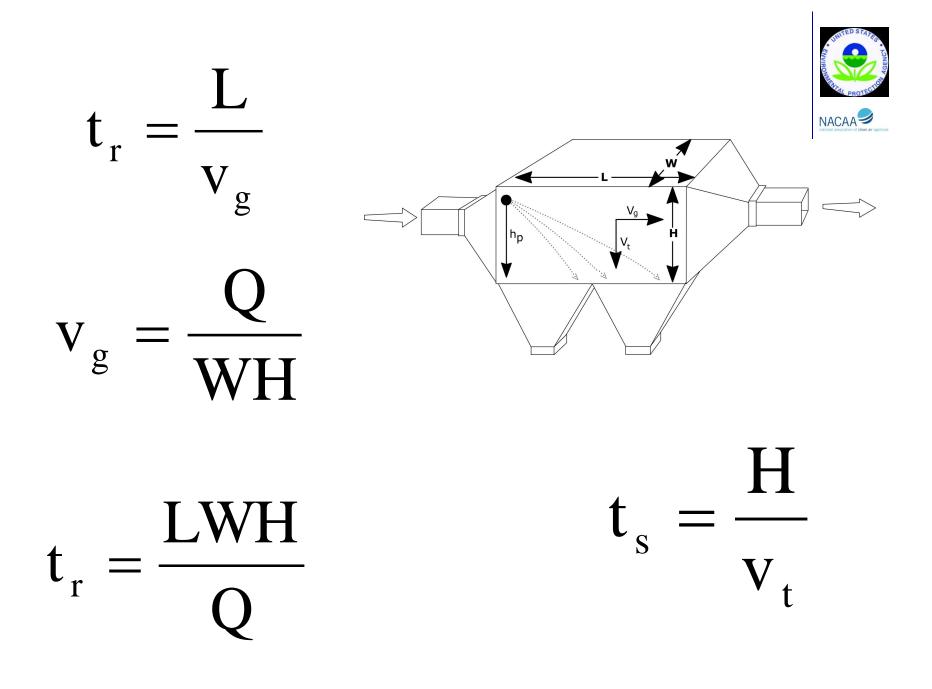
### **Collection Efficiency**

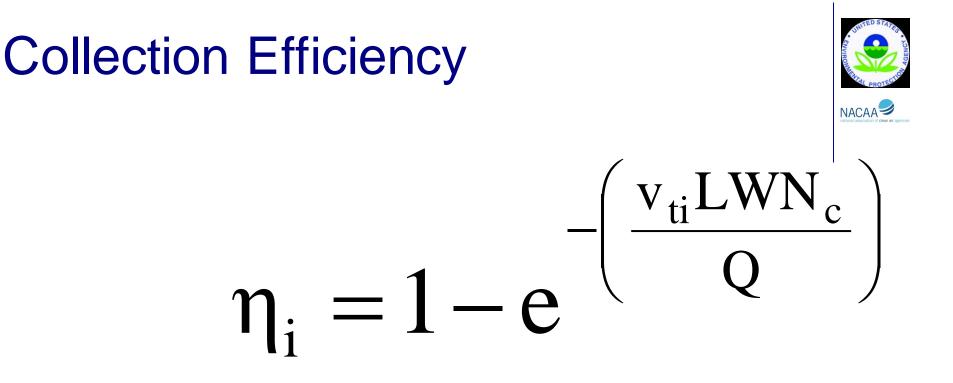


# $\eta_{i} = 1 - e^{-x}$ $x_{i} = \frac{t_{r}}{t_{s}}$

where

 $t_r$  = chamber residence time  $t_{si}$  = particle settling time





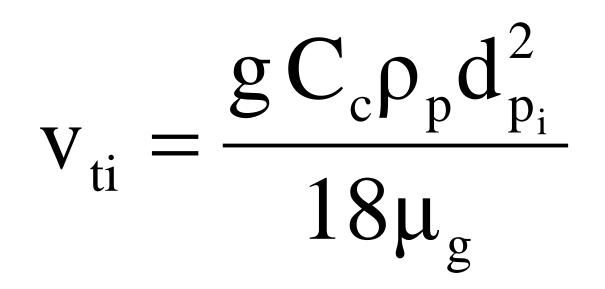
where

- v<sub>t</sub> = particle terminal settling velocity (ft/sec)
- L = chamber length (ft)
- $Q = gas flow rate (ft^3/sec)$
- W = chamber width (ft)

 $N_c$  = number of passages through chamber

#### Terminal Settling Velocity Laminar Regime





## **Collection Efficiency**

Laminar Regime



# $\eta_i = 1 - e^{-\left(\frac{g\rho_p LWN_c}{18\mu_g Q}\right)d_{p_i}^2}$

#### **Chamber Velocity**



#### **Pickup Velocities of Various Materials**

Material	Density (g/cm3)	Median Size (mm)	Pickup Velocity (ft/sec)
Aluminum chips	2.72	335	14.2
Asbestos	2.20	261	17.0
Nonferrous foundry dust	3.02	117	18.8
Lead oxide	8.26	15	25.0
Limestone	2.78	71	21.0
Starch	1.27	64	5.8
Steel shot	6.85	96	15.2
Wood chips	1.18	1,370	13.0
Sawdust		1,400	22.3

#### Example 5-1

Estimate the collection efficiency of a 75  $\mu$ m diameter particle in a simple settling chamber 10 ft wide by 10 ft high by 30 ft long when the gas velocity through the chamber is 5 ft/sec.

Assume a particle density of 120  $lb_m/ft^3$  and gas stream conditions of 68°F and 1 atm.

#### Solution

Convert particle size to feet:

$$d_{p} = 75 \mu m \left[ \frac{ft}{0.3048 \times 10^{6} \mu m} \right] = 2.46 \times 10^{-4} ft$$



#### Example 5-2 continued...



Calculate volumetric flow rate:

$$Q = v_g WH = \left(5 \frac{ft}{sec}\right)(10ft)(10ft) = 500 \frac{ft^3}{sec}$$

Calculate collection efficiency:

$$\eta = 1 - e^{-\left(\frac{g\rho_{p}LWN_{c}}{18\mu_{g}Q}\right)d_{p}^{2}} = 1 - e^{-\left[\frac{\left(32.17\frac{ft}{sec^{2}}\right)\left(120\frac{lb_{m}}{ft^{3}}\right)(30ft)(10ft)(1)}{18\left(1.21\times10^{-5}\frac{lb_{m}}{ft^{4}sec}\right)\left(500\frac{ft^{3}}{sec}\right)}\right]}(2.46\times10^{-4}ft)^{2} = 1 - e^{-\left(\frac{g\rho_{p}LWN_{c}}{18\mu_{g}Q}\right)d_{p}^{2}} = 1 - e^{-\left(\frac{g\rho_{p}LWN_{c}}{18\mu_{g}Q}\right)d_{p$$

=0.475 = 47.5%

#### Advantages and Disadvantages

#### Advantages:

Low Capital Cost Very Low Energy Cost No Moving Parts Few Maintenance Requirements Low Operating Costs Excellent Reliability Low Pressure Drop Device Not Subject to Abrasion Provides Incidental Cooling of Gas Stream Dry Collection and Disposal

#### Disadvantages:

Relatively Low PM Collection Efficiencies Unable to Handle Sticky or Tacky Materials Large Physical Size Trays in Multiple-Tray Settling Chamber may Warp



#### **Review Questions**

Estimate the collection efficiency of a 50  $\mu$ m diameter particle in a simple settling chamber 5 meters wide by 2 meters high by 10 meters long when the gas velocity is 0.3 m/sec.

Assume a particle density of 4.6 g/cm<sup>3</sup> and gas stream conditions of 20°C and 1 atm.



#### **Review Solutions**

Calculate the volumetric flow rate:



$$Q = v_g WH = \left[0.3 \frac{m}{sec}\right](5m)(2m) = 3.0 \frac{m^3}{sec} = 3.0 \times 10^6 \frac{cm^3}{sec}$$

#### Calculate collection efficiency:

$$\eta = 1 - e^{-\left(\frac{g\rho_{p}LWN_{c}}{18\mu_{g}Q}\right)d_{p}^{2}}$$

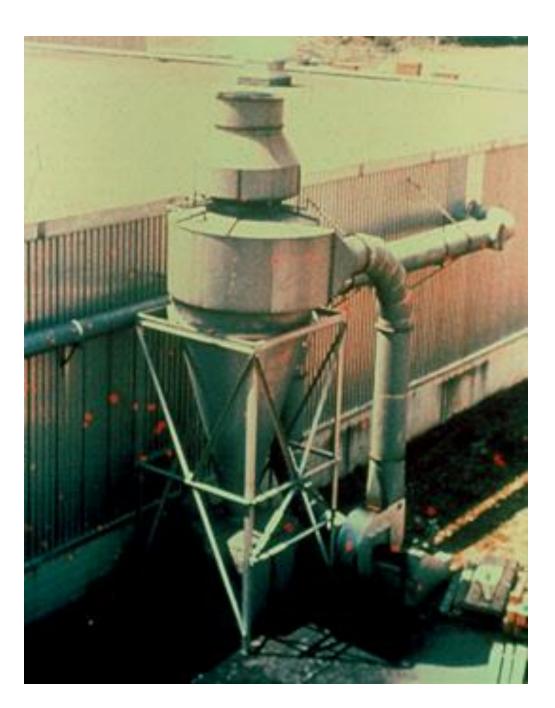
$$=1-e^{\left[\frac{\left(980\frac{\text{cm}}{\text{sec}^{2}}\right)\left(120\frac{\text{g}}{\text{cm}^{3}}\right)(1000\text{cm})(500\text{cm})(1)}{18\left(1.80\times10^{-4}\frac{\text{g}}{\text{cm}^{4}\text{sec}}\right)\left(3.0\times10^{6}\frac{\text{cm}^{3}}{\text{sec}}\right)}\right](50\times10^{-4}\text{cm})^{2}}=0.997=99.7\%$$

#### **Chapter 6**

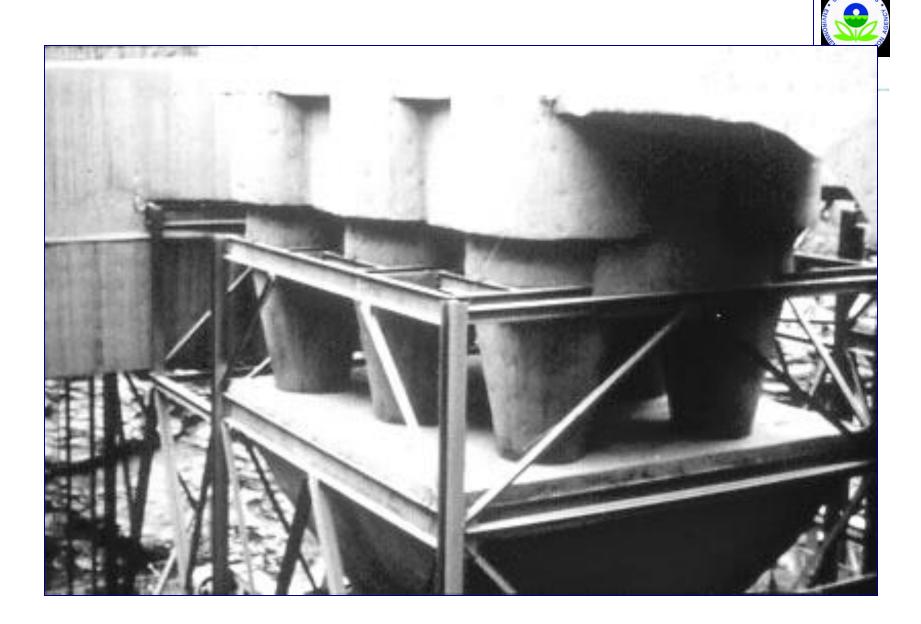


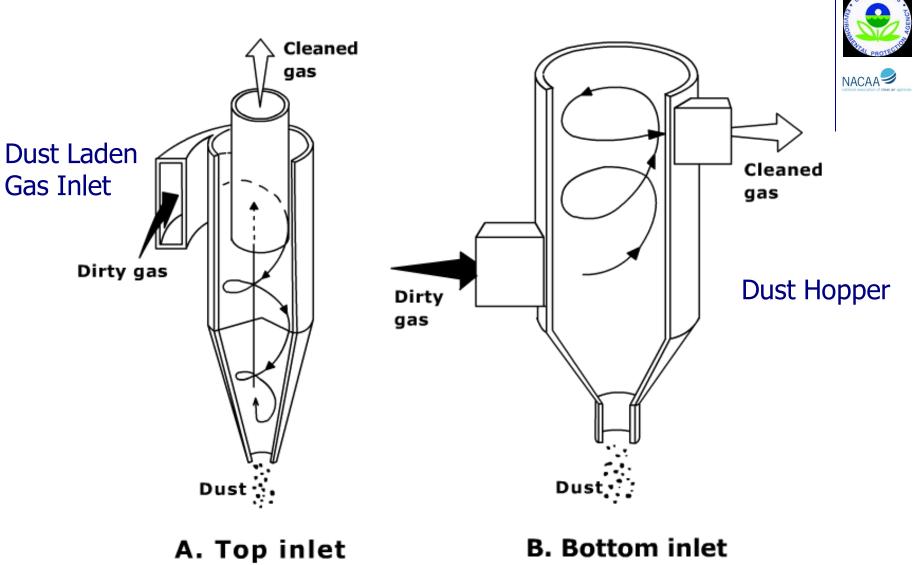
on of clean air











#### **Factors Affecting Performance**



Particle diameter: H = f(d<sup>2</sup>)
Gas flow rate: H = f(Q<sup>2</sup>)
Cyclone diameter
Residence time

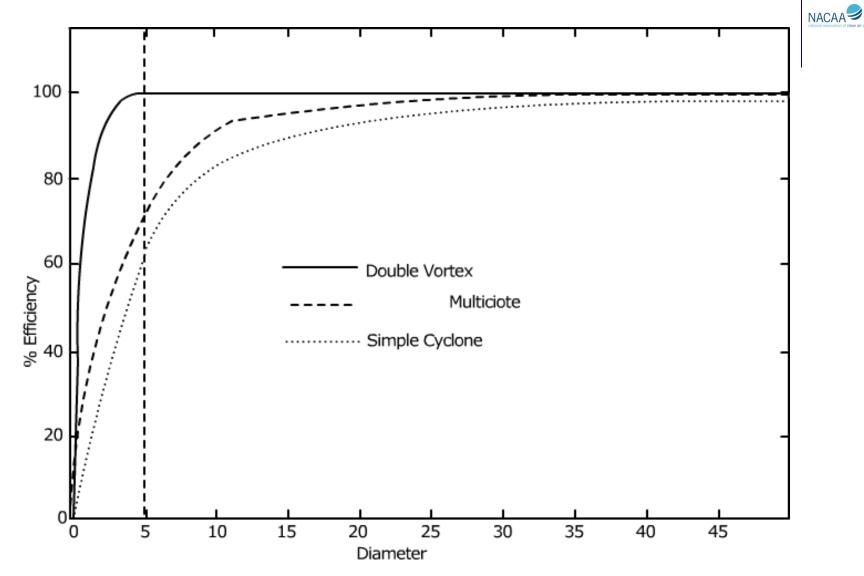




## -----625D .51 SIMPLE CYCLONE

#### Size Efficiency Curves



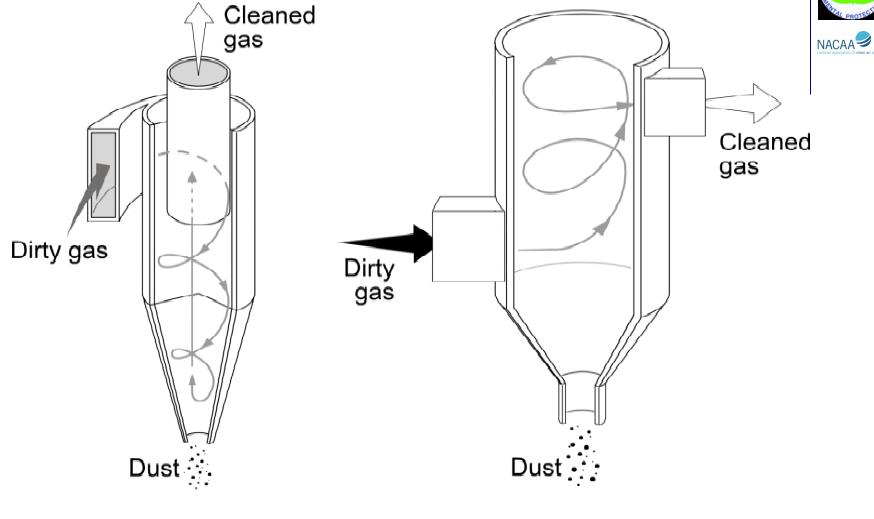






## Large diameter cyclones Small diameter multi-cyclones

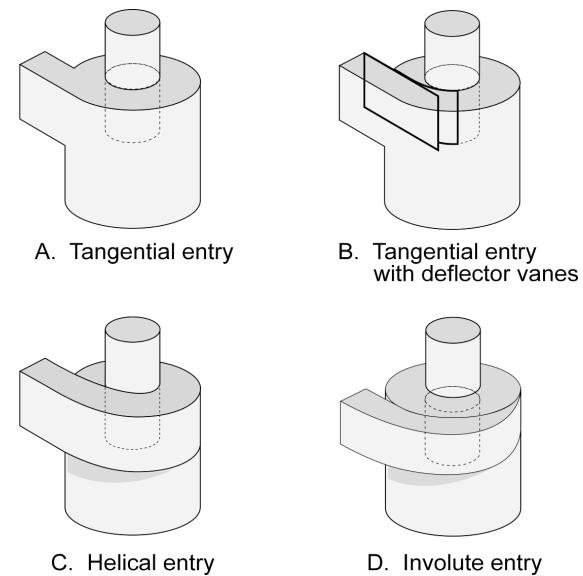


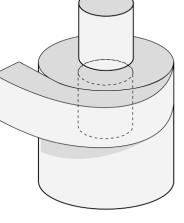


A. Top inlet

**B. Bottom inlet** 

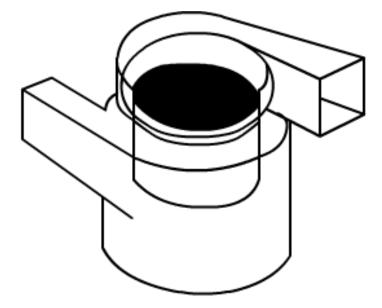




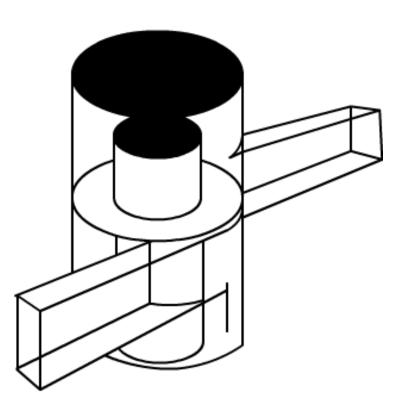


D. Involute entry

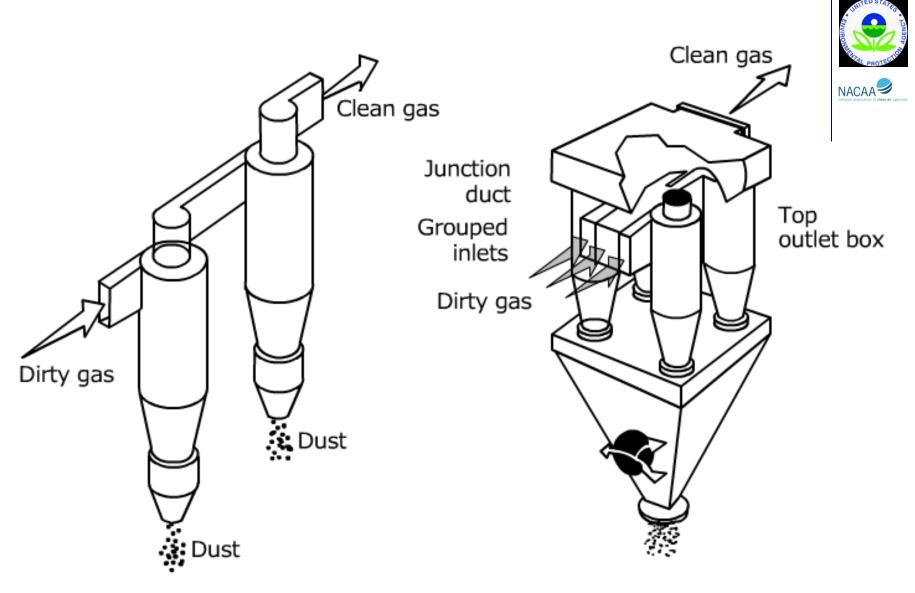




A. Involute scroll outlet

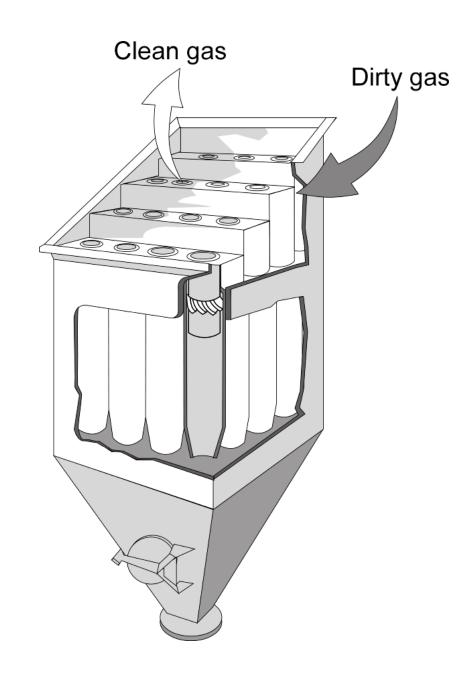


B. Outlet drum

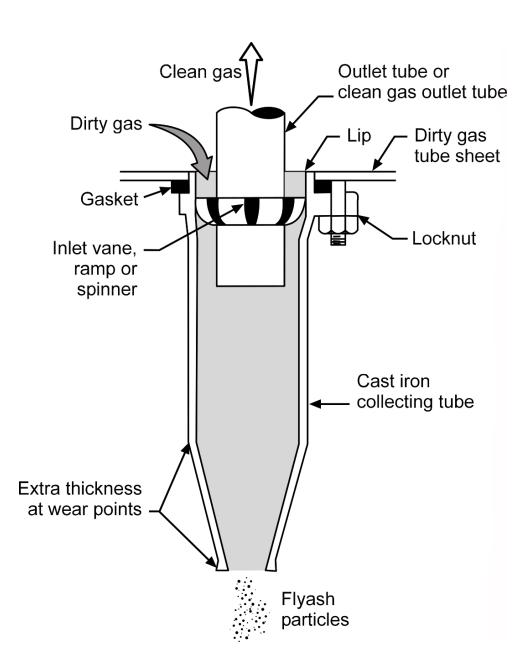


A. two cyclones in series

B. Four cyclones in parallel

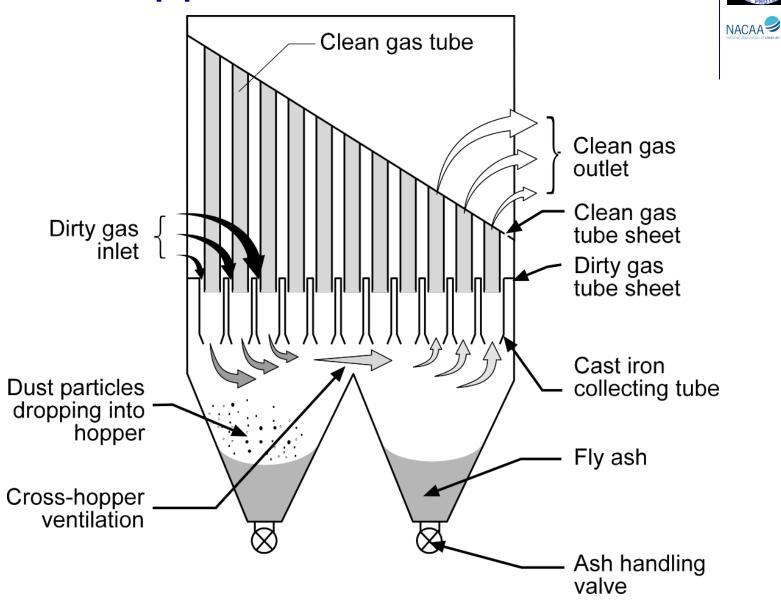








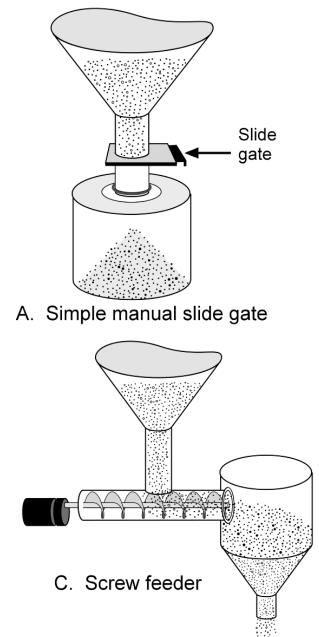
# **Cross Hopper Recirculation**

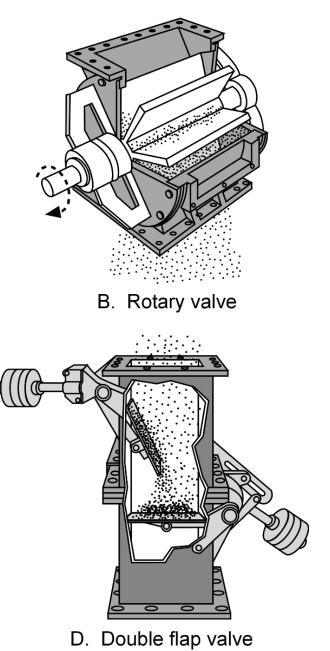




Properly sealing solids discharge valve
Adequately sized hopper throat
Adequately sloped hopper walls
Strike plates or vibrators
Thermal insulation

#### Solids Removal Valves









# **Collection Efficiency**

Lapple Technique

$$\left[d_{p}\right]_{cut} = \sqrt{\frac{9\mu_{g}B}{2\pi n_{t}v_{i}\rho_{p}}}$$

where

 $\rho_p$ 

 $\rho_{g}$ 

B<sub>c</sub>

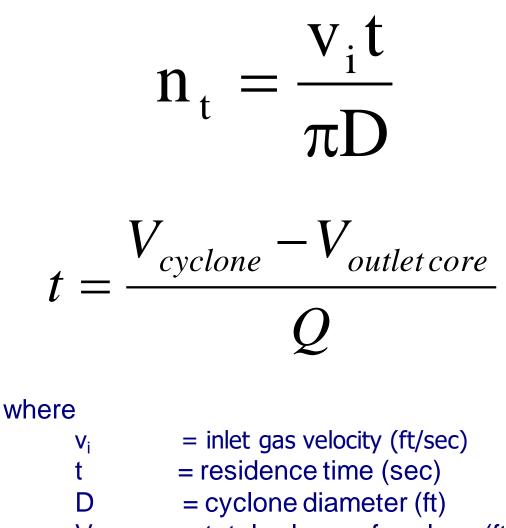
n<sub>t</sub>

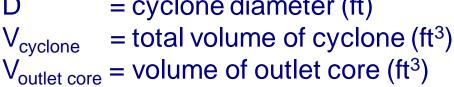
 $[d_p]_{cut} = cut \, diameter \, (ft) \, (the particle size collected with 50% efficiency)$  $\mu_g = gas \, viscosity \, (lb_m/ft \cdot sec)$  $v_i = inlet gas \, velocity \, (ft/sec)$ 

= particle density (
$$lb_m/ft^3$$
)

- = cyclone inlet width (ft)
- = number of turns





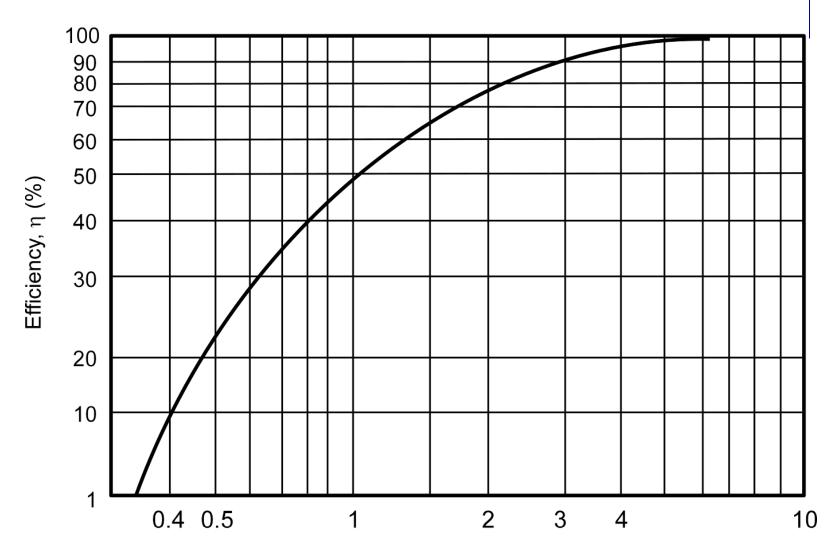


Q

= volumetric flow rate (ft<sup>3</sup>/sec)

# Lapple Efficiency Curve





Particle size ratio, [dp]/[dp]cut

#### Example 6-1

A large diameter cyclone is being used for the removal of grain dust in the range of 8 to 100  $\mu m$  diameter.

What are collection efficiencies over this range if the cyclone has an inlet width of 1 ft, an inlet gas velocity of 50 ft/sec, and an operating temperature of 68°F?

Assume  $n_t = 1$  and a particle density of 80 lb<sub>m</sub>/ft<sup>3</sup>.

$$\left[d_{p}\right]_{cut} = \sqrt{\frac{9\mu_{g}B_{c}}{2\pi\pi(1)}} = \sqrt{\frac{9\left(1.21\times10^{-5}\,lb_{m}/ft\cdot sec\right)(1\,ft)}{2\pi\pi(1(50\,ft/sec)(80^{10}/ft^{3}))}} = 6.58\times10^{-5}\,ft = 20\mu0$$



#### Example 6-1 continued...



Estimate efficiency of 8, 12, 20, 30, 50 and 100  $\,\mu\text{m}$  diameter particles:

Example 6-1 Efficiency Estimates					
[d <sub>p</sub> ] <sub>i</sub> (mm)	[d <sub>p</sub> ] <sub>i</sub> /[d <sub>p</sub> ] <sub>cut</sub>	hi (%)			
8	0.40	9			
12	0.60	28			
20	1.00	50			
30	1.50	65			
50	2.50	85			
100	5.00	98			

# **Collection Efficiency**

Leith Technique



 $\eta_i = 1 - e^{-2(C\Psi)^{\frac{1}{2n+2}}}$ 

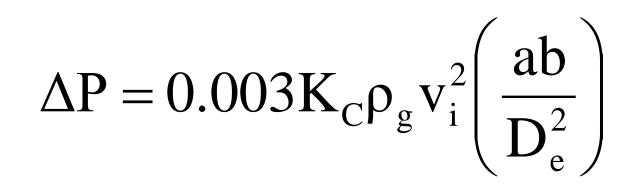
#### where

 $\eta_i$  = efficiency for particle diameter i (dimensionless) C = cyclone dimension factor (dimensionless)  $\Psi$  = cyclone inertial impaction parameter (dimensionless) n = vortex exponent (dimensionless)

The steps to achieve the answer to the above equation are covered in your text, pages 12 - 15 of Chapter 6.

#### **Pressure Drop**





where

 $\Delta P$  = static pressure drop (in WC)

 $K_C = 16$ , for tangential inlet; 7.5, for inlet vane (dimensionless)

 $\rho_g$  = gas density (lbm/ft<sup>3</sup>)

- $v_i = inlet velocity (ft/sec)$
- a = cyclone inlet height (ft)
- b = cyclone inlet width (ft)

 $D_e$  = outlet pipe diameter (ft)

#### **Pressure Drop**



# $\Delta P = K_P \rho_g v_g^2$

# where $$\begin{split} & \Delta P = \text{static pressure drop (in WC)} \\ & K_P = 0.013 \text{ to } 0.024 \\ \text{(dimensionless)} \\ & \rho_g = \text{gas density (lb}_m/\text{ft}^3) \\ & v_g = \text{inlet velocity (ft/sec)} \end{split}$$

#### Example 6-2

A single high efficiency cyclone has an inlet width of 2 ft, an inlet height of 5 ft and an outlet pipe diameter of 5 ft.



Using Equation 6-13:

$$\Delta P = 0.003 K_c \rho_g V_g^2 \left[ \frac{ab}{D_e^2} \right]$$
$$= 0.003(16) \left[ 0.075 \frac{lb_m}{ft^3} \right] \left[ 50 \frac{ft}{sec} \right]^2 \left[ \frac{(5ft)(2ft)}{(5ft)^2} \right] = 3.6in$$



WC





Using Equation 6-14:

$$\Delta P = K_p \rho_g V_g^2 = 0.024 \left[ 0.075 \frac{lb_m}{ft^3} \right] \left[ 50 \frac{ft}{sec} \right] = 4.5 \text{ in WC}$$



Static pressure drop gauges
 Inlet and outlet temperature gauges

#### Advantages and Disadvantages



#### Advantages

Low Capital Cost No Moving Parts Few Maintenance Problems Low Operating Cost **Relatively Low Pressure Drop** Dry Collection and Disposal **Relatively Small Space Requirement** Disadvantages **Relatively Low PM Collection Efficiencies Unable to Handle Sticky Materials High Efficiency Units Experience Higher Pressure Drop** 

1. What is the normal range of inlet gas stream velocity for large diameter cyclones? (page 3)

5 to 10 feet per second 20 to 50 feet per second 5 to 10 feet per minute 20 to 50 feet per minute



2. What is the purpose of using a solids discharge valve on the hoppers of cyclone collectors? Select all that apply. (page 6) Minimize air infiltration into the cyclone Minimize the risk of fires Maintain solids flow out of the hopper

3. What design feature initiates the spinning gas flow in a large diameter cyclone? (page 4)
 Turning vanes
 Gravity

Tangential gas inlet None of the above





4. Which type of cyclone collector has higher radial velocities? (page 2)
 Large diameter cyclones
 Multi-cyclones

5. What is the purpose of the clean side tube sheet in a multi-cyclone collector? (page 6)
Support the cyclone tubes
Separate the inlet gas stream from the outlet gas stream
Separate the outlet gas stream from the hopper
None of the above

6. What is the typical number of complete turns (360 degrees) achieved in a large diameter cyclene operating with a normal inlet gas velocity? (page

3) One-half to three Two to five Five to ten Greater than ten







7. What is the typical range in the diameters of multi-cyclone tubes? (page 6)

1 to 6 inches 6 to 12 inches 12 to 18 inches 18 to 24 inches



8. Must multi-cyclone tubes be oriented vertically (inlet at top, cyclone discharge at bottom) in order to operate properly? (page 6)



9. Why is it important to fabricate the outlet extension tubes of multicyclone collectors from abrasion resistant material? (page 3) Minimize abrasion caused by the inlet gas stream Minimize abrasion caused by the outlet gas stream Minimize fracturing the inlet particulate matter All of the above

10. The performance of a cyclone collector is related to the \_\_\_\_ of the particle diameter.

First power Second power Third power



Performance is independent of particle size

11. The performance of a cyclone collector is related to the \_\_\_\_\_ of the gas\_velocity.

First power Second power Third power



Performance is independent of radial gas velocity

12. Static pressure drop across a cyclone collector is related to the \_\_\_\_\_ of the gas flow rate.

First power Second power Third power



Static pressure drop is independent of gas flow rate



13. Typical static pressure drops in a multi-cyclone collector are:

1 to 3 in WC 2 to 6 in WC 1 to 3 psig 2 to 6 psig



14. Multi-cyclone collectors are capable of effectively removing particles down to approximately \_\_\_\_\_ micrometers.

0.5 micrometers3 micrometers10 micrometers20 micrometers50 micrometers





#### **Review Problem #1**

- 1. What is the overall collection efficiency for a single cyclone collecting dust with the distribution given below?
- The collector has a diameter of 1 ft, an inlet gas velocity of 50 ft/sec, and an operating temperature of 200°F?
- The particle density is 70 lb<sub>m</sub>/ft<sup>3</sup>. Assume the gas stream spins two complete rotations within the cyclone. (page 10)

Size (µm)	10	20	30	40	50	60	70	80	100	
% of Mass	1	3	9	13	24	29	15	4	2	100%



#### **Review solution**



#### **Solution**

#### Estimate the gas viscosity at 200°F:

$$\mu = \mu_{ref} \left(\frac{T}{T_{ref}}\right)^{0.768} = 1.21 \times 10^{-5} \frac{lb_m}{ft \cdot \sec} \left(\frac{660^{\circ}R}{528^{\circ}R}\right)^{0.768} = 1.44 \times 10^{-5} \frac{lb_m}{ft \cdot \sec}$$

#### Calculate the cut diameter:

$$\left[d_{p}\right]_{cut} = \sqrt{\frac{9\mu_{g}B}{2\pi n_{t}v_{i}\rho_{p}}} = \sqrt{\frac{9\left(1.44x10^{-5}\frac{lb_{m}}{ft\cdot\sec}\right)1ft}{2\pi(2\left(50\frac{ft}{\sec}\right)\left(70\frac{lb_{m}}{ft^{3}}\right)}} = 5.43x10^{-5}ft = 16.5\,\mu m$$

#### And then...



#### Calculate the fractional efficiencies:

Problem 6-1 Efficiency Estimates						
[d <sub>p</sub> ] <sub>i</sub> (µm)	[d <sub>p</sub> ] <sub>i</sub> /[d <sub>p</sub> ] <sub>cut</sub>	η <sub>i</sub> (%)				
10	0.6	28				
20	1.2	55				
30	1.8	74				
40	2.4	83				
50	3.0	90				
60	3.6	94				
70	4.2	97				
80	4.8	98				
100	6.1	100				

#### And finally...

#### Calculate the overall efficiency:



Size (gm)	% of Mass	<b>η</b> <sub>i</sub> (%)	Mass collected (%)
10	1	28	0.28
20	3	55	1.65
30	9	74	6.66
40	13	83	10.79
50	24	90	21.60
60	29	94	27.26
70	15	97	14.55
80	4	98	3.92
100	2	100	2.00
	100%		88.71%

#### Review problem #2

2. A single cyclone collector has the following fractional efficiency curve. Estimate the overall collection efficiency of a dust with a  $d_{50}$  of 50  $\mu$ m and a  $\sigma_g$  of 1.67. (page 10)



Solution...

#### Plot cumulative distribution plot...

Divide into particle size ranges and determine the percent mass in each size range:

Size (gm)	% of Mass Less Than Size	Size Range (mm)	% of Mass
10	0.1	0 to 10	0.1
15	1.0	10 to 15	0.9
26	10.0	15 to 26	9.0
40	32.0	26 to 40	22.0
67	70.0	40 to 67	38.0
100	90.0	67 to 100	20.0
		>100	10.0



And then...

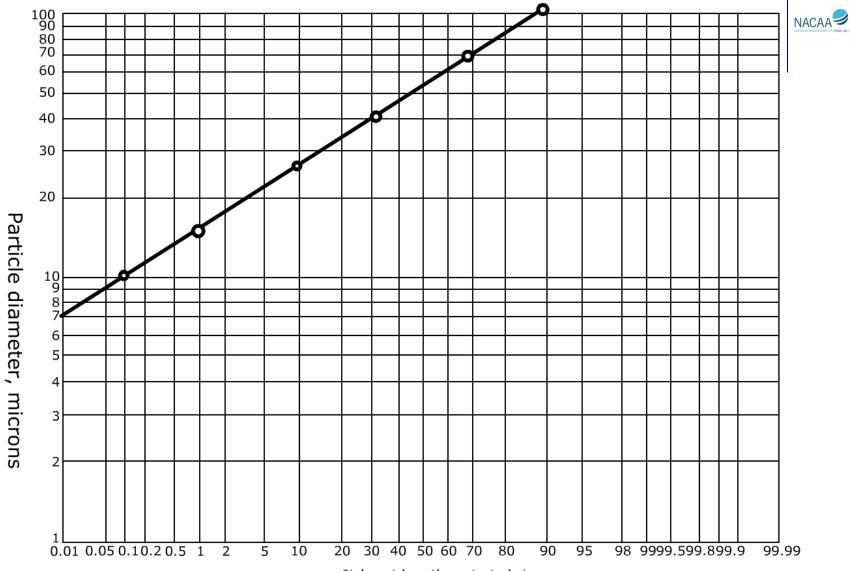


#### Calculate the overall efficiency:

Size Range (gm)	Avg Size (gm)	% of Mass	hi (%)	Mass Collected (%)
0 to 10	5.0	0.1	28	0.03
10 to 15	12.5	0.9	52	0.47
15 to 26	20.5	9.0	68	6.12
26 to 40	33.0	22.0	82	18.04
40 to 67	53.5	38.0	93	35.34
67 to 100	83.5	20.0	99	19.80
>100	100.0	10.0	99	9.90
		100%		89.70%

#### And plot...





% by wt less then started size

#### **Chapter 7**







# **Particle Collection Steps**



#### Capture particulate matter using a filtration media

- Remove collected material from the filter surface
- Dispose of accumulated solids

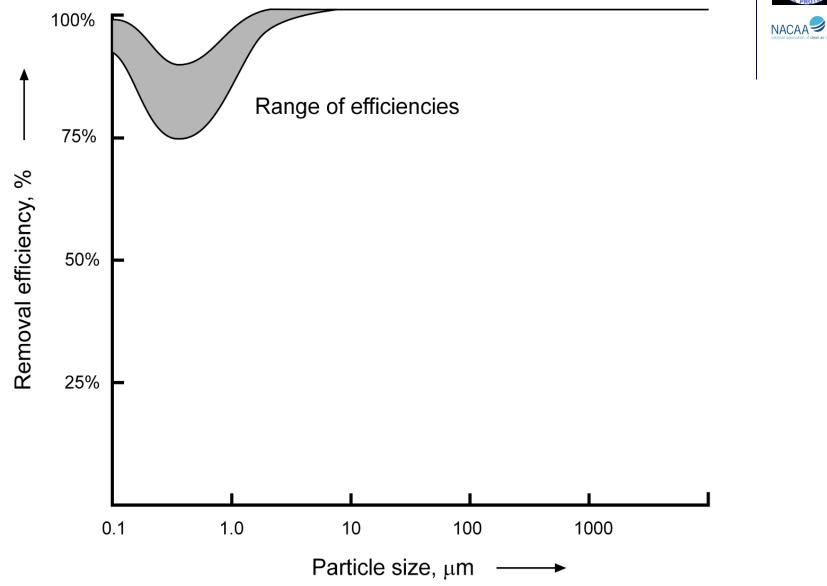
### **Capture Mechanisms**





- Inertial impaction
- Brownian motion
- Electrostatic attraction
- Gravitational settling
- Sieving





# **Factors Affecting Efficiency**



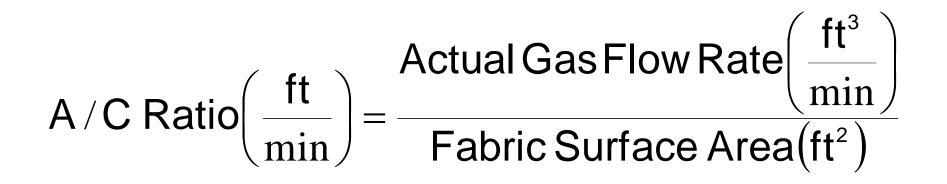


# Air-to-cloth ratio Holes, tears and gaps Blinding and bag blockage



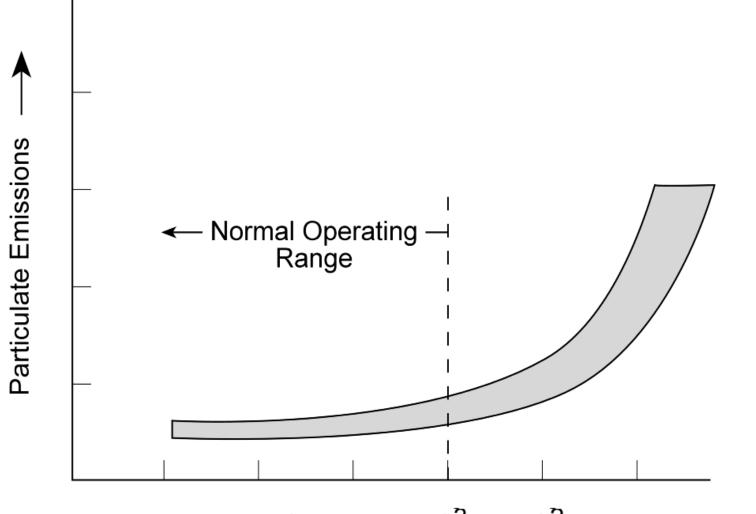


#### **Air-to-Cloth Ratio**





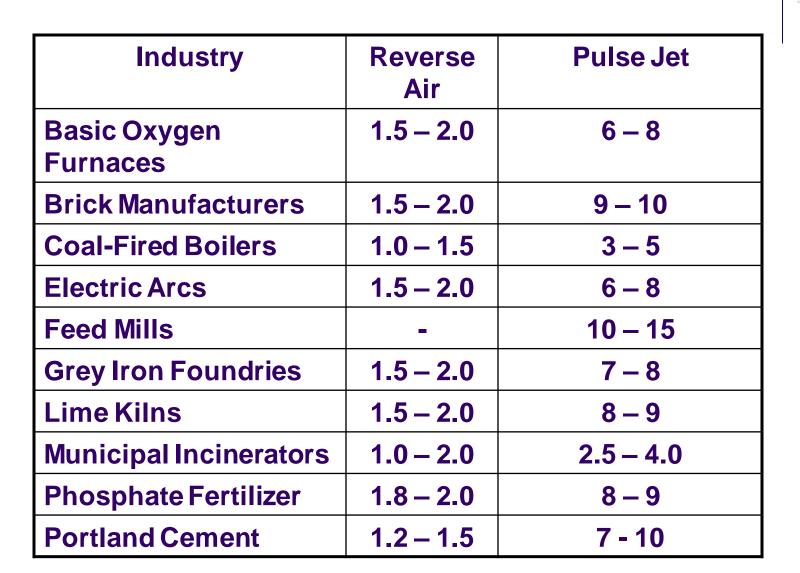
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Air-to-Cloth Ratio,  $(ft^3/min)/ft^2 \longrightarrow$ 

#### Air-to-Cloth Ratios in Various Industrial Categories





## Example 7-1

Calculate the gross and net air-to-cloth ratios for a reverse air baghouse with 20 compartments, 360 bags per compartment, a bag length of 30 ft, and a bag diameter of 11 inches.

Use an actual gas flow rate of  $1.2 \times 106$  ft<sup>3</sup>/min.

Assume that two compartments are out of service when calculating the net air-to-cloth ratio



#### **Solution**



NACAA

Bag area =  $\pi$ DL Area/bag =  $\pi$  (11 inches)( ft/12 in.) 30 ft = 86.35 ft<sup>2</sup>/bag

The gross air-to-cloth ratio is calculated assuming that all the bags are in service.

Total number of bags = (360 bags/compartment)(20 compartments) = 7,200 bags

Total fabric area =  $(7,200 \text{ bags})(86.35 \text{ ft}^2/\text{bag}) = 621,720 \text{ ft}^2$ 

### **Solution (continued)**



$$(A/C)_{gross} = \frac{1.2 \times 10^6 \text{ ft}^3 / \text{min}}{621,720 \text{ ft}^2} = 1.93 (\text{ft}^3 / \text{min}) / \text{ft}^2$$

The net air-to-cloth ratio is calculated by subtracting the compartments that are not in filtering service.

Total number of bags = (360 bags/compartment)(18 compartments) = 6,480 bags

Total fabric area =  $(6,480 \text{ bags})(86.35 \text{ ft}^2/\text{bag}) = 559,548 \text{ ft}^2$ 

$$(A/C)_{net} = \frac{1.2 \times 10^6 \text{ ft}^3 / \text{min}}{559,548 \text{ ft}^2} = 2.14 (\text{ft}^3 / \text{min}) / \text{ft}^2$$

### **Factors Affecting Efficiency**





# Air-to-cloth ratio Holes, tears and gaps Blinding and bag blockage

# **Factors Affecting Efficiency**





- Air-to-cloth ratio
- Holes, tears and gaps
- Blinding and bag blockage
  - Water
  - Lubricating oil
  - Condensed organic
  - Submicrometer particles

## **Applicability Limitations**



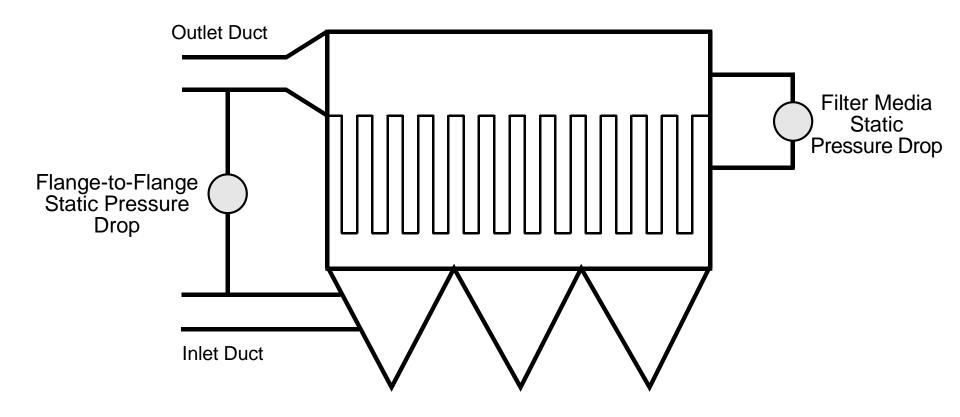
NACAA

Blinding
Large particle abrasion
Fire or explosion
Gas temperature



NACAA

#### **Static Pressure Drop**



#### **Pressure Drop Modeling**



NACAA



#### where $\Delta P_t = \text{total pressure drop}$ $\Delta P_f = \text{fabric pressure drop}$ $\Delta P_c = \text{dust cake pressure drop}$

#### **Fabric Pressure Drop**





 $\Delta P_f = K_1 V_f$ 

# where $K_1 = fabric resistance factor v_f = filtration velocity$



#### **Dust Cake Pressure Drop**

 $\Delta P_c = K_2 C_i V_f^2 t$ 

where

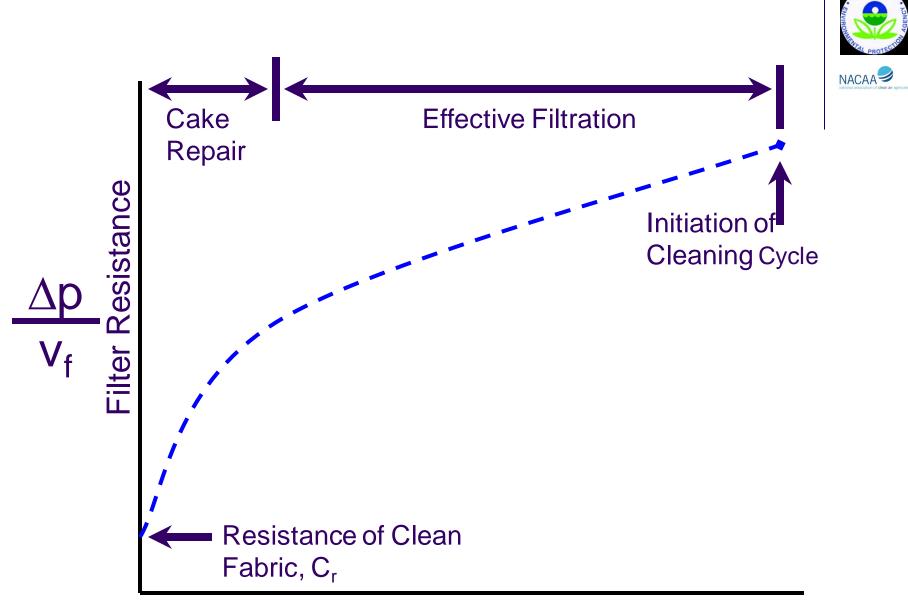
- $K_2$  = dust cake resistance factor
- c<sub>i</sub> = inlet dust concentration
- $v_f$  = filtration velocity
- t = time





 $\Delta P_{t} = K_1 v_f + K_2 c_i v_f^2 t$  $S = \Delta P_{\rm f}/v_{\rm f} = K_1 + K_2 c_{\rm i} v_{\rm f} t$ 

where S = filter drag



#### Mass of Dust Deposit (proportional to time)

#### **Cleaning Method**





Shaker
Reverse air
Pulse jet

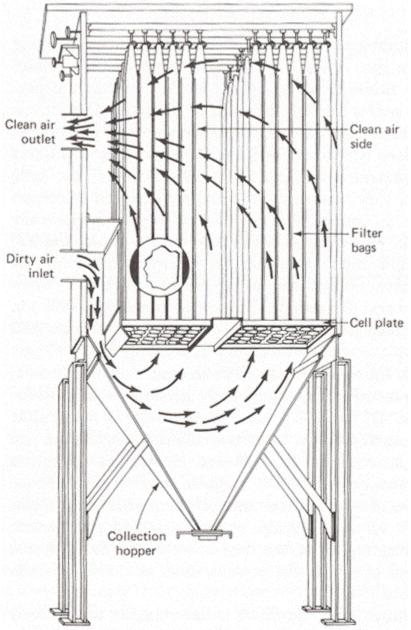
#### **Operating Mode**



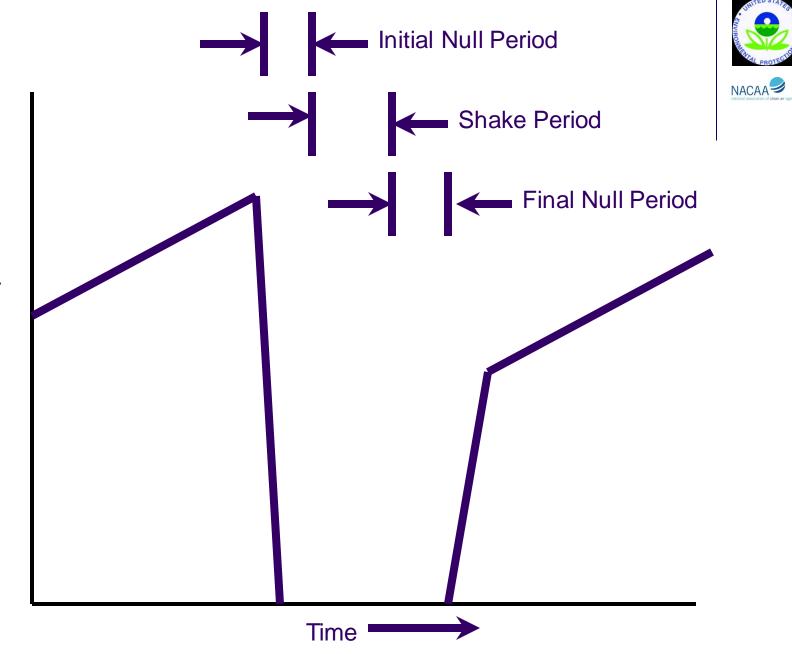


Intermittent
Periodic
Continuous

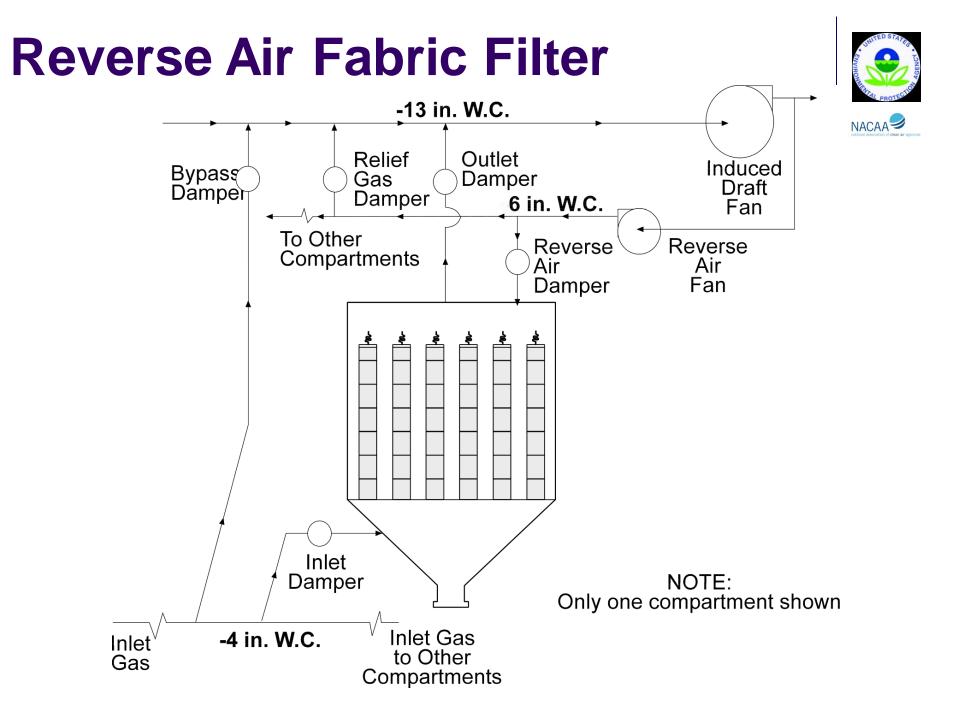
#### **Shaker Fabric Filter**







Pressure Drop

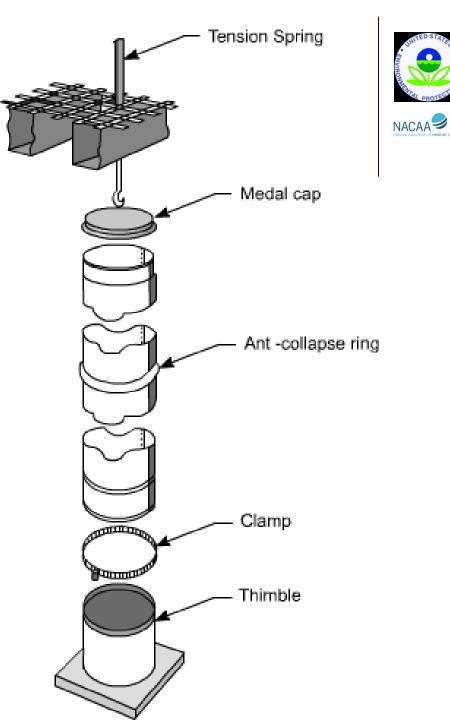


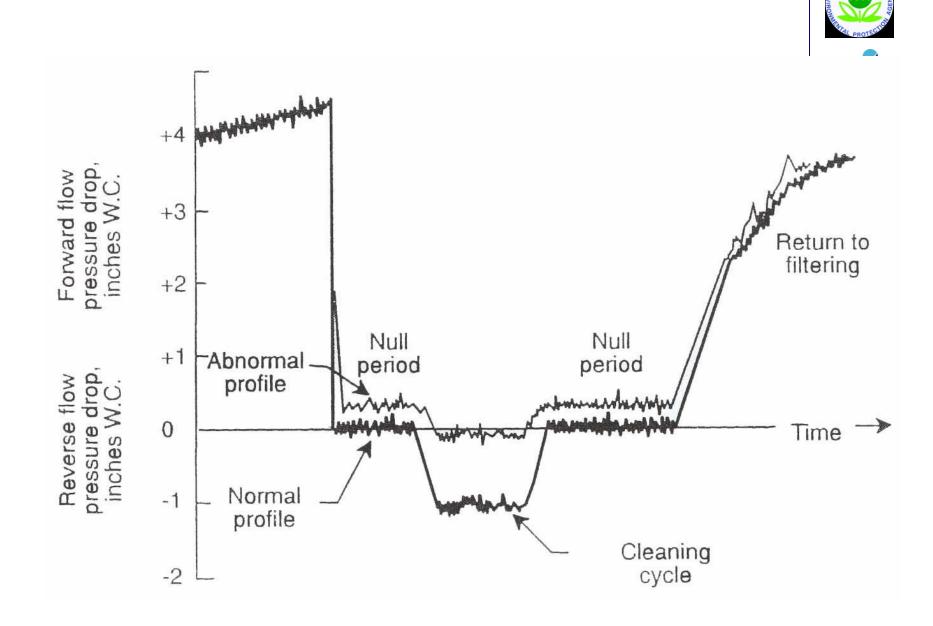






#### **Bag Attachment**



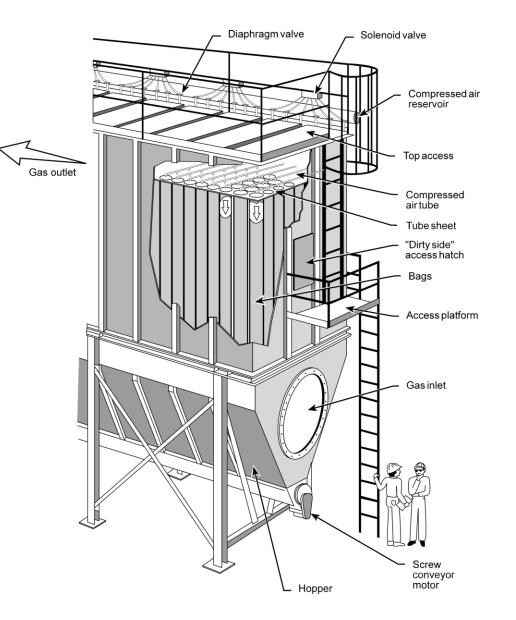


#### **Pulse Jet Fabric Filter**





#### **Pulse Jet Fabric Filter**







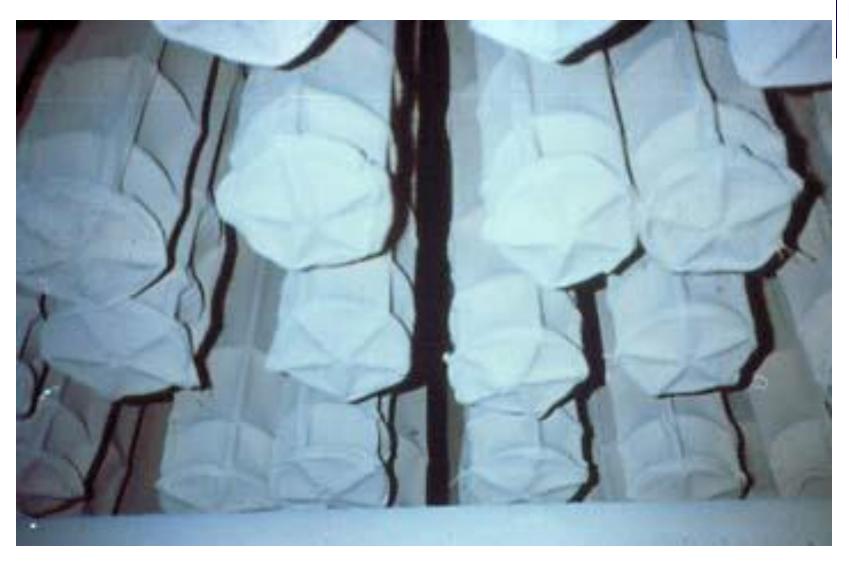








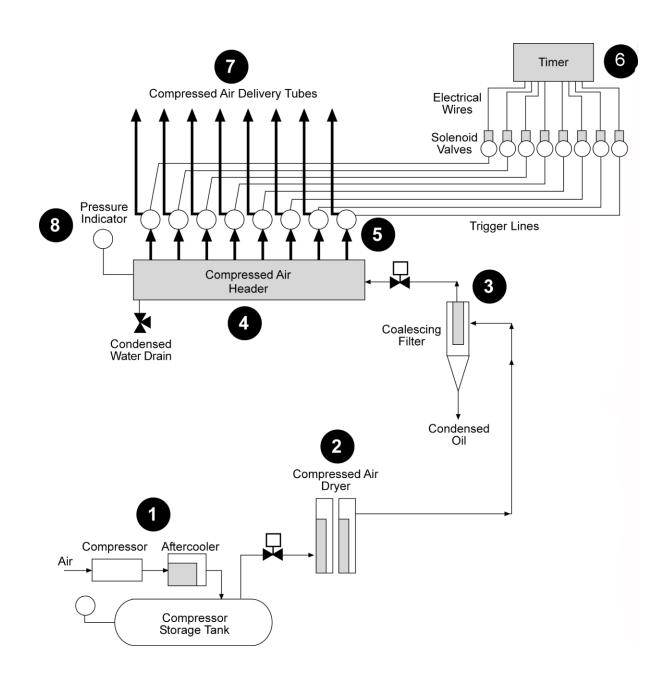










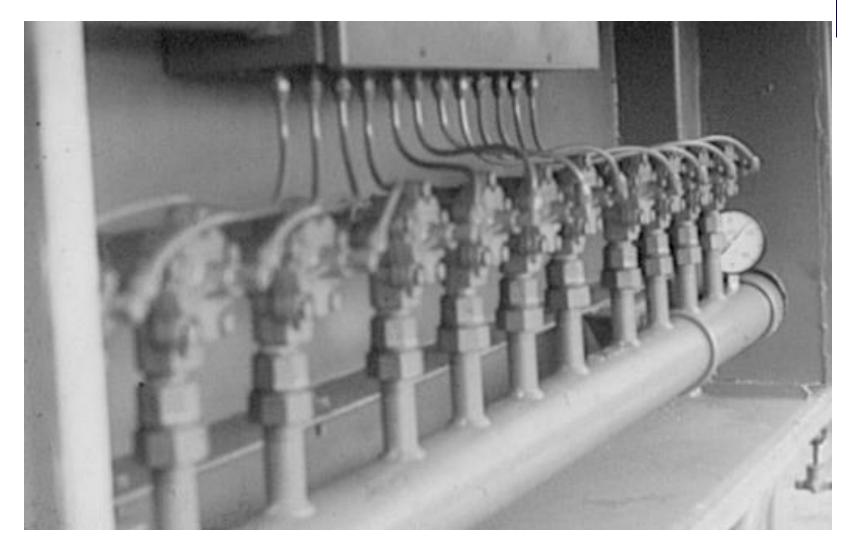












#### **Filtration Media**



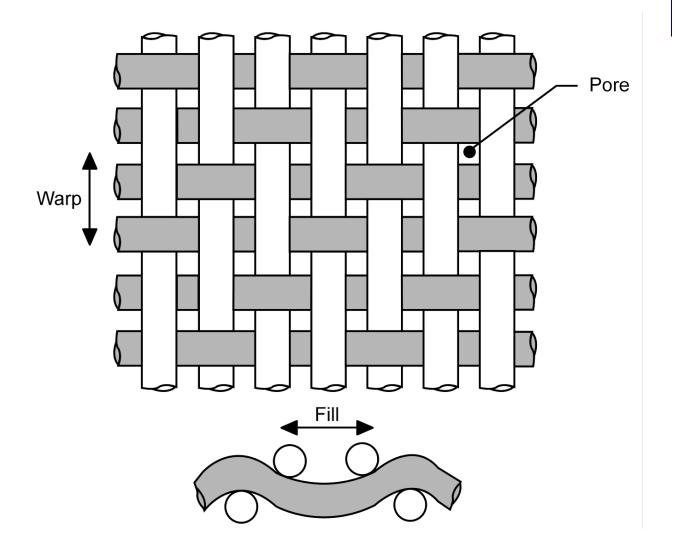


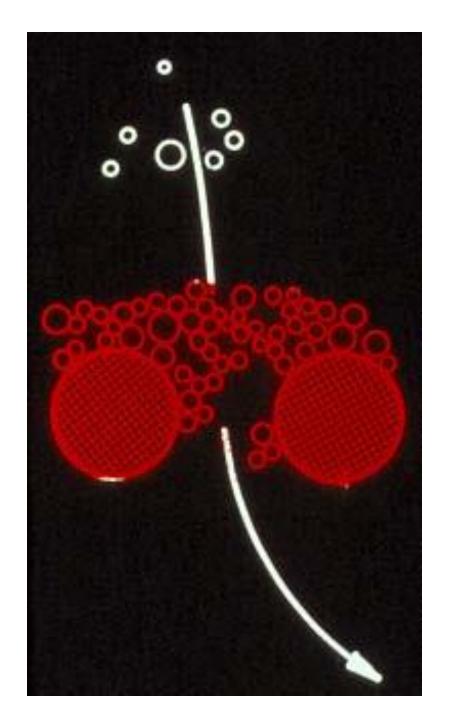
- Woven fabric
- Felted fabric
- Membrane fabric
- Sintered metal fiber
- Ceramic cartridge

#### **Woven Fabrics**



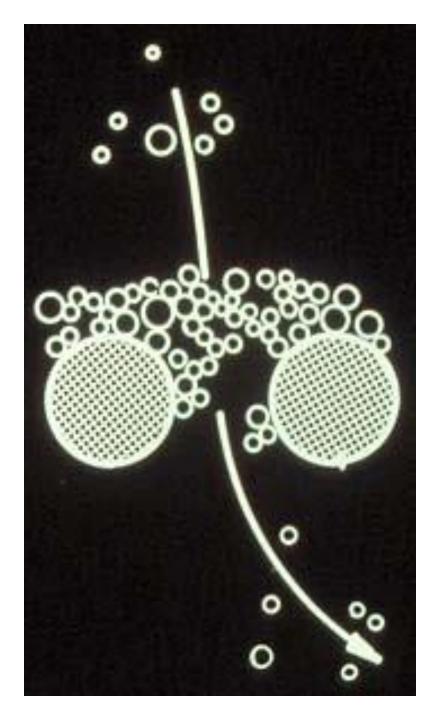
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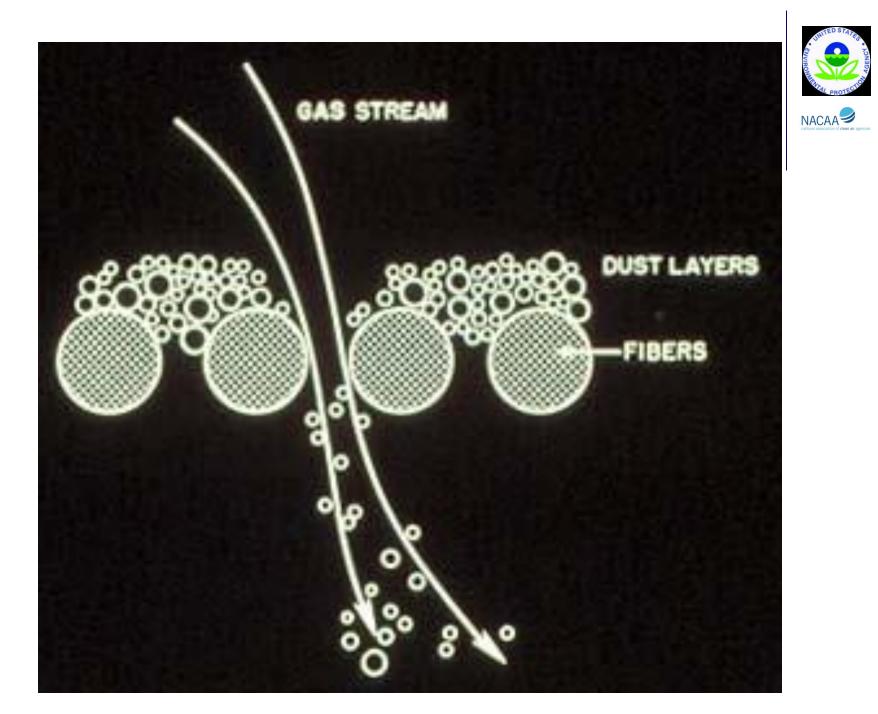








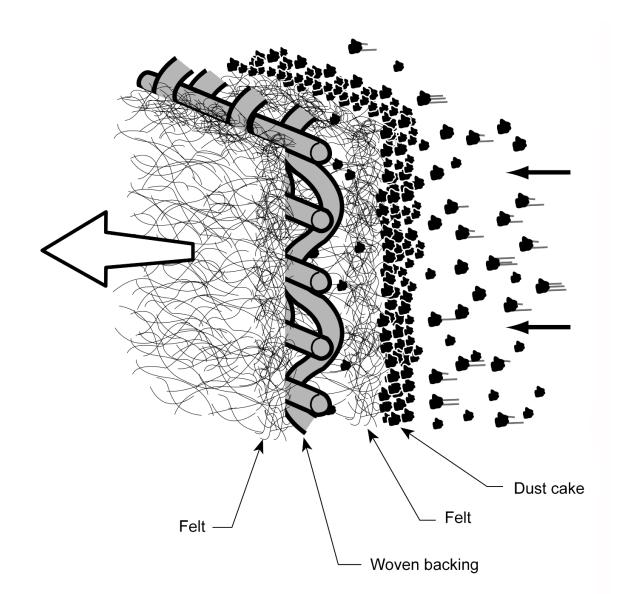




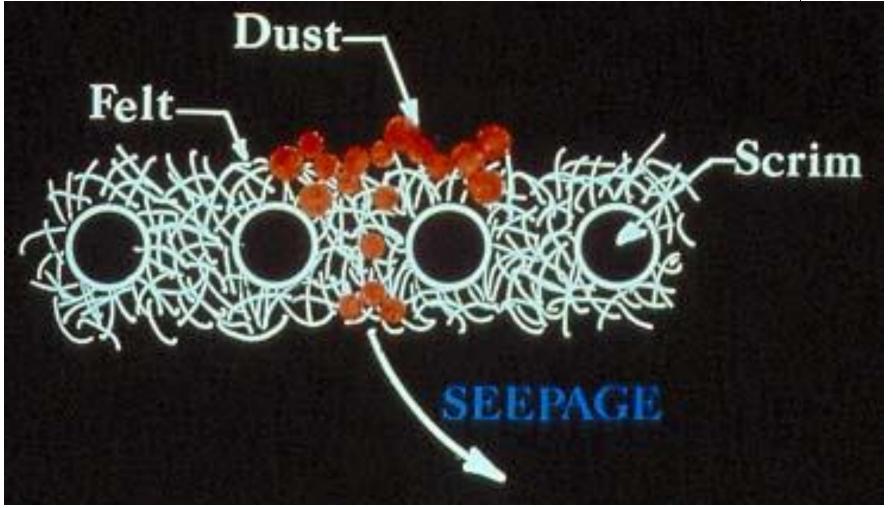
#### **Felted Fabrics**



NACAA







#### **Cartridge Filters**







#### **Cartridge Filters**



NACAA



# **Fabric Selection**



- Maximum temperature of the gas stream
- Composition of the gas stream
- Physical abrasion
- Fabric flex conditions

Temperature & Acid Resistance Characteristics						
Generic	Common or	Max. Temp. °F		Acid		
Name	Trade Name	Continuous	Surges	Resistance		
Natural Fiber, Cellulose	Cotton	180	225	Poor		
Polyolefin	Polyolefin	190	200	Good to Excellent		
Polypropylene	Polypropylene	200	225	Excellent		
Polyamide	Nylon®	200	225	Excellent		
Acrylic	Orlon <sup>®</sup>	240	260	Good		
Polyester	Dacron®	275	325	Good		
Aromatic Polyamide	Nomex®	400	425	Fair		
Polyphenylene Sulfide	Ryton®	400	425	Good		
Polyimide	P-84®	400	425	Good		
Fiberglass	Fiberglass	500	550	Fair		
Fluorocarbon	Teflon <sup>®</sup>	400	500	Excellent		
Stainless Steel	Stainless Steel	750	900	Good		
Ceramic	Nextel®	1300	1400	Good		

Fabric Resistance to Abrasion and Flex				
Generic Name	Common or Trade Name	<b>Resistance to</b> <b>Abrasion and Flex</b>		
Natural Fiber, Cellulose	Cotton	Good		
Polyolefin	Polyolefin	Excellent		
Polypropylene	Polypropylene	Excellent		
Polyamide	Nylon®	Excellent		
Acrylic	Orlon <sup>®</sup>	Good		
Polyester	Dacron <sup>®</sup>	Excellent		
Aromatic Polyamide	Nomex®	Excellent		
Polyphenylene Sulfide	Ryton®	Excellent		
Polyimide	P-84®	Excellent		
Fiberglass	Fiberglass	Fair		
Fluorocarbon	Teflon®	Fair		
Stainless Steel	Stainless Steel	Excellent		
Ceramic	Nextel®	Fair		



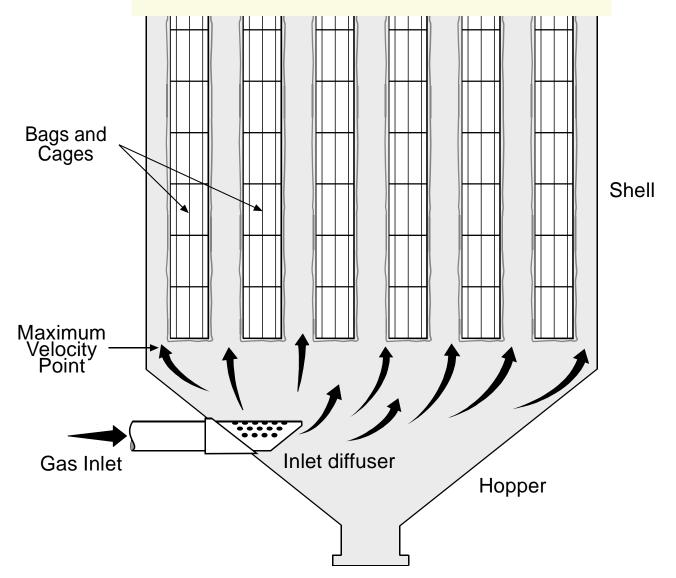
NACAA

# **Fabric Utilization**

- Gas approach velocity
- Bag spacing and length
- Bag reach and accessibility



#### **Gas Approach Velocity**



# Example 7-3



What is the difference in gas approach velocities for two identical pulse jet fabric filters with the following design characteristics?

Characteristic	Unit A	Unit B	
Compartment area, ft <sup>2</sup>	130	130	
Number of bags	300	300	
Bag diameter, in.	6	6	
Bag height, ft	10	10	
Air-to-cloth ratio,	5	8	
$(ft^3/min)/ft^2$			

#### **Solution**



The bag area for both units is identical. It is calculated using the circumference of the bag times the length.

Bag area =  $\pi$ DL =  $\pi$ (6 in.)(1 ft/12 in.)(10 ft) = 15.7 ft<sup>2</sup>/bag Total bag area = (300 bags)(15.7 ft<sup>2</sup>/bag) = 4,710 ft<sup>2</sup>

Total gas flow rate, Unit A =

$$\frac{5(ft^3 / \min)}{ft^2} (4,710 ft^2) = 23,550 ft^3 / \min$$

Total gas flow rate, Unit B =

$$\frac{8(ft^3 / \min)}{ft^2} (4,710 ft^2) = 37,680 ft^3 / \min$$

The area for gas flow at the bottom of the pulse jet bags is identical in both units.

# **Solution (continued)**



Area for flow = total area – bag projected area

= total area – (number of bags)(circular area of bag at bottom)

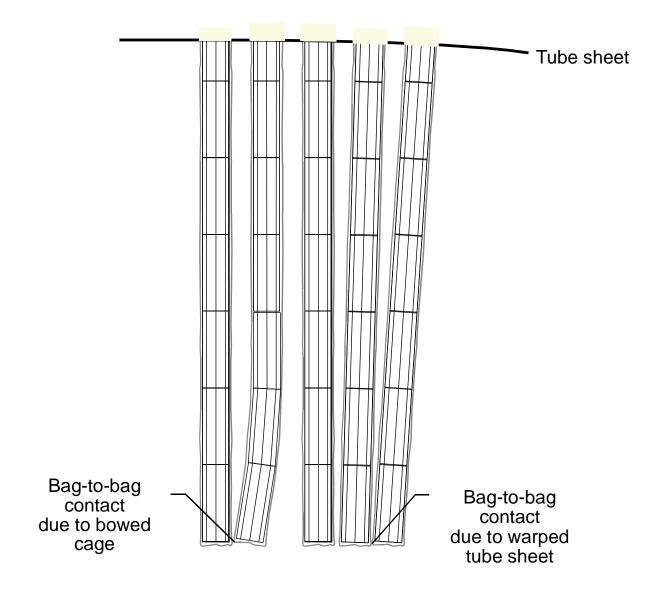
 $= 130 \text{ ft}^{2} - (300)(\pi D^{2}/4)$ = 130 ft^{2} - 58.9 ft^{2} = 71.1 ft^{2} Gas approach velocity for Unit A =  $\frac{23,550 \text{ ft}^{3} / \text{min}}{71.1 \text{ ft}^{2}} = 331 \text{ ft} / \text{min}$ 

Gas approach velocity for Unit B =  $\frac{37,680 \text{ ft}^3 / \text{min}}{71.1 \text{ ft}^2}$  = 530 ft / min

# **Bag Spacing and Length**



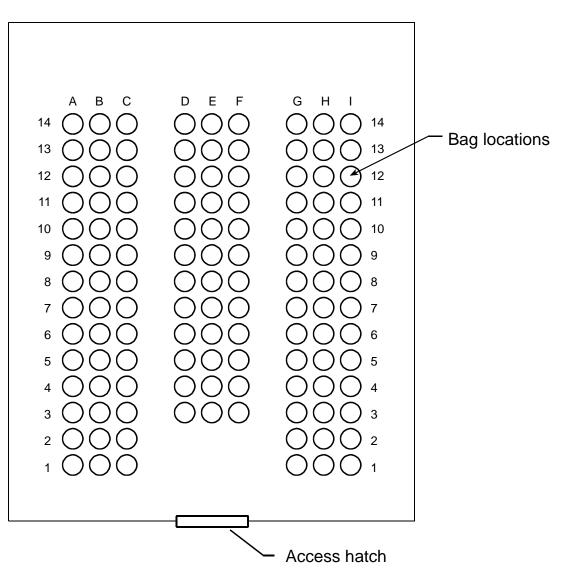
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# **Bag Reach and Accessibility**



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#### Instrumentation

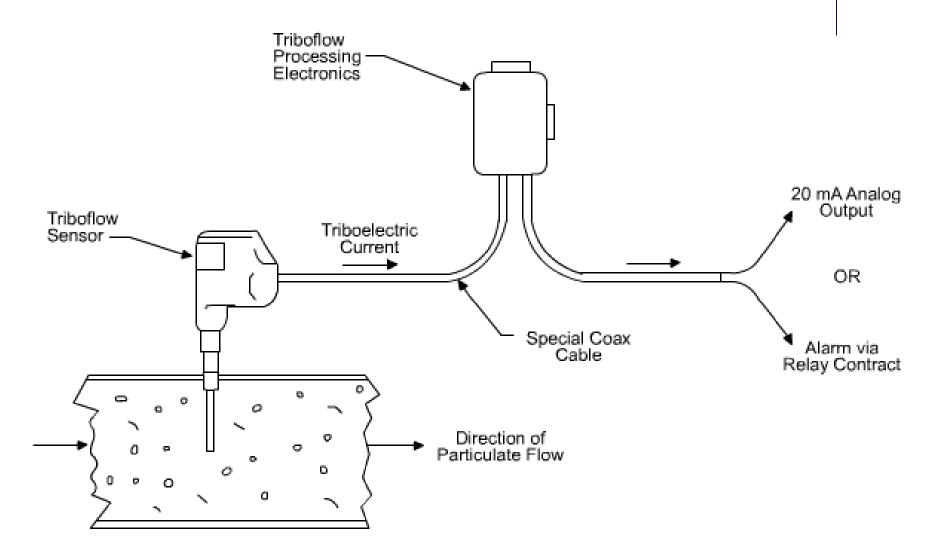




- Static pressure drop gauges
- Inlet and outlet gas temperature gauges
- Bag break detector
- Opacity monitor

### **Bag Break Detector**





# **Advantages and Disadvantages**

#### Advantages

High Collection Efficiency (>99%) Effective for a Wide Range of Dust Types Modules Can be Factory Assembled Operates Over Wide Range of Gas Flow Rates Reasonably Low Pressure Drop Good Efficiency for Small Particles Dry Collection and Disposal

Disadvantages Large Footprint Temperature Limitations Requires Dry Environment Fire or Explosion Potential High Maintenance Cost



### **Review Problems**



- 1. Calculate the net air-to-cloth ratio for a reverse air baghouse with 12 compartments containing 276 bags each.
- The diameter of each bag is 11 in, and the bag height is 28 ft. One of the compartments is always off-line for cleaning, and another is off-line for maintenance.

Use a gas flow rate of 350,000 acfm.

#### Solution #1



Individual bag area = 
$$\pi$$
Dh =  $\pi \left[ 11 in \left( \frac{1 ft}{12 in} \right) \right] (28 ft) = 80.6 \frac{ft^2}{bag}$ 

Total net bag area =  $80.6 \frac{\text{ft}^2}{\text{bag}} \left( 276 \frac{\text{bags}}{\text{compartment}} \right) (10 \text{ compartments}) = 222,456 \text{ ft}^2$ 

$$= \frac{Q}{A} = \frac{350,000 \frac{\text{ft}^3}{\text{min}}}{222,456 \text{ft}^2} = 1.57 \frac{\text{ft}}{\text{min}}$$

Net air-to-cloth ratio

#### **Review Problems**

NACAAO

2. Calculate the gas approach velocity for a pulse jet baghouse having a single compartment, 60 rows of bags with 10 bags each, and a bag diameter of 6 in.

Assume that the internal dimensions of the compartment are 6.5 ft x 40 ft.

Use a gas flow rate of 66,000 acfm.

# Total bachouse shell area = (6.5 ft)(40 ft) =

Total baghouse shell area =  $(6.5 \text{ ft})(40 \text{ ft}) = 260 \text{ ft}^2$ 

Bottom area of bag 
$$= \frac{1}{4} = \frac{1}{4} = \frac{1}{4} = 0.196 \frac{1}{bag}$$
  
Total bottom area  $= 0.196 \frac{\text{ft}^2}{\text{bag}} \left(10 \frac{\text{bags}}{\text{row}}\right) (60 \text{ rows}) = 118 \text{ft}^2$ 

Open area = total shell area - total bottom area =

 $260 \text{ ft}^2 - 118 \text{ ft}^2 = 142 \text{ ft}^2$ 

Gas approach velocity

Solution #2

$$= \frac{Q}{A} = \frac{\frac{66,000}{\frac{\text{ft}^3}{\text{min}}}}{142 \text{ ft}^2} = 465 \frac{\text{ft}}{\text{min}} = 7.75 \frac{\text{ft}}{\text{sec}}$$

 $\pi D^{2} = \pi \left[ 6 \sin \left( \frac{1 \text{ ft}}{12 \text{ in}} \right) \right]^{2} \qquad \text{ft}^{2}$ 



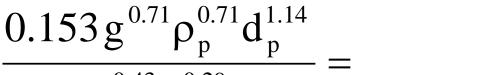
# **Review Problem #3**



- 3. Would a 150 µm size particle or particle agglomerate successfully settle by gravity in the pulse jet baghouse described in Problem 2?
- Assume a temperature of 20°C, a particle density of 1.0 g/cm<sup>3</sup>, and that the transitional region terminal settling velocity equation is appropriate for this particle size.

#### **Solution #3**





$$V_{t} = \frac{1}{\mu_{g}^{0.43} \rho_{g}^{0.29}} = \frac{1}{\mu_{g}^{0.43} \rho_{g}^{0.29}} = \frac{1}{1.59} \frac{1}{1.8 \times 10^{-4} \frac{g}{cm \cdot sec}} = \frac{1}{1.2 \times 10^{-3} \frac{g}{cm^{3}}} = \frac{1}{1.2 \times 10^{-3} \frac{g}{cm^{3}}} = \frac{1}{1.59} \frac{1}{1.59} \frac{1}{sec}$$

The 150  $\mu$ m particle will not settle. The upward velocity of the gas stream is much higher than the terminal settling velocity.

#### **Review Problem #4 & solution**



4. Calculate the static pressure difference between the clean gas plenum of a top access type pulse jet baghouse and the ambient air.

Assume that the inlet static pressure to the baghouse is - 4 in WC and the static pressure drop across the baghouse is 5 in WC.

#### Solution

Static pressure in the clean gas plenum = -4 in WC – (5 in WC) = -9 in WC

Since the ambient gauge pressure is 0 in WC, the static pressure difference between the clean gas plenum and the ambient air is 9 in WC.

#### **Review Problem #5**

5. It is proposed to install a pulse jet fabric filter with an air-to-cloth ratio of 2.5 ft/min to clean a 10,000 scfm air stream at 250°F.



Determine the filtering area required for this operation and, using the information below, choose an appropriate filter bag and determine how many will be needed.

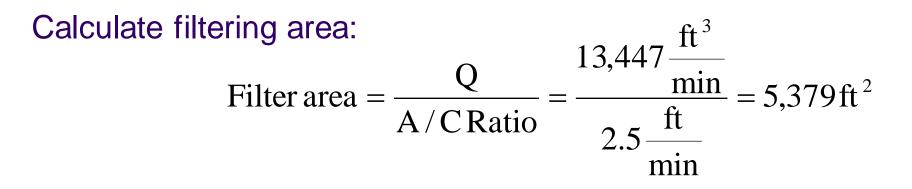
Filter bag	А	В	С	D
Tensile strength	Excellent	Very good	Fair	Excellent
Maximum temperature (°F)	260	275	260	220
Relative cost per bag	2.6	3.8	1.0	2.0
Size	4¾" x 10'	6" x 10'	6" x 14'	6" x 14'

#### **Solution #5**

NACAA

Calculate actual flow rate:

$$Q = 10,000 \frac{\text{ft}^3}{\text{min}} \left( \frac{250^\circ \text{F} + 460}{68^\circ \text{F} + 460} \right) = 13,447 \frac{\text{ft}^3}{\text{min}}$$



Bag D can be eliminated because its maximum temperature is too low. Bag C can be eliminated because it has only fair tensile strength.

Only Bags A and B will be considered further.

#### **Solution (continued)** For Bag A: NACAA Bag Area $= \pi Dh = \pi \left| 4.75 \operatorname{in} \left( \frac{1 \operatorname{ft}}{12 \operatorname{in}} \right) \right| (10 \operatorname{ft}) = 12.44 \frac{\operatorname{ft}^2}{\operatorname{bag}} \right|$ $\frac{5,379 \text{ ft}^2}{12.44 \frac{\text{ft}^2}{\text{bag}}} = 432 \text{ bags} \qquad \begin{array}{l} \text{Relative} \\ \text{Cost} \end{array} = \left(\frac{2.6}{\text{bag}}\right) 432 \text{bags} = 1,123 \end{array}$ Number of Bags For Bag B: $= \pi \mathrm{Dh} = \pi \left| 6 \mathrm{in} \left( \frac{1 \mathrm{ft}}{12 \mathrm{in}} \right) \right| (10 \mathrm{ft}) = 15.71 \frac{\mathrm{ft}^2}{\mathrm{bag}}$ Bag Area Relative Cost $=\left(\frac{3.8}{\text{bag}}\right)342\text{bags} = 1,300$ Number $\frac{5,379 \,\text{ft}^2}{15.71 \frac{\text{ft}^2}{\text{ft}^2}} = 342 \,\text{bags}$ of Bags bag

#### Bag A should be chosen b/c of its lower relative cost.



#### **Chapter 8**



#### **Particle Collection Steps**

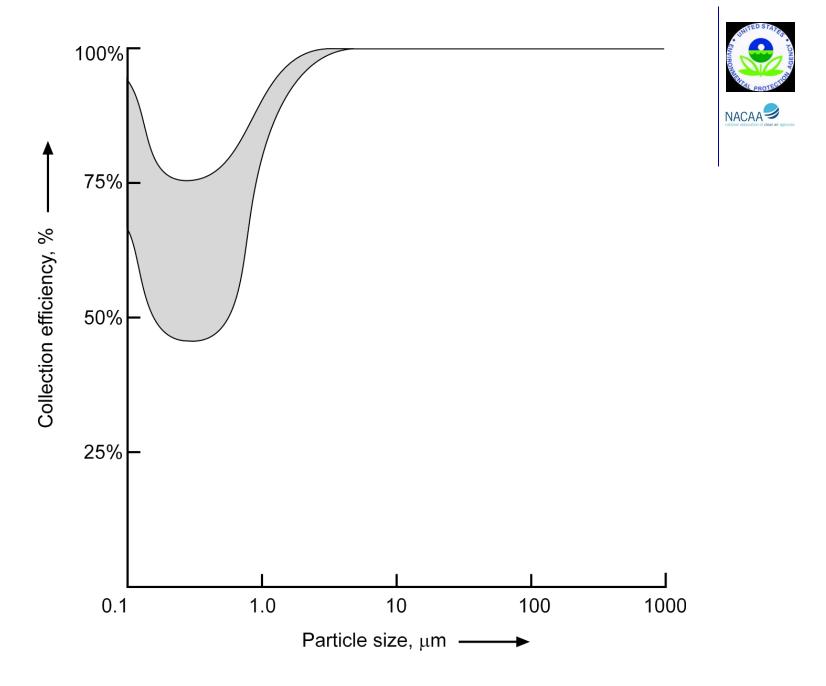


- Capture particulate matter in droplets, liquid sheets or liquid jets
- Capture droplets entrained in the gas stream
- Treat contaminated liquid prior to reuse or discharge

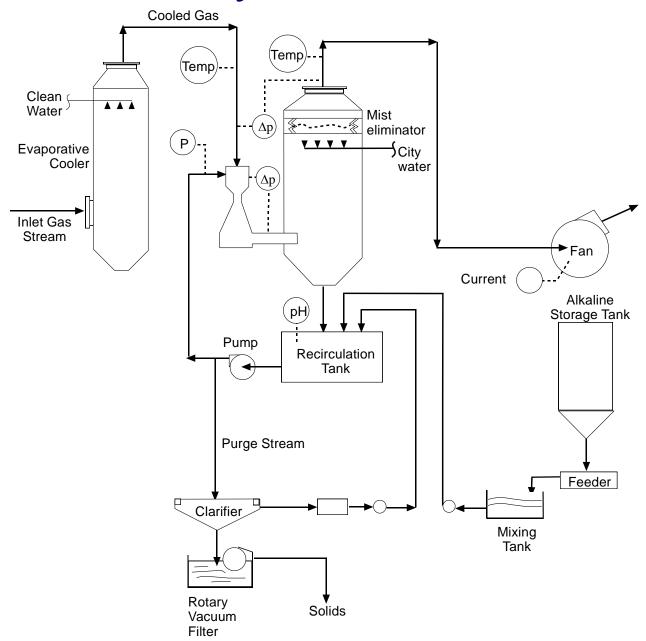
#### **Collection Mechanisms**



- Inertial impaction
- Brownian motion
- Electrostatic attraction



#### Wet Scrubber System





#### **Operational Issues**



 Gas cooling
 Liquid to Gas Ratio
 Alkali addition
 Wastewater treatment and Liquid Recirculation

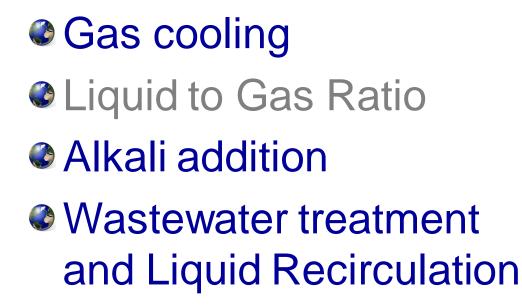
#### **Operational Issues**

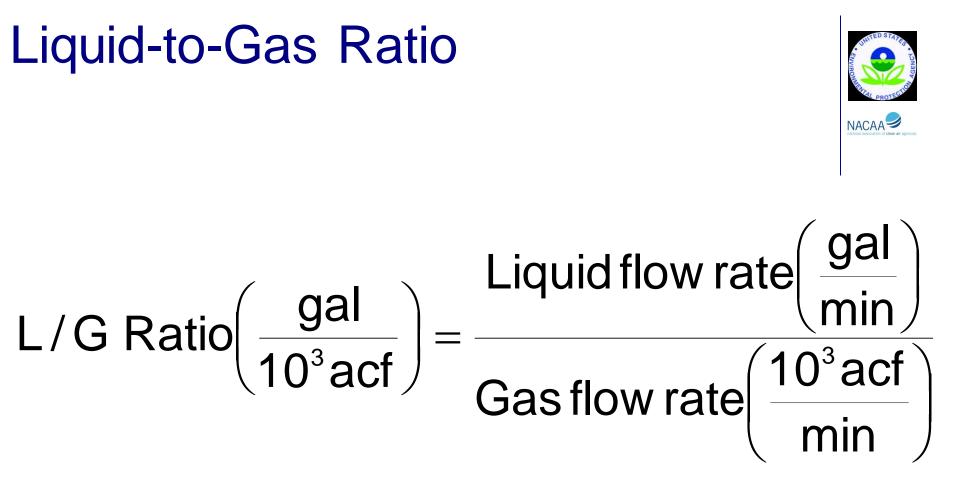


 Gas cooling
 Liquid to Gas Ratio
 Alkali addition
 Wastewater treatment and Liquid Recirculation

#### **Operational Issues**







# Example 8-1

What is the design liquid-to-gas ratio for a scrubber system that has an outlet gas flow rate of 15,000 acfm, a pump discharge rate of 100 gpm, and a liquid purge rate of 10 gpm?

The purge stream is withdrawn from the pump discharge side.

$$\frac{L}{G} = \frac{Inlet \ liquid \ flow (gpm)}{Outlet \ gas \ flow \ rate (1,000 \ acfm)}$$

Inlet liquid flow = 100 gpm - 10 gpm = 90 gpm

 $\frac{L}{G} = \frac{90 \text{ gpm}}{15,000 \text{ acfm}} = 0.006 \frac{\text{gal}}{\text{acf}} = 6.0 \frac{\text{gal}}{1,000 \text{ acf}}$ 







 Gas cooling
 Liquid to Gas Ratio
 Alkali addition
 Wastewater treatment and Liquid Recirculation

#### Alkali Requirements and Addition



SO3= + Ca(OH)2 → CaSO4 + H2O Reaction 8-1 2HCI + Ca(OH)2 → CaCl2 + 2H2O Reaction 8-2 2HF + Ca(OH)2 → CaF2 + 2H2O Reaction 8-3

#### Example 8-3

Calculate the amount of calcium hydroxide (lime) needed to neutralize the HCl absorbed from a gas stream having 50 ppmv HCl and a flow rate of 10,000 scfm.

Assume an HCI removal efficiency of 95%.

#### Solution

Calculate HCI absorbed in the scrubbing liquid:

$$50 \text{ ppmv} = \frac{50 \text{ ft}^3 \text{ HCl}}{10^6 \text{ ft}^3 \text{ total}} = 0.00005 \frac{\text{ ft}^3 \text{ HCl}}{\text{ ft} \text{ total}} = 0.00005 \frac{\text{ lb} - \text{ mole HCl}}{\text{ lb} - \text{ mole total}}$$



#### And then...

#### Solution (continued)

HCl absorbed = 10,000 scfm 
$$\left(\frac{lb - mole}{385.4 scf}\right) \left(0.00005 \frac{lb - mole HCl}{lb - mole total}\right) (0.95)$$
  
=  $0.00123 \frac{lb - mole}{min}$   
Ca(OH)<sub>2</sub> required =  $\left(\frac{1 \ lb - mole \ Ca(OH)_2}{2 \ lb - mole \ HCl}\right) \left(0.00123 \frac{lb - mole \ HCl}{min}\right)$   
=  $0.00062 \frac{lb - mole}{min} \left(74 \frac{lb \ Ca(OH)_2}{lb - mole}\right) \left(60 \frac{min}{hr}\right)$   
=  $2.75 \frac{lb}{hr}$ 





Gas cooling
Liquid to Gas Ratio
Alkali addition
Wastewater treatment and

Liquid Recirculation

#### Factors Affecting Liquid Purge Rate



- Rate of particulate matter capture
- Maximum acceptable suspended solids concentration
- Rate of dissolved solids precipitation
- Rate of chlorine or fluorine accumulation

## **Applicability Limitations**



- Particle size distribution
- Water availability
- Wastewater treatment
- Condensation plume

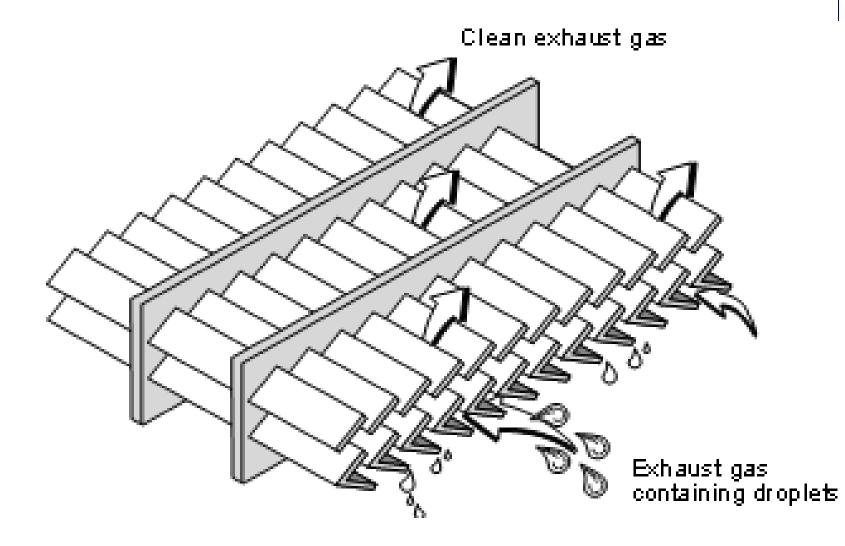
#### **Types of Mist Eliminators**

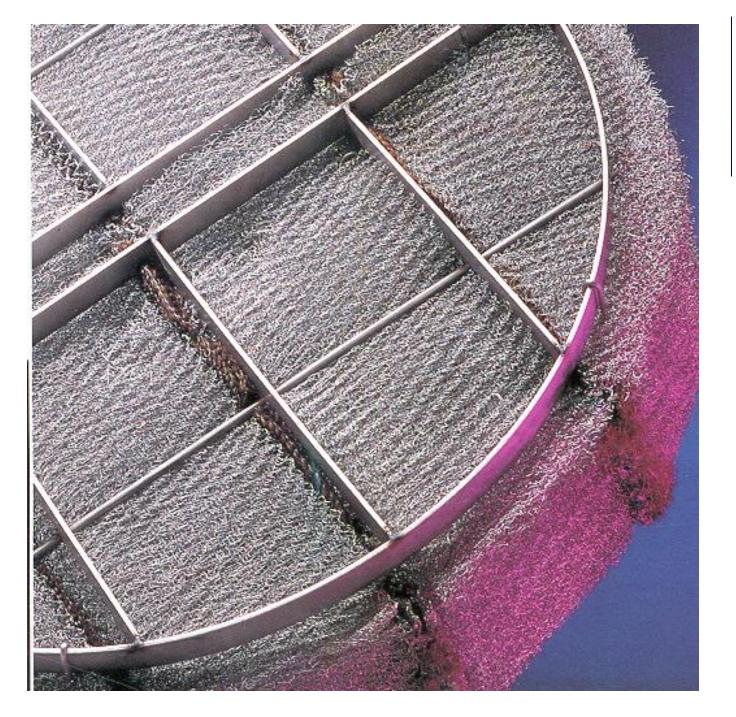


Chevrons
Mesh and woven pads

Cyclones



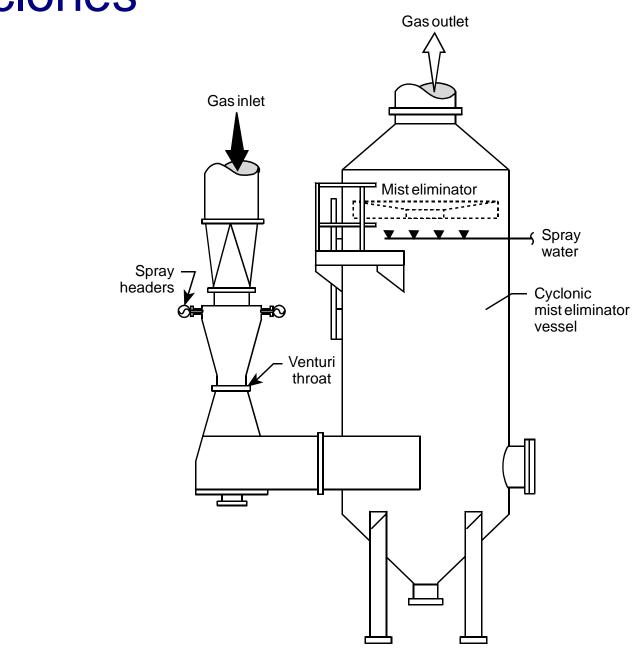








## Cyclones





#### Mist Eliminator Velocity



# Velocity = $\frac{\text{Gas flow rate (ACFM) (min/60 sec)}}{\text{Mist eliminator area (ft}^2)}$

#### Maximum Velocities



Mist Eliminator Type	Orientation	Maximum Gas Velocity, ft/sec
Zigzag	Horizontal	15 – 20
Zigzag	Vertical	12 – 15
Mesh Pad	Horizontal	15 – 23
Mesh Pad	Vertical	10 – 12
Woven Pad	Vertical	8 – 15
Tube Bank	Horizontal	18 – 23
Tube Bank	Vertical	12 – 16

#### Example 8-4

Estimate the gas velocity through a mist eliminator having a diameter of 6.5 feet, an average gas flow rate of 4,000 dscfm\*, and a peak gas flow rate of 4,760 dscfm.

The peak gas stream temperature is 130°F, the static pressure during peak flow in the vessel is – 30 in. WC, and the barometric pressure is 29.4 in. Hg.

The moisture content of the gas stream is 6% by volume.

\*dscfm = dry standard cubic feet per minute



#### **Solution**



The gas velocity should be evaluated under peak flow conditions because this is the time when reentrainment is most probable.

Convert the gas flow rate to actual conditions:

scfm = 
$$\frac{\text{dscfm}}{\left(\frac{100 - \% \text{H}_2 \text{O}}{100}\right)} = \frac{4,760 \,\text{dscfm}}{\left(\frac{100 - 6}{100}\right)} = 5,064 \,\text{scfm}$$

#### Solution (continued)



Absolute pressure = 29.4 in. Hg + 
$$\left[-30 \text{ in. WC}\left(\frac{1 \text{ in. Hg}}{13.6 \text{ in. WC}}\right)\right] = 27.19 \text{ in. Hg}$$

Absolute temperature =  $130^{\circ}F + 460^{\circ} = 590^{\circ}R$ 

acfm = 5,064 
$$\left(\frac{590^{\circ}\text{R}}{528^{\circ}\text{R}}\right) \left(\frac{29.92 \text{ in. Hg}}{27.19 \text{ in. Hg}}\right) = 6,227 \text{ acfm}$$
  
Area =  $\frac{\pi d^2}{4} = \frac{\pi (6.5 \text{ ft})^2}{4} = 33.2 \text{ ft}^2$   
Velocity =  $\frac{6,227 \frac{\text{ft}^3}{\text{min}} \left(\frac{\text{min}}{60 \text{ sec}}\right)}{33.2 \text{ ft}^2} = 3.13 \text{ sec}$ 

### Scrubber Systems

- Spray tower scrubbers
- Orifice scrubbers
- Mechanically aided scrubbers
- Packed bed scrubbers
- Ionizing wet scrubbers
- Tray or plate scrubbers
- Catenary grid scrubbers
- Venturi scrubbers
- Collision scrubbers



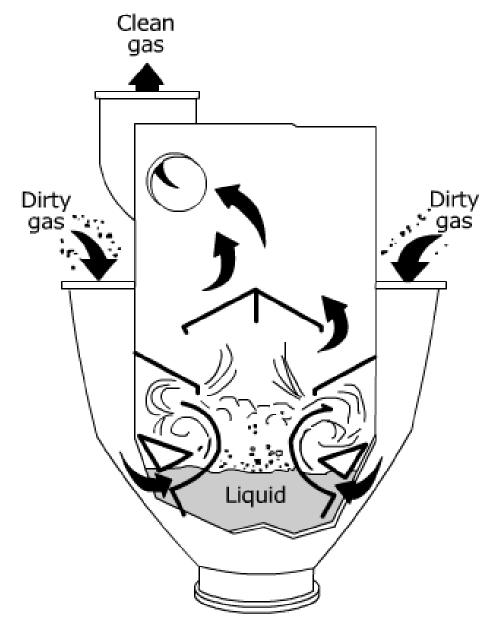




# Spray

## Tower

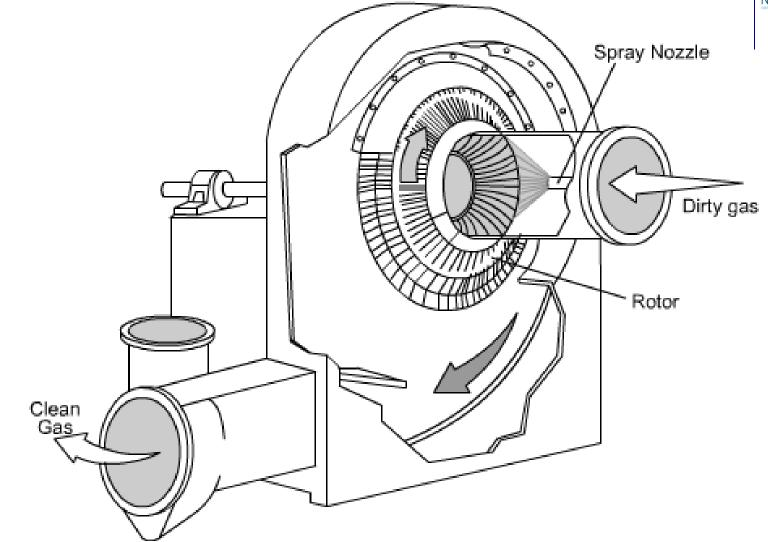
#### **Orifice Scrubber**

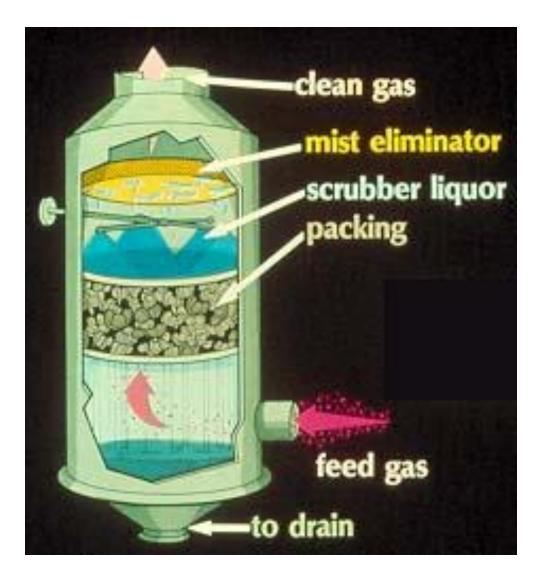




#### Mechanically Aided Scrubber







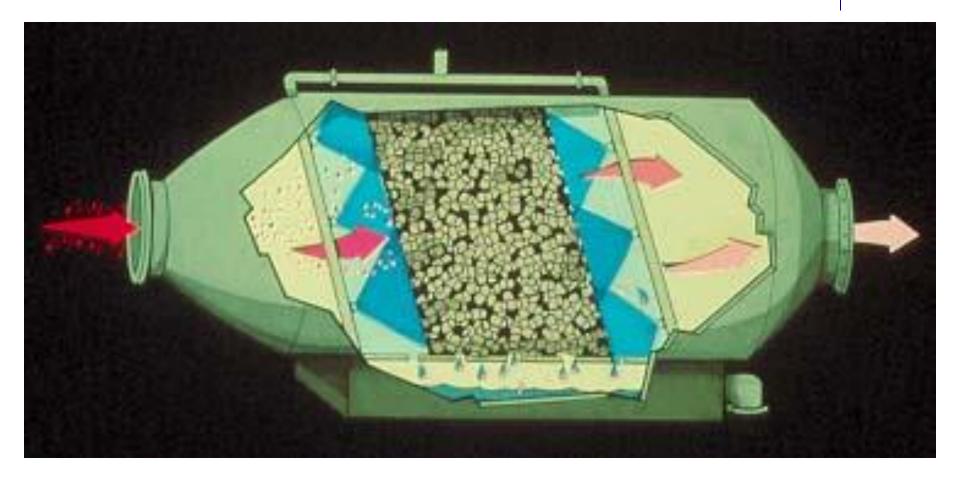


# Packed

Bed

#### Horizontal Packed Bed

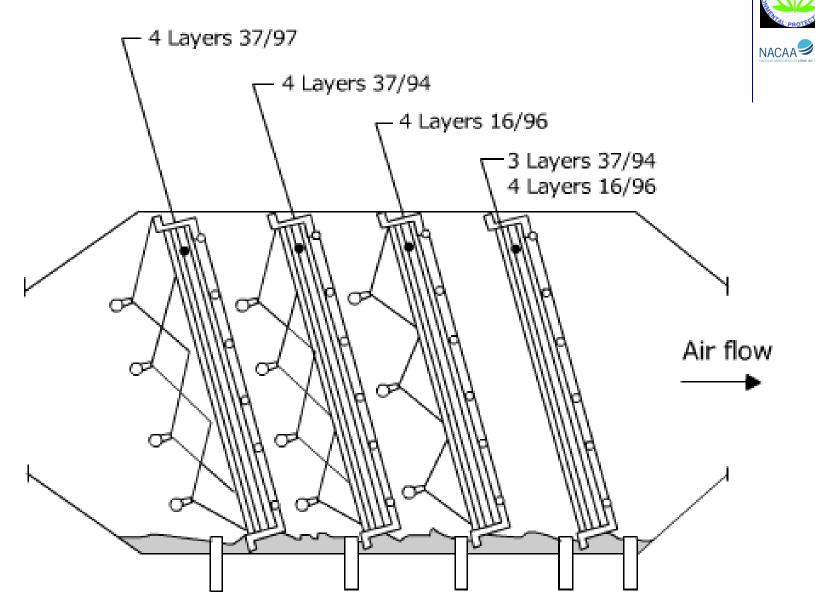




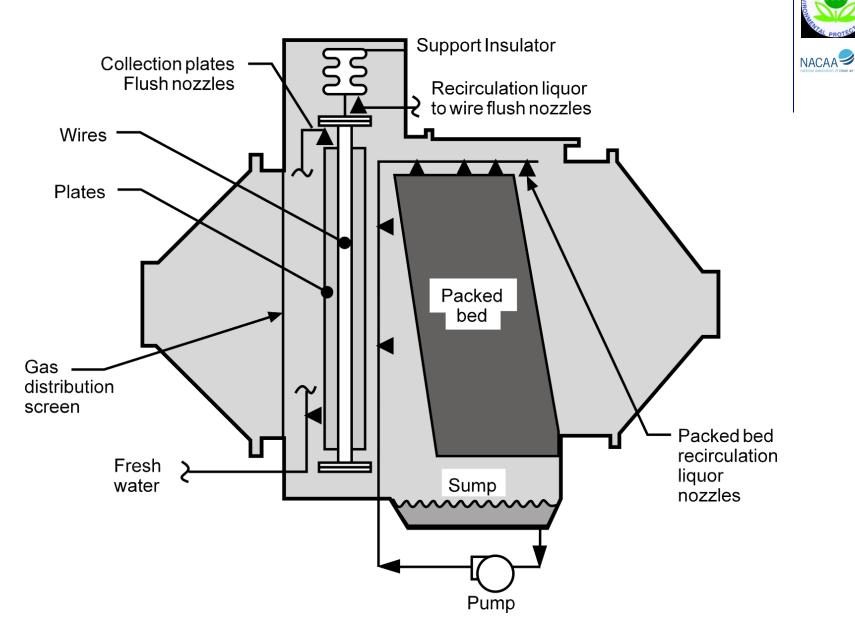




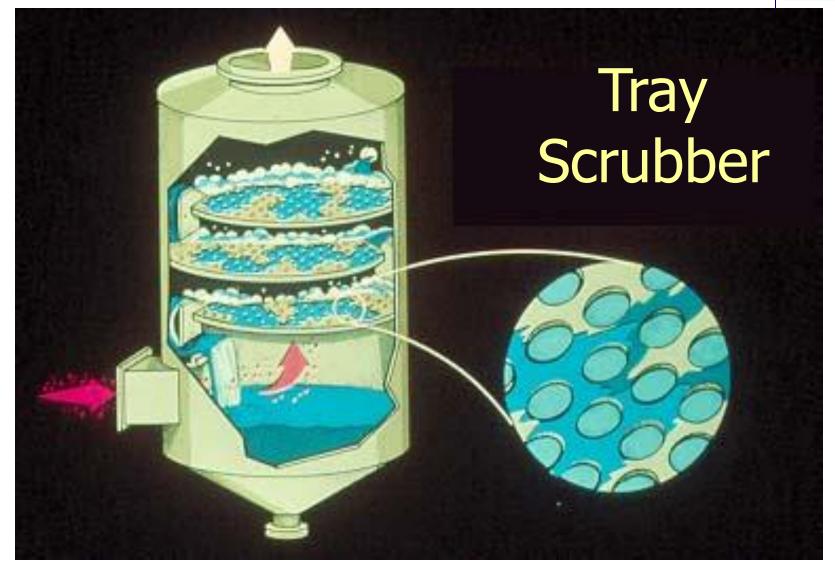
#### Fiber Bed Scrubber



## Ionizing Wet Scrubber





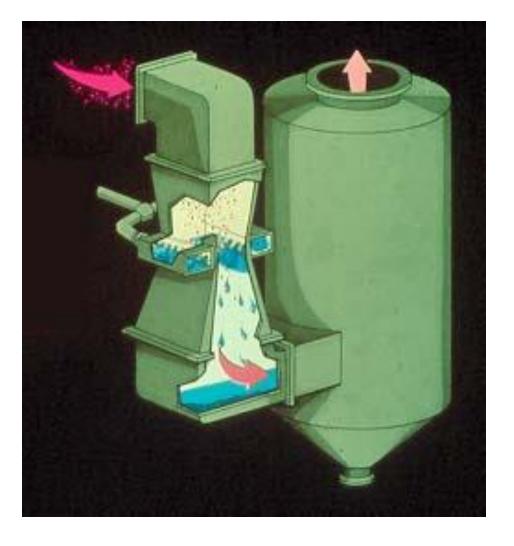


#### **Catenary Grid Scrubber**

Gas outlet Catenary-shaped, open-wire mesh grids < Liquid inlet Gas inlet Liquid outlet

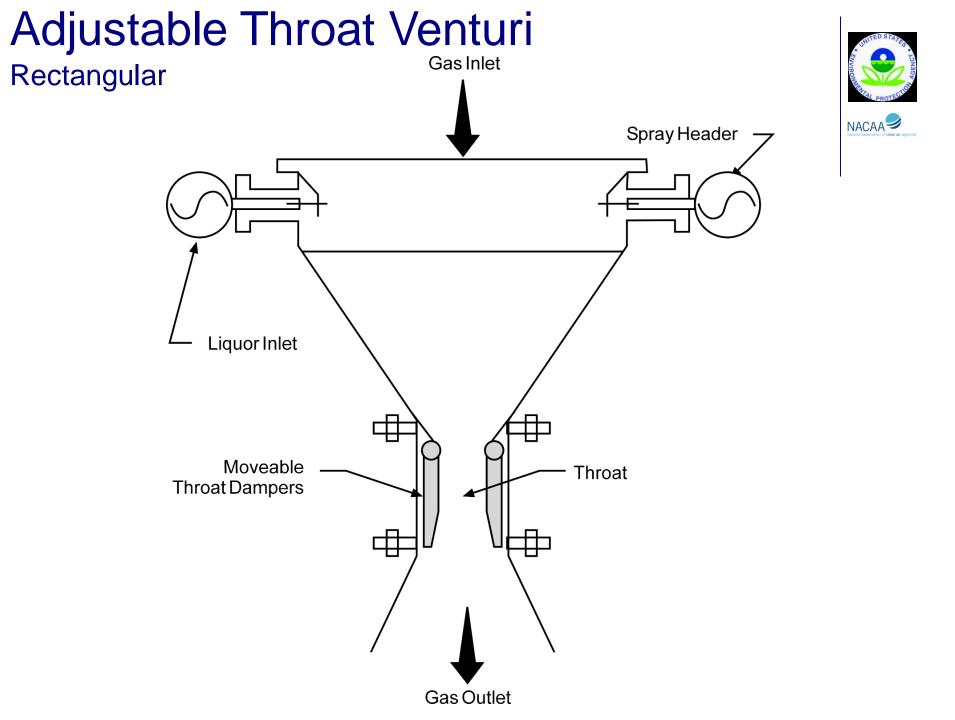


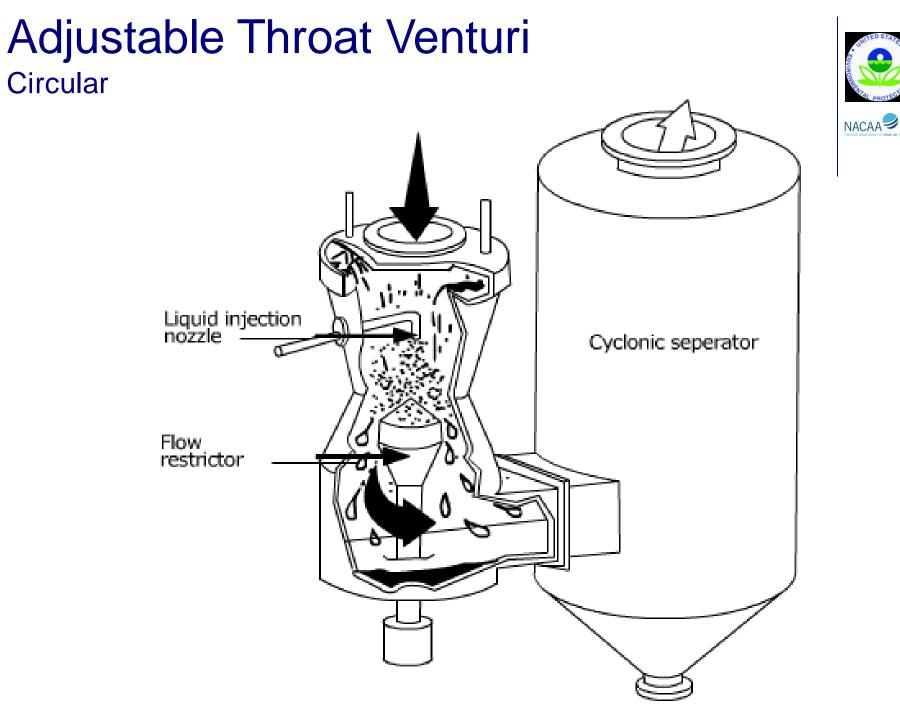






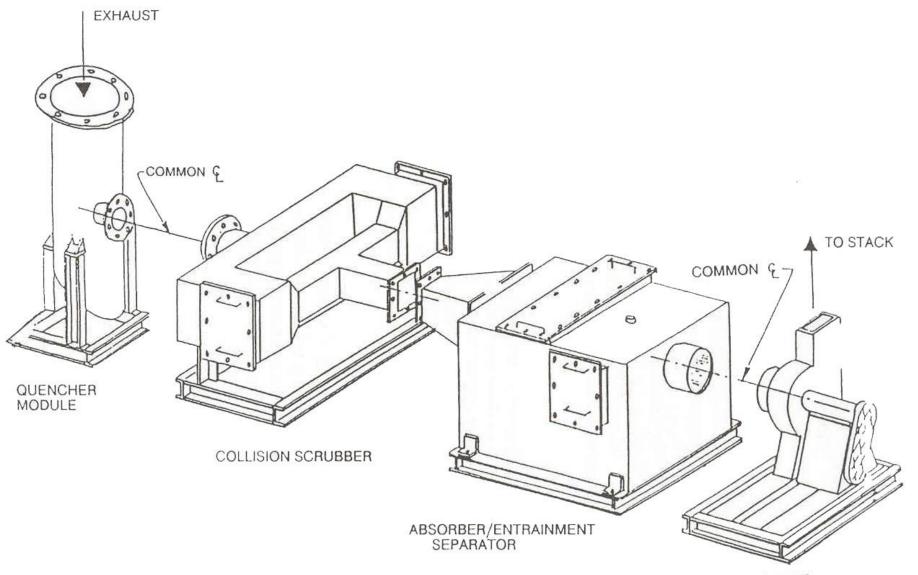
# Scrubber



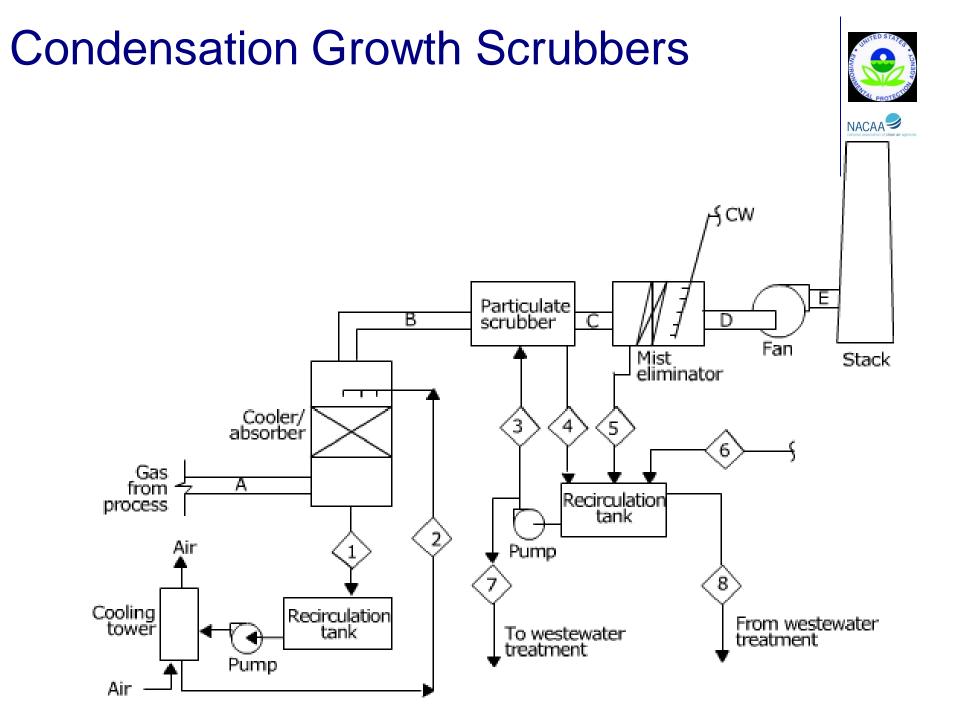


#### **Collision Scrubber**





FAN MODULE



#### **Performance Evaluation**



- Empirical evaluation
- Pilot scale tests
- Theoretical models

#### **Inertial Impaction Parameter**



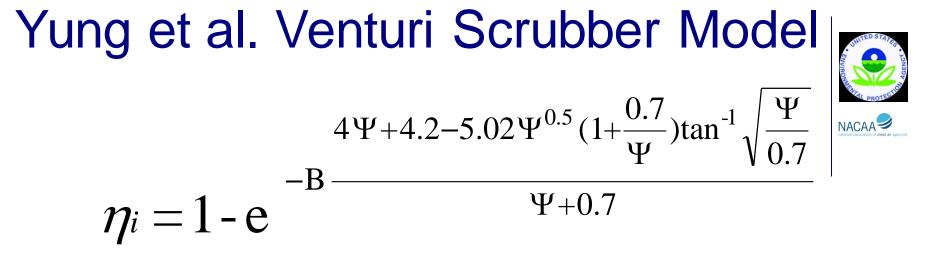
 $\frac{C_c d_p^2 \rho_p V}{18 \mu_g D_c}$ 

where

 $C_c$  = Cunningham slip correction factor

- d<sub>p</sub> = physical particle diameter, cm
- $\rho_p$  = particle density, gm/cm<sup>3</sup>
- V = difference in velocities of particle and target, cm/sec
- D<sub>c</sub> = target diameter, cm

 $\mu_g$  = gas viscosity, gm/cm • sec



where  $\eta_i$ = penetration for particle size i

= parameter defined below

 $\Psi$  = impaction parameter at throat entrance, dimensionless

$$\mathbf{B} = \left(\frac{\mathbf{L}}{\mathbf{G}}\right) \frac{\rho_{\mathrm{l}}}{\rho_{\mathrm{g}} \mathbf{C}_{\mathrm{D}}}$$

B

where

 $\begin{array}{l} L/G = liquid \ to \ gas \ ratio, \ dimensionless \\ \rho_{1,} \ \rho_{g} = \ liquid \ and \ gas \ density, \ kg/m^{3} \\ C_{D} \ \ = \ drag \ coefficient \ (liquid \ at \ the \ throat) \end{array}$ 

$$\Psi = \frac{\mathrm{d}^2 v_{gt} C_c \rho_p}{9\mu_g d_d}$$

 $\begin{array}{ll} d &= \mbox{ particle physical diameter, cm} \\ v_{gt} &= \mbox{ gas velocity in throat, cm/sec} \\ \mu_g &= \mbox{ gas viscosity, gm/cm·sec} \\ d_d &= \mbox{ droplet diameter, cm} \\ C_c &= \mbox{ Cunningham slip corr. factor} \\ \rho_p &= \mbox{ particle density (gm/cm^2)} \end{array}$ 

# Calvert Spray Tower Model $P_{i} = e^{-\left[\frac{0.75 v_{t} \eta_{i} Z}{r_{d} (v_{t} - v_{G})}\right] \left[\frac{L}{G}\right]} \qquad \eta_{i} = \left[\frac{\Psi_{i}}{(\Psi_{i} + 0.7)}\right]^{2}$

#### where

- $P_i$  = penetration for particle size I (penetration = 1 collection efficiency)
- $\Psi_i$  = impaction parameter, dimensionless
- $v_t$  = droplet terminal settling velocity, cm/sec.
- $\eta_i$  = efficiency due to impaction parameter, dimensionless
- Z = scrubber height, cm
- $r_d = droplet radius, cm$
- $v_G$  = gas superficial velocity, cm/sec
- L/G = liquid to gas ratio, dimensionless

## **Calvert Tray Tower Model**



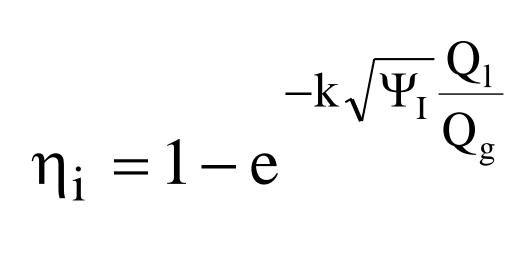
An equation for estimating the collection efficiency of a single size particle has been developed by Calvert et al for counter-current spray tower scrubbers:

$$\eta_{i} = 1 - e^{-\left[\frac{1.5v_{t}\eta_{I}z}{d_{d}(v_{t} - v_{g})}\right]\left(\frac{L}{G}\right)}$$

#### Where:

- $\eta_i$  = collection efficiency for particle size i
- v<sub>t</sub> = droplet terminal settling velocity (cm/sec)
- $\eta_{I}$  = single droplet collection efficiency due to impaction (dimensionless)
- z = scrubber height (cm)
- d<sub>d</sub> = droplet diameter (cm)
- v<sub>g</sub> = gas velocity (cm/sec)
- L/G = liquid to gas ratio (dimensionless; i.e., liters/min per liters/min)

Johnstone model for estimating the collection efficiency for a single size particle (Venturi Scrubber)



#### Where:

- $\eta_i \ k \ \Psi_l$
- = collection efficiency for particle size i
  - = constant (1,000 ft3/gal)
  - = inertial impaction parameter (dimensionless)
- $Q_{I}/Q_{g}$  = liquid to gas ratio (gal/1,000 ft<sup>3</sup>)

In this relationship, the inertial impaction parameter is calculated using the gas velocity in the throat. The constant, k, is typically 0.1-0.21,000 ft<sup>3</sup>/gal.



#### Instrumentation



- Inlet and outlet gas stream temperatures
- Inlet and purge liquid flow rates
- Recirculation pump discharge pressure
- Liquid distribution header pressure
- Inlet and outlet liquid pH
- Scrubber pressure drop
- Mist eliminator pressure drop

#### Advantages and Disadvantages

Venturi Scrubbers Advantages High Collection Efficiency Capable of Handling Flammable and Explosive Dusts Can Handle Mists Low Maintenance Simple Design and Easy to Install Provides Cooling for Hot Gases Neutralizes Corrosive Gases and Dusts

Disadvantages

Waste Water Must be Treated Collected Particulates are in Sludge Form High Corrosion Potential High Pressure Drop May Require Protection Against Freezing Final Exhaust Must be Reheated Sludge Disposal May be Expensive



#### **Review Problems**



1. Calculate the liquid-to-gas ratio for a scrubber system with a gas flow rate of 4,000 ft3/sec and a recirculation liquor flow rate of 2,000 gal/min.

Is this value in the normal range for a particulate matter wet scrubber? Solution

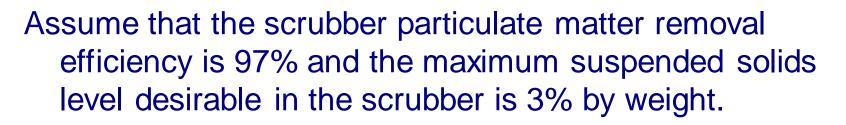
Gas Flow Rate 
$$\left(4,000\frac{\text{ft}^3}{\text{sec}}\right)\left(60\frac{\text{sec}}{\text{min}}\right) = 240,000\frac{\text{ft}^3}{\text{min}}$$
  
Liquid-to-gas ratio  $\frac{2,000\frac{\text{gal}}{\text{min}}}{240\frac{1,000\text{ ft}^3}{\text{min}}} = 8.33\frac{\text{gal}}{1,000\text{ ft}^3}$ 

min

This is within the normal range of 4-20 gal/1,000 acf

#### **Review Problems**

1. Estimate the liquid purge rate for a scrubber system treating a gas stream of 25,000 scfm with a particulate matter loading of 1.0 grains per scf.



#### Solution

Calculate the inlet particulate mass:

Inlet mass = 25,000 
$$\frac{\text{ft}^3}{\text{min}} \left( \frac{1.0 \text{ grains}}{\text{ft}^3} \right) \left( \frac{\text{lb}}{7,000 \text{ grains}} \right) = 3.57 \frac{\text{lb}}{\text{min}}$$



#### And then...

#### Solution #2 (continued)



Collected mass = 0.97 (Inlet mass) = 3.46  $\frac{\text{lb}}{\text{min}}$ 

Purge solids of 3.46 lb/min are 3% of the total purge stream, therefore:

Purge stream = 
$$\frac{3.46 \frac{\text{lb}}{\text{min}}}{0.03} = 115.3 \frac{\text{lb}}{\text{min}}$$

And then...

#### Solution #2 (continued)

A stream with 3% suspended solids has a specific gravity of about 1.03, therefore:

Purge stream density = 
$$\left(8.34 \frac{\text{lb water}}{\text{gal}}\right)(1.03) = 8.59 \frac{\text{lb}}{\text{gal}}$$

Purge stream flow rate = 
$$\frac{115.3 \frac{\text{lb}}{\text{min}}}{8.59 \frac{\text{lb}}{\text{gal}}} = 13.4 \frac{\text{gal}}{\text{min}}$$



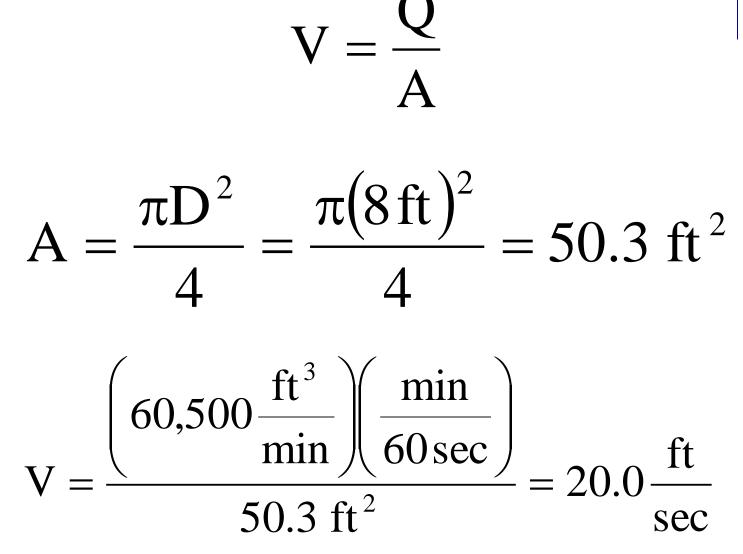
#### **Review Problem #3**



- 3. A chevron mist eliminator is 8 ft in diameter. The gas flow rate through the scrubber system has been measured at 60,500 acfm.
- a. What is the average velocity through the mist eliminator?
- b. What is the average velocity if 40% of the mist eliminator is completely blocked due to solids accumulation? Is this velocity within the normal operating range of a vertically mounted chevron mist eliminator?

Solution for part a:





#### Solution for part b:



 $A_{open} = 0.6A = 0.6(50.3) = 30.2 \text{ ft}^2$ 

$$V = \frac{\left(60,500 \frac{\text{ft}^3}{\text{min}}\right) \left(\frac{\text{min}}{60 \text{ sec}}\right)}{30.2 \text{ ft}^2} = 33.4 \frac{\text{ft}}{\text{sec}}$$

This is not within normal operating range.

#### **Review Problem #4**

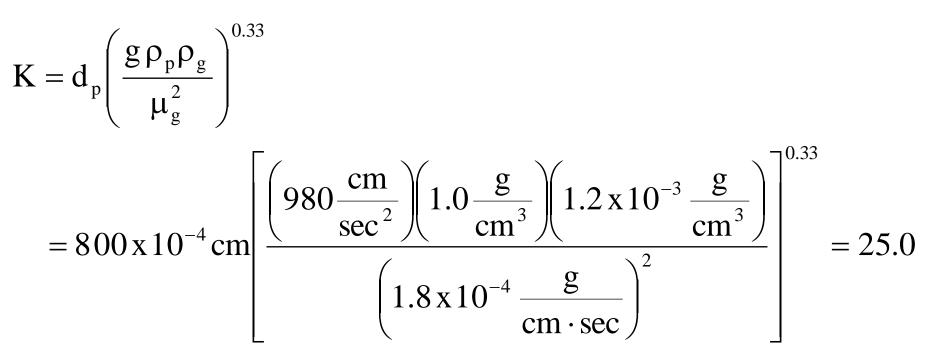


- 4. Estimate the collection efficiency of 5  $\mu$ m diameter particles with a density of 2.0 g/cm<sup>3</sup> in a countercurrent spray tower 2.5 meters high. The gas flow rate is 200 m<sup>3</sup>/min, the water flow rate is 150 l/min, the gas velocity is 100 cm/sec, and the mean droplet diameter is 800  $\mu$ m.
- Assume a temperature of 20°C and a Cunningham correction of 1.0.



Calculate the droplet terminal settling velocity:

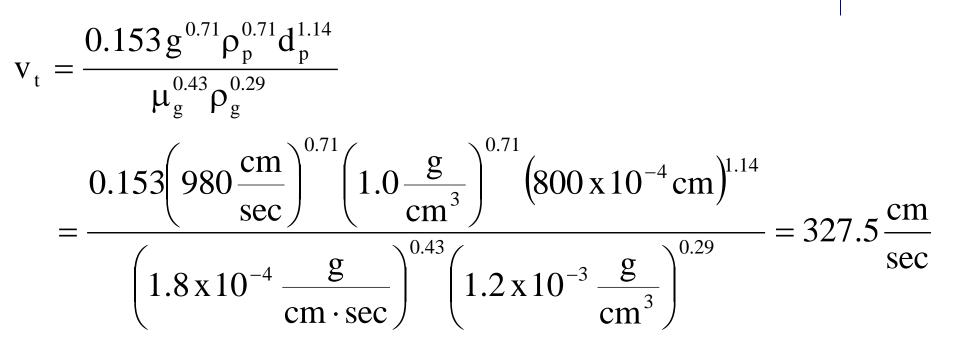
Determine the flow region:



Therefore, the flow region is transition.

And then...





And then...

Calculate the inertial impaction parameter:



$$\Psi_{I} = \frac{(1.0)(5 \times 10^{-4} \text{ cm})^{2} \left(2.0 \frac{g}{\text{ cm}^{3}}\right) \left(327.5 \frac{\text{ cm}}{\text{sec}} - 100 \frac{\text{ cm}}{\text{sec}}\right)}{18 \left(1.8 \times 10^{-4} \frac{g}{\text{ cm} \cdot \text{sec}}\right) \left(800 \times 10^{-4} \text{ cm}\right)} = 0.439$$

#### And then...

Calculate the single droplet collection efficiency:

$$\eta_{\rm I} = \left(\frac{0.439}{0.439 + 0.35}\right)^2 = 0.310$$

And then...



#### Calculate the particle collection efficiency:

$$\eta = 1 - e^{-\left[\frac{1.5\left(327.5\frac{cm}{\sec}\right)(0.310)(250\,cm)}{\left(800\,x10^{-4}\,cm\right)\left(327.5\frac{cm}{\sec}-100\frac{cm}{\sec}\right)}\right]\left[\frac{\left(150\frac{l}{\min}\right)\left(1x10-3\frac{m^3}{\min}\right)}{200\frac{m^3}{\min}}\right]}{\eta = 1 - e^{-100\frac{cm}{\sec}}}$$

$$= 0.792 = 79.2\%$$

#### **Review Problem #5**



- 5. Using the relationship of Johnstone et al, estimate the collection efficiency of a 0.5 µm diameter particle with a density of 1.5 g/cm<sup>3</sup> in a venturi scrubber having a throat gas velocity of 500 ft/sec and a liquid to gas ratio of 10.0 gal/1,000 ft<sup>3</sup>.
- Assume a temperature of  $68^{\circ}$ F and a k of 0.15 1,000 ft<sup>3</sup>/gal.





Calculate the mean droplet diameter:

$$d_{d} = \frac{16,400}{500} + 1.45(10.0)^{1.5} = 78.7\,\mu\text{m}$$

Calculate the Cunningham correction factor:

$$C_{c} = 1 + \frac{6.21 \times 10^{-4} \text{ T}}{d_{p}} = 1 + \frac{6.21 \times 10^{-4} (293 \text{ K})}{0.5 \,\mu\text{m}} = 1.36$$

And then...



Calculate the inertial impaction parameter:

$$\Psi_{\rm I} = \frac{(1.36)(0.5 \,\mathrm{x} \,10^{-4} \,\mathrm{cm})^2 \left(1.5 \,\frac{\mathrm{g}}{\mathrm{cm}^3}\right) \left(500 \,\frac{\mathrm{ft}}{\mathrm{sec}} \,\mathrm{x} \,30.48 \,\frac{\mathrm{cm}}{\mathrm{ft}}\right)}{18 \left(1.8 \,\mathrm{x} \,10^{-4} \,\frac{\mathrm{g}}{\mathrm{cm} \cdot \mathrm{sec}}\right) (78.7 \,\mathrm{x} \,10^{-4} \,\mathrm{cm})} = 3.048$$

Calculate the particle collection efficiency:

$$\eta_{i} = 1 - e^{-0.15 \frac{1,000 \, \text{ft}^{3}}{\text{gal}} \sqrt{3.048} \left( 10.0 \frac{\text{gal}}{1,000 \, \text{ft}^{3}} \right)} = 0.927 = 92.7\%$$



### **Chapter 9**

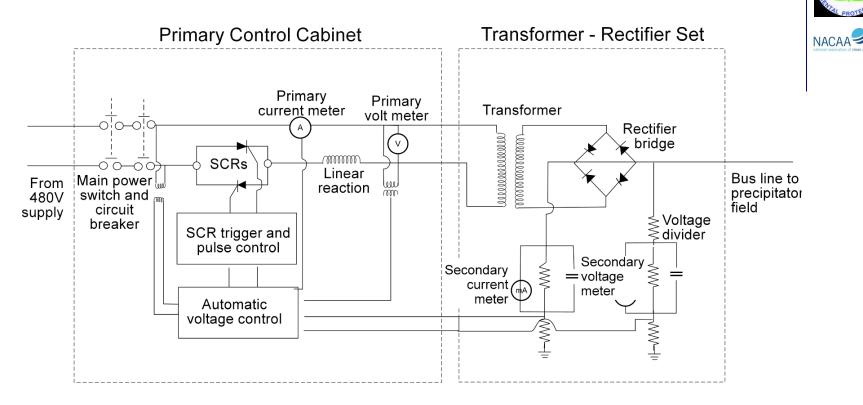


#### **Particle Collection Steps**



- Capture particulate matter on vertical plates using electrostatic attraction
- Remove collected material from the plates
- Dispose of accumulated solids

# **Precipitator Energization**

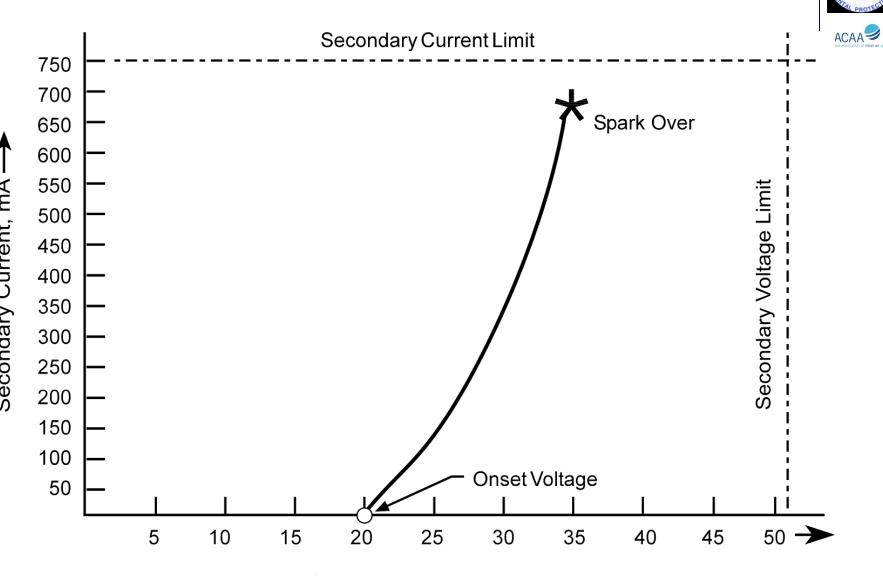


#### Basic Steps in Energizing a Precipitator Field

- Open/close 480 volt A.C. power supply to the primary control cabinet
- Control voltage and adjust voltage and current waveforms in primary line to the transformer
- Control current flow during sparking
- Increase voltage
- Convert electricity to direct current form

#### Components

- Main power switch and circuit breaker
- Automatic voltage controller, silicon controlled rectifiers (SCRs), trigger/pulse control for SCRs
- Linear reactor (located adjacent to primary control cabinet)
- Transformer
- Rectifier bridge



Secondary Voltage, kV

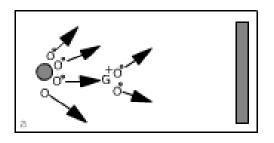
Secondary Current, mA

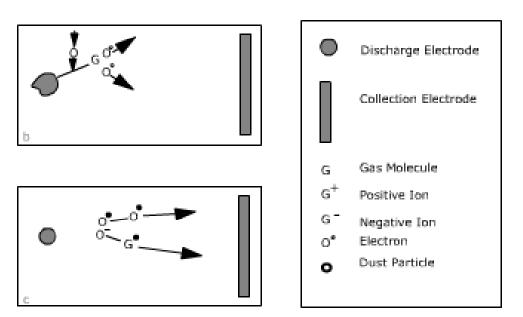
# **Voltage Limiting Factors**

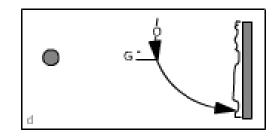


- Primary voltage limit
- Primary current limit
- Secondary voltage limit
- Secondary current limit
- Spark rate limit
- SCR conduction angle

# Particle Charging and Migration









#### **Particle Migration Velocity**



# $\omega = \frac{neEC_{c}}{3\pi\mu_{g}d_{p}}$





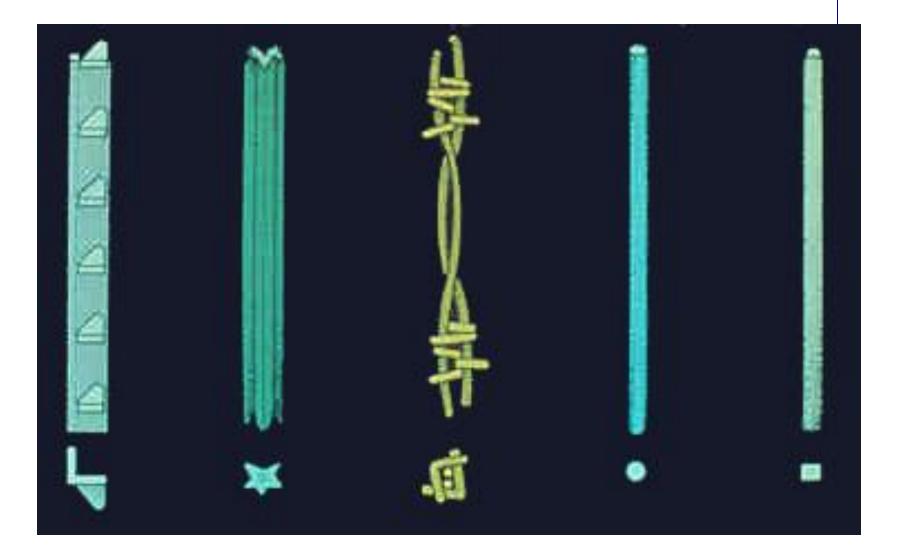
# High Voltage System





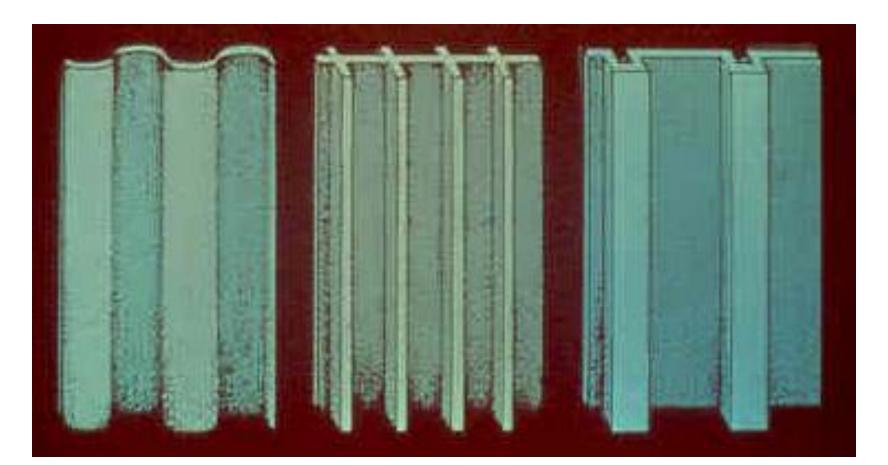
# **Discharge Electrodes**





#### **Collection Plates**







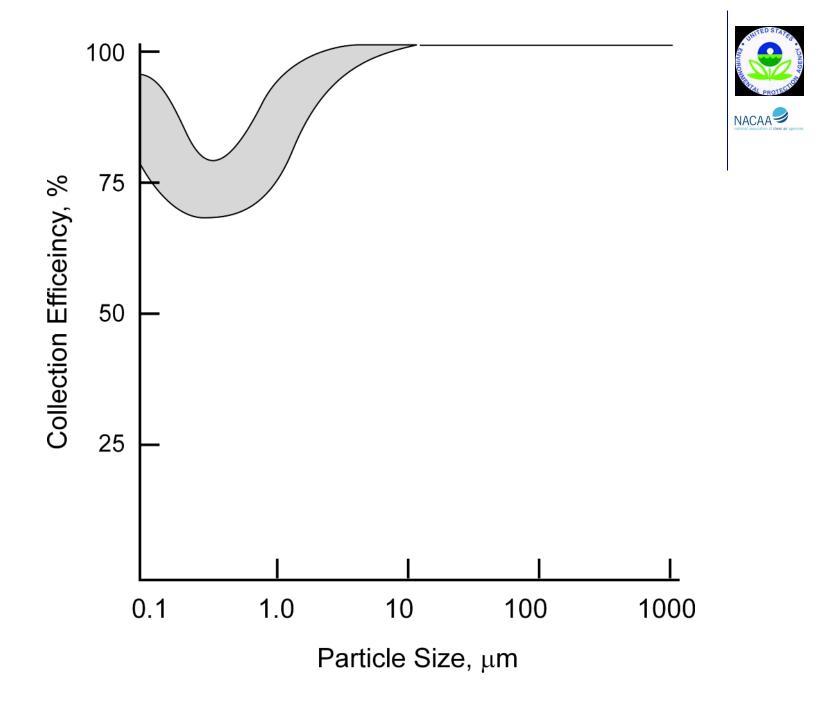




## **Collection Mechanisms**



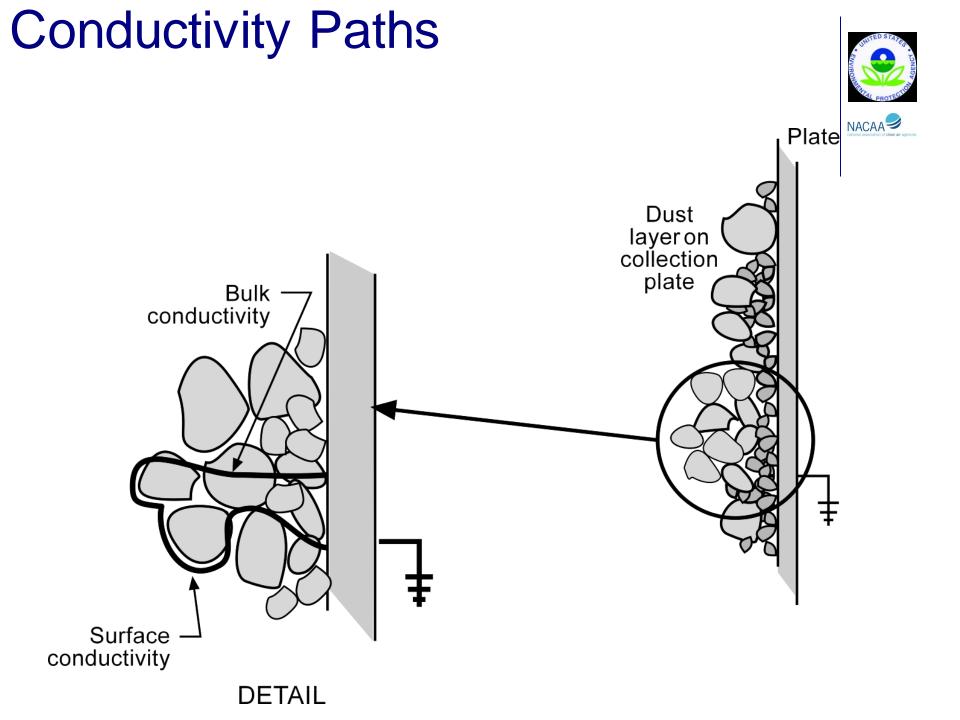
Electrostatic attraction
 Gravitational settling



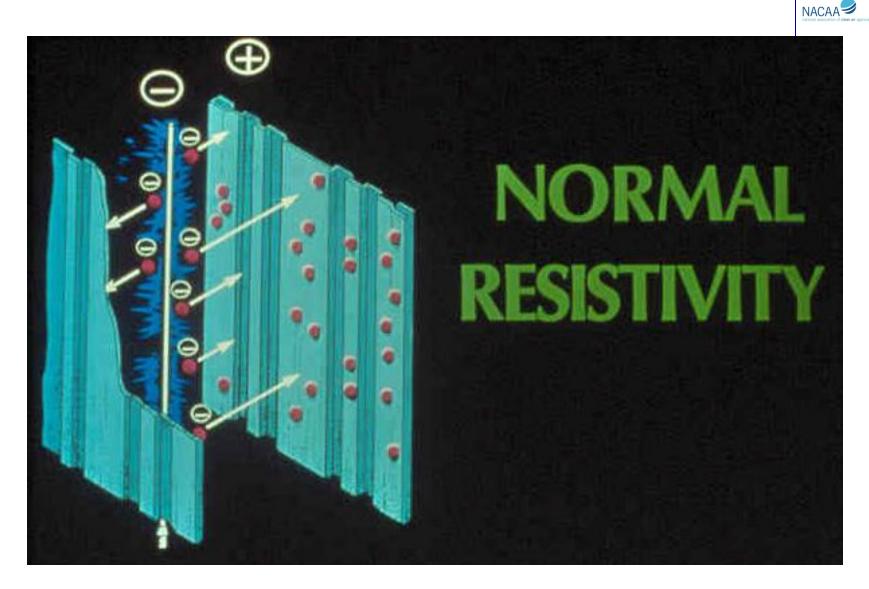




# Opposite of conductivity Controls deposition of particles onto plate



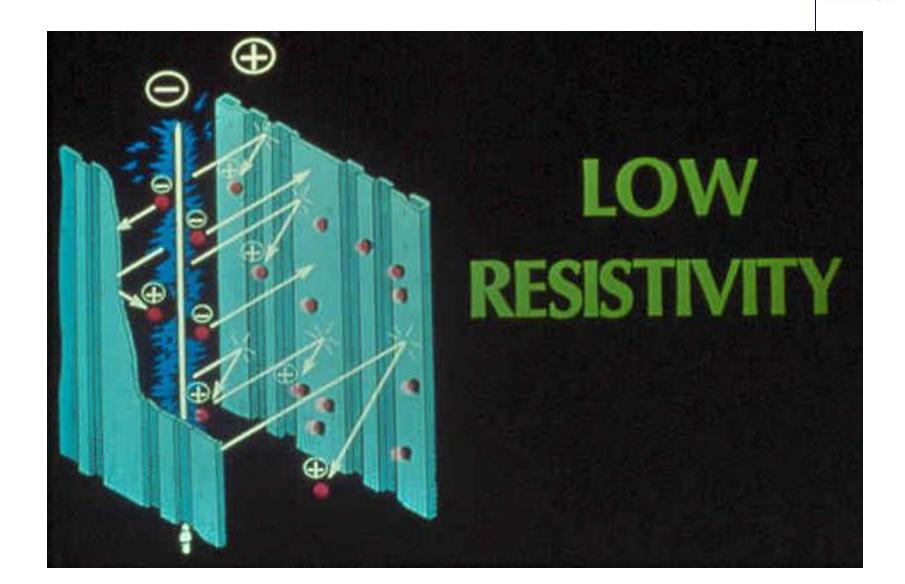




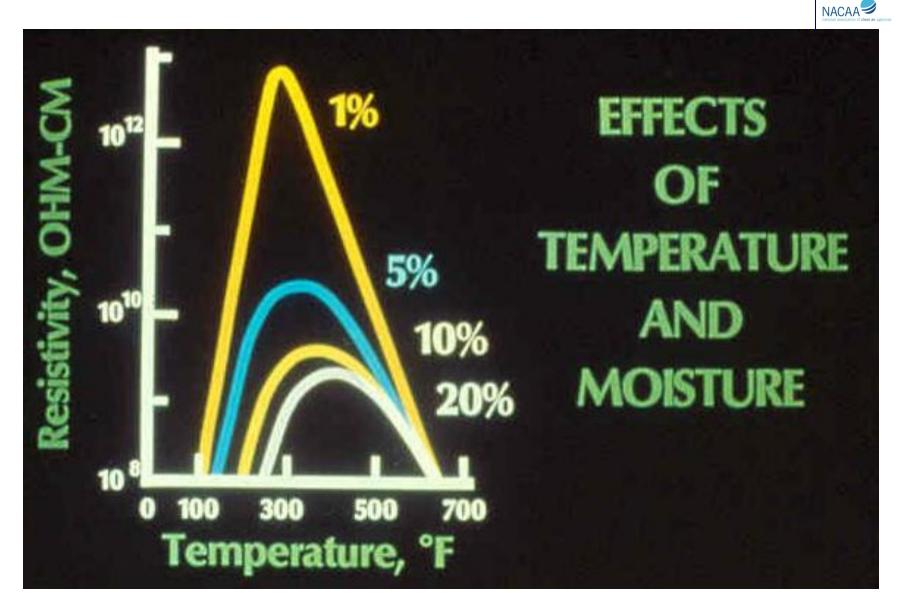




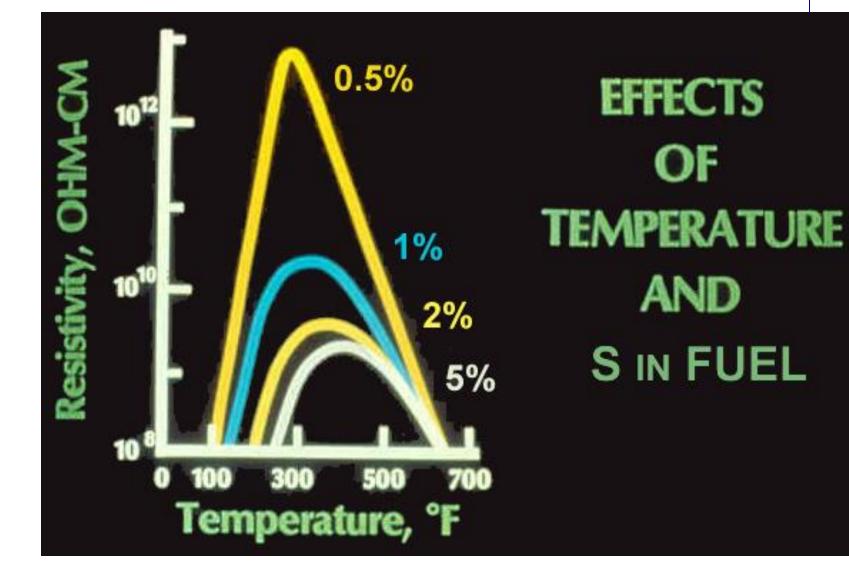












### Conditioning High Resistivity



Adjust temperature
 Condition with additional substances (e.g., H<sub>2</sub>O, SO<sub>3</sub>, NH<sub>3</sub>)

### **Common ESP Designs**



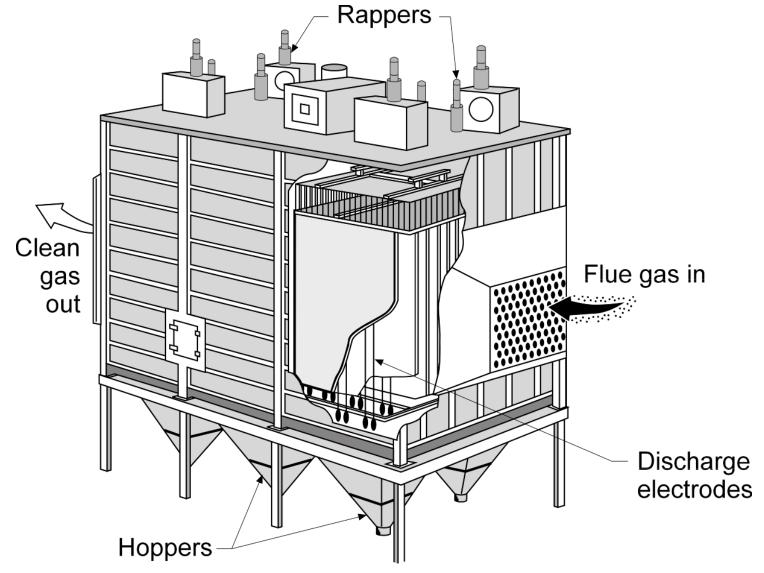
Negative corona, single stage, dry
Negative corona, single stage, wet
Positive corona, two stage, wet





### Negative corona or positive corona?

### Negative Corona, Single Stage, Dry ESP

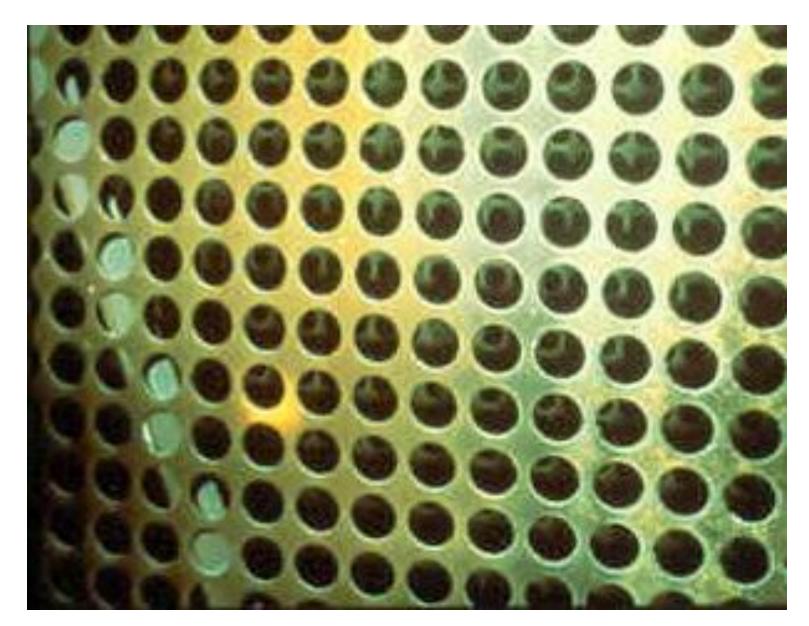




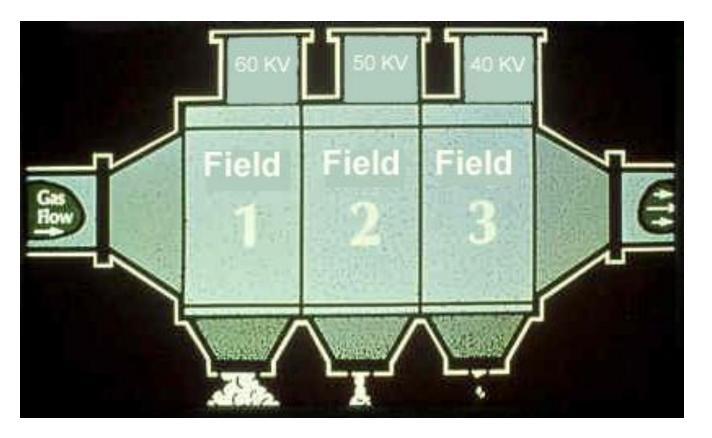
### **Gas Distributor**







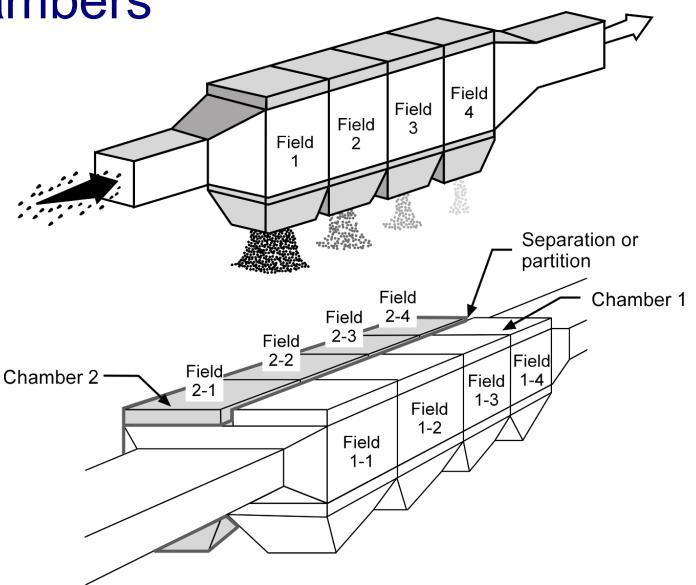
### **Field Construction**





One advantage of this system is that if you only had one field and it went down, your whole operation would have to be shut down.

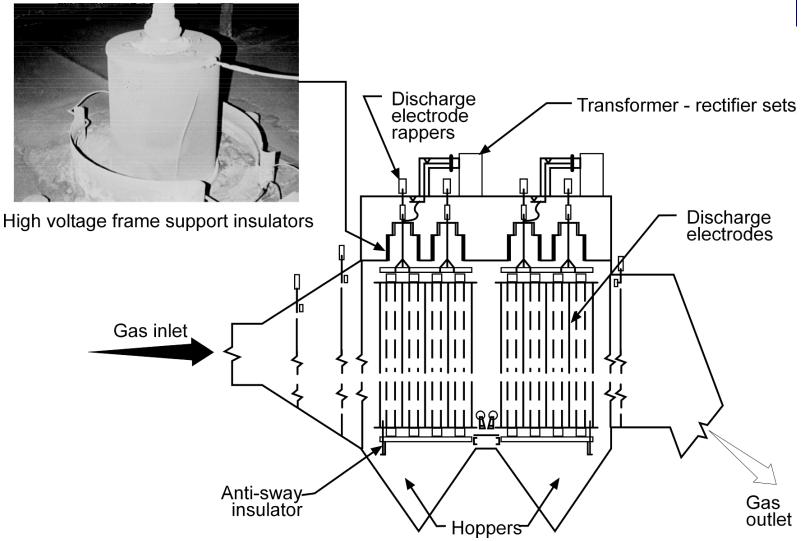
# Arrangement of Fields and Chambers



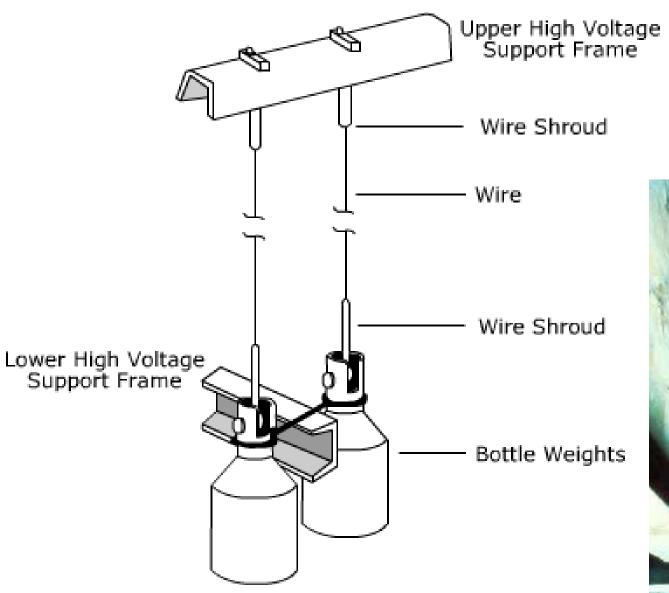


# High Voltage Frame Support Insulators





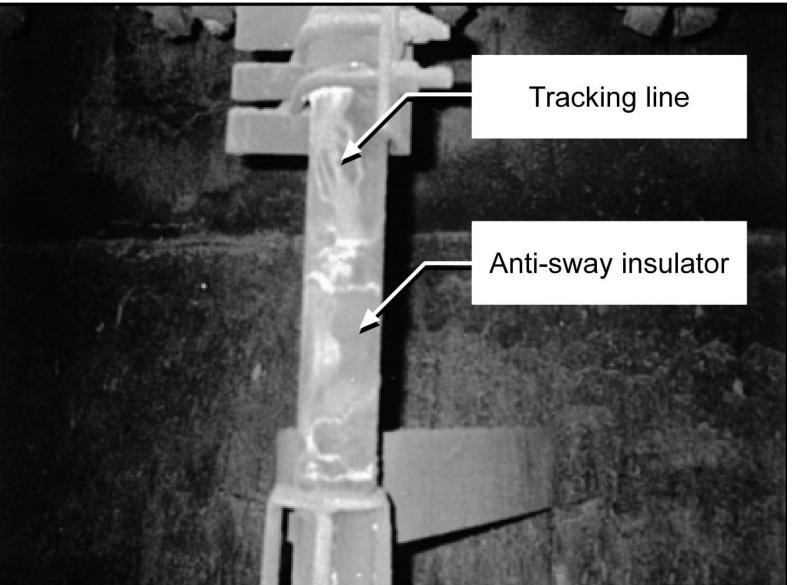
### Wire Type Discharge Electrodes

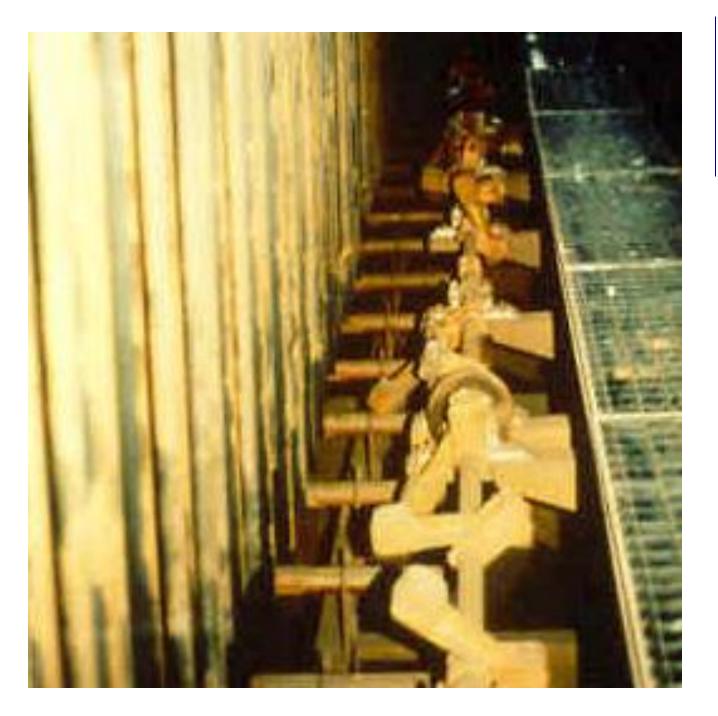














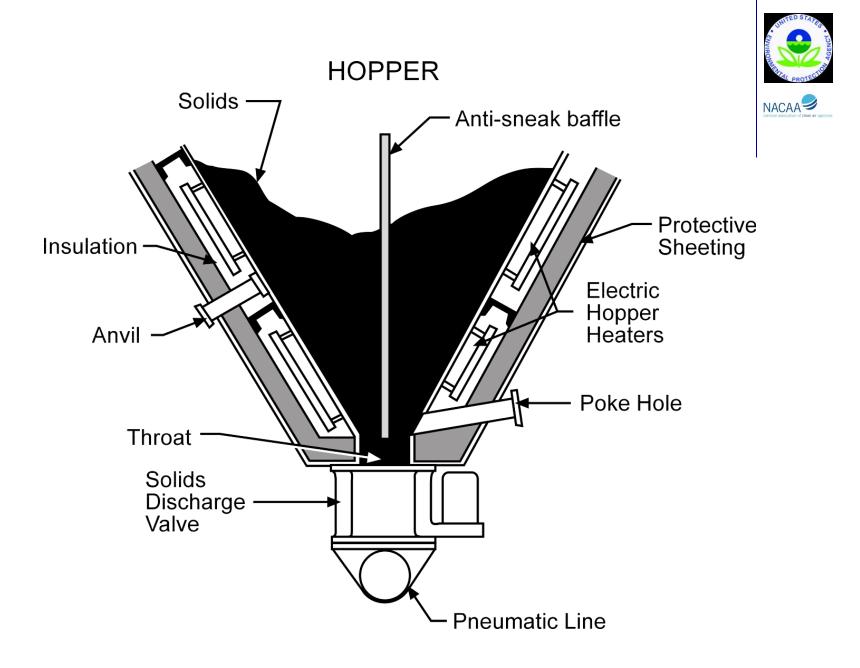


### Rappers











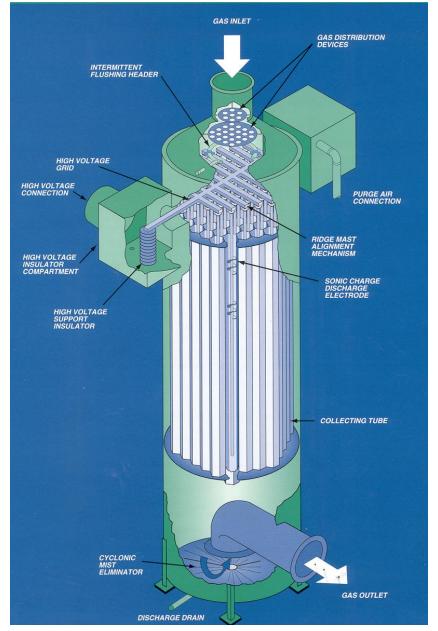


# Negative corona or positive corona?Single stage or two stage?



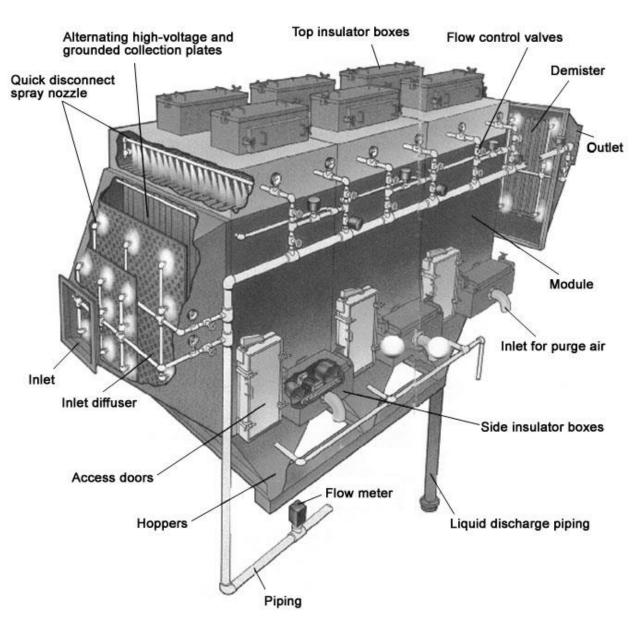
# Negative corona or positive corona? Single stage or two stage? Wet or dry?

### Vertical Flow Wet ESP





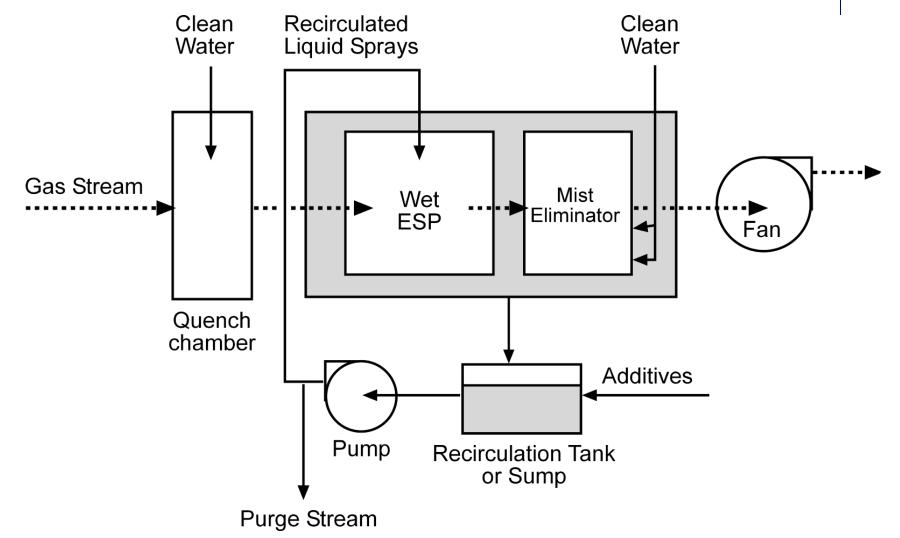
### Horizontal Flow Wet ESP



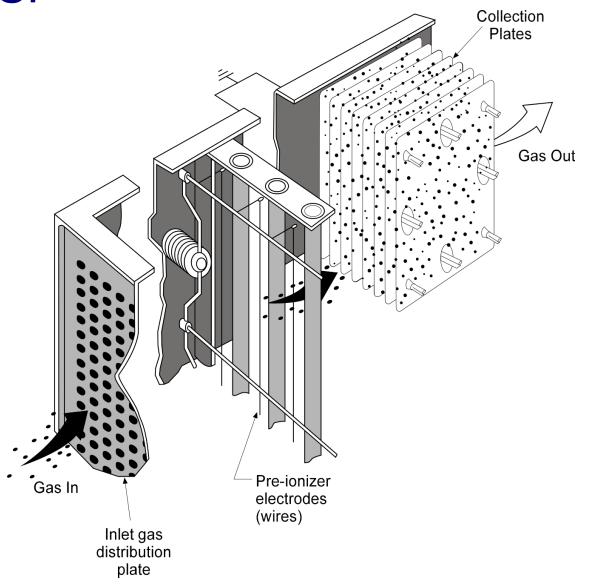


# Negative Corona, Single Stage, Wet ESP





### Positive Corona, Two Stage, Wet ESP





# **Collection Efficiency**

Deutsch-Anderson Equation



 $\eta = 1 - e^{-1}$ 

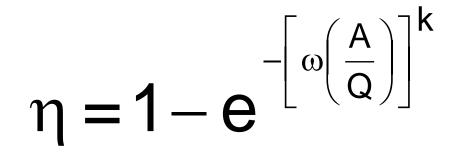
#### where

- $\eta$  = efficiency (decimal form)
- $\omega$  = migration velocity (ft/sec)
- A = total collection plate area (ft<sup>2</sup>)
- $Q = total gas flow rate (ft^3/sec)$
- e = base of natural logarithm = 2.718

### **Collection Efficiency**

Matts-Ohnfield Equation





#### where k = dimensionless constant

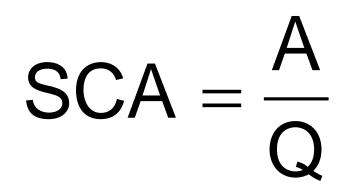
# Effective Migration Velocities for Various Industries



Application	<b>Effective Migration Velocity</b>		
	ft/sec	cm/sec	
Utility Coal-Fired Boiler	0.13 - 0.67	4.0 - 20.4	
Pulp & Paper Mill	0.21 - 0.31	6.4 - 9.5	
Sulfuric Acid Mist	0.19 - 0.25	5.8 - 7.6	
Cement (Wet Process)	0.33 - 0.37	10.1 - 11.3	
Cement (Dry Process)	0.19 - 0.23	5.8 - 7.0	
Gypsum	0.52 - 0.64	15.8 - 19.5	
<b>Open-Hearth Furnace</b>	0.16 - 0.19	4.9 - 5.8	
Blast Furnace	0.20 - 0.46	6.1 - 14.0	

### **Specific Collecting Area**

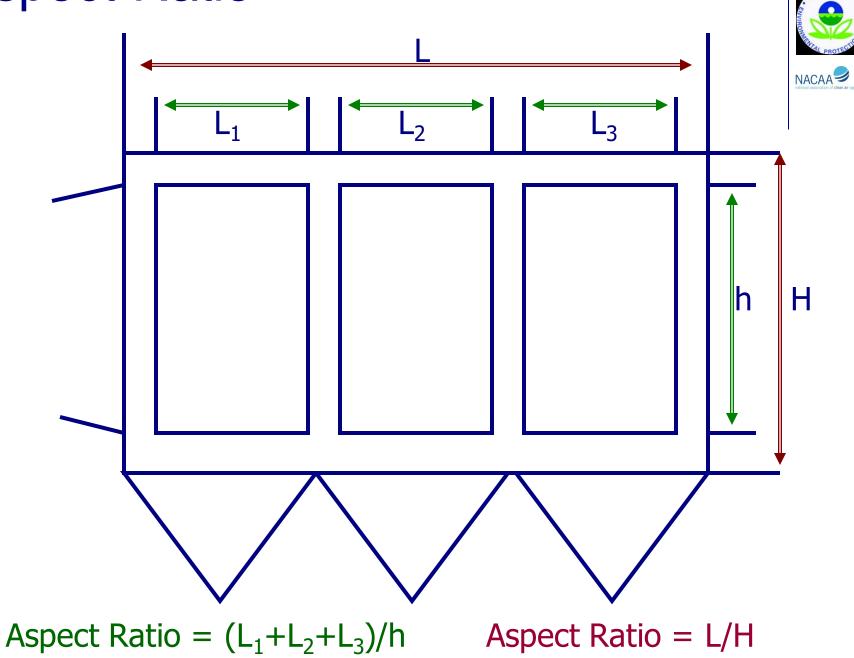




#### where

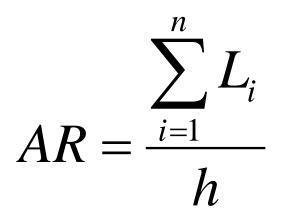
- SCA = specification collection area,  $ft^2/(1,000 \text{ ACFM})$
- A = total collection plate area,  $ft^2$
- Q = total gas flow rate,  $ft^3/min \times 0.001$

### Aspect Ratio



### Aspect Ratio





#### where:

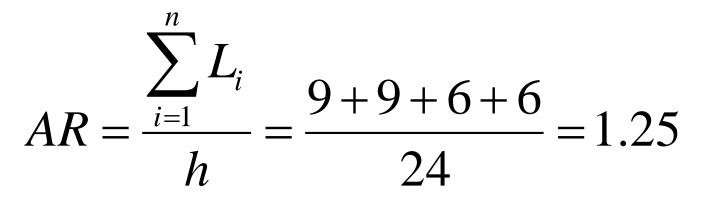
h

- AR = aspect ratio (dimensionless) L
  - = length of plates in field i (ft)
  - = collection plate height (ft)
- = number of fields in series n

### Example 9-3

An electrostatic precipitator serving a cement kiln has four fields in series. All of the fields have collection plates that are 24 feet high. The first two fields have collection plate lengths of 9 feet each. The last two fields have collection plate lengths of 6 feet.

What is the aspect ratio?



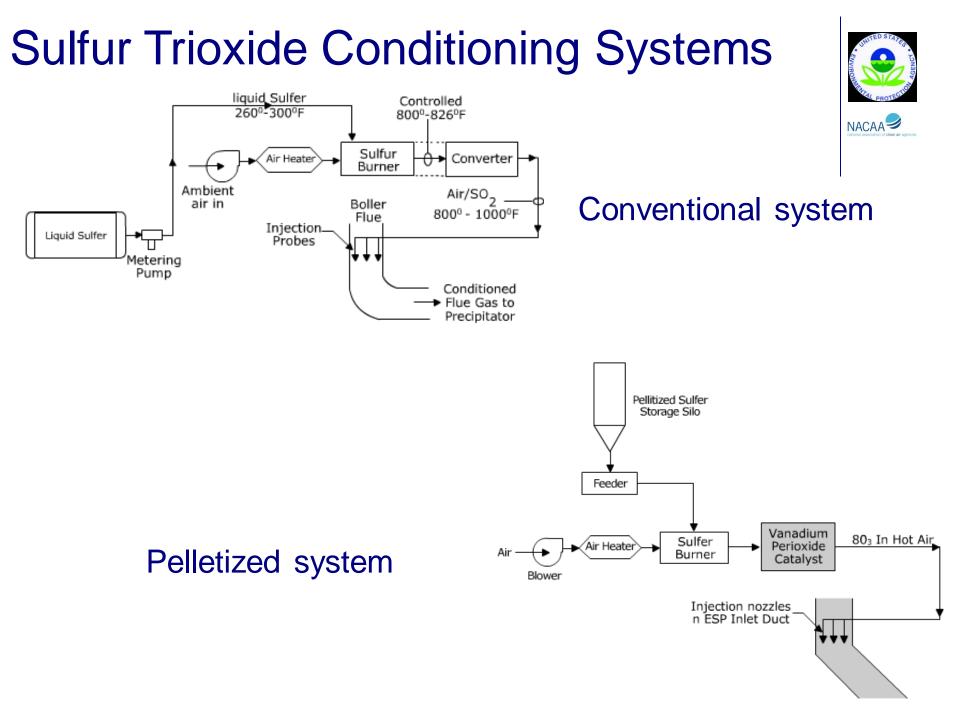


### Example 9-4

Estimate the quantities of dust in each field of a fourfield electrostatic precipitator having efficiencies of 80%, 75%, 70%, and 65% respectively. Assume a gas flow rate of 250,000 ACFM and a particulate matter loading of 2 grains per actual cubic foot.

Field	Assumed Efficiency	Particulate Entering (Ib <sub>m</sub> /hr)	Particulate Leaving, (Ib <sub>m</sub> /hr)	Particulate Collected (lb <sub>m</sub> /hr)
1 (inlet)	80	4,286	857	3,429
2 (middle)	75	857	214	643
3 (middle)	70	214	64	150
4 (outlet)	65	64	22	42





### Example 9-5

A coal-fired utility boiler generates 5 ppm of sulfuric acid. Diagnostic tests have indicated that 17 ppm of sulfuric acid are needed in the gas stream to maintain the flyash resistivity in the moderate range.

Calculate the sulfur required to operate a sulfur trioxide conditioning system for a period of one year.

Assume that the boiler has a gas flow rate of  $1.0 \times 10^{6}$  ACFM, the gas temperature is  $310^{\circ}$ F, the boiler operates 82% of the year, and the sulfur trioxide system is needed 85% of the operating time.



### **Example 9-5 Solution**



### Sulfur Trioxide System Operating Hours:

Operating hours = 8,760 total hours 
$$\left(\frac{0.82 \text{ boiler hours}}{\text{total hours}}\right) \left(\frac{0.85 \text{ FGC hours}}{\text{boiler hours}}\right)$$

= 6,106 FGC hours

Sulfur Trioxide on Demand:

SO<sup>3</sup> needed = 17 ppm – 5 ppm = 12 ppm =  $1.2 \times 10^{-5}$  lb moles SO<sup>3</sup>/lb mole flue gas

### **Example 9-5 continued**



### Sulfur Trioxide Injection Requirements:

 $SO_{3} needed = \left(1x10^{6} \frac{ft^{3}}{\min}\right) \left(\frac{528^{\circ}R}{770^{\circ}R}\right) \left(\frac{lb-mole}{385.4 \, std \, ft^{3}}\right) \left(60\frac{\min}{hr}\right) \left(1.2 \, x10^{-5} \frac{lb-mole \, SO_{3}}{lb-mole}\right)$ 

= 1.28 lb-moles/hr

### **Example 9-5 continued**



### Sulfur Required:

Sulfur lb moles =  $SO_3$  lb moles = 1.28 lb-moles/hr

# Sulfur required = $\left(1.28 \frac{lb - moles}{hr}\right) \left(6,106 \frac{hrs}{year}\right) \left(32 \frac{lb S}{lb - mole}\right) \left(\frac{ton}{2,000 lbs}\right)$

= 125 tons/year

### Instrumentation



- Electrical parameters
- Rapper parameters
- Inlet and outlet gas temperature
- Inlet and outlet oxygen concentration

### Instrumentation

Electrical parameters Primary voltage Primary current Secondary voltage Secondary current Spark rate SCR conduction angle Field limiting condition Power input



#### Advantages and Disadvantages

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Electrostatic Precipitators Advantages High Collection Efficiency Dry Collection and Disposal Small Pressure Drop Capable of Handling Large Gas Flow Rates Low Electrical Power Requirements Low Maintenance

Disadvantages High Capital Cost Particle Resistivity Limitations May Require Injection of SO3 or NH3 to Control Resistivity Relatively Large Footprint Special Precautions for Safe Operating at High Voltage

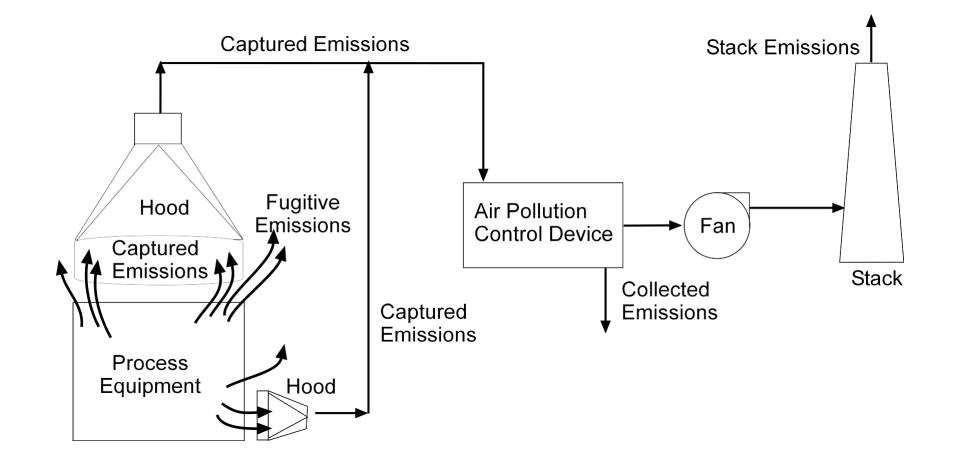
# Chapter 10





## Hoods What Hoods do





## **Fugitive Emissions**

NACAA

- Escape capture by process equipment exhaust hoods
- Are emitted during material transfer
- Are emitted to the atmosphere from the source area
- Are emitted directly from process equipment

Fugitive emissions = Total emissions – Emissions captured by hood Stack emissions = Emissions captured by hood  $x\left(\frac{100 - \eta}{100}\right)$ 

## Example 10-1

Calculate the fugitive emissions and the stack emissions if the process equipment generates  $100 \text{ lb}_m/\text{hr}$  of particulate matter, the hood capture efficiency is 95%, and the collection efficiency of the air pollution control device is 95%.

#### Solution

#### calculate the fugitive emissions:

Fugitive emissions = Total emissions - Emissions captured by hood

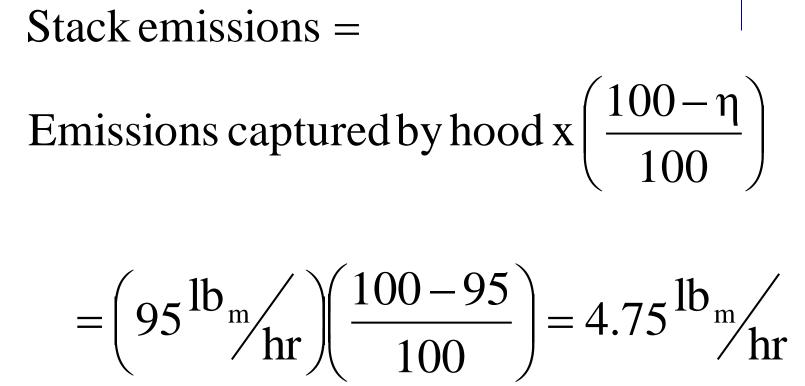
$$100^{lb_{m}}/hr - 95^{lb_{m}}/hr = 5^{lb_{m}}/hr$$

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And then...

#### Calculate the stack emissions:





## Example 10-2

Calculate the fugitive emissions and the stack emissions if the process equipment generates  $100 \text{ lb}_m/\text{hr}$  of particulate matter, the hood capture efficiency is 90%, and the collection efficiency of the air pollution control device is 95%.

#### Solution

#### calculate the fugitive emissions:

Fugitive emissions = Total emissions - Emissions captured by hood

$$100^{lb} \text{m/hr} - 90^{lb} \text{m/hr} = 10^{lb} \text{m/hr}$$



#### Calculate the stack emissions:



#### Stack emissions =

Emissions captured by hood x  $\left(\frac{100 - \eta}{100}\right)$ 

$$= \left(90^{lb} \text{m/hr}\right) \left(\frac{100 - 95}{100}\right) = 4.5^{lb} \text{m/hr}$$

Slight changes in the ability of the hood to capture the pollutants can have a large impact on the total fugitive and stack emissions released into the atmosphere.

## Can't Always see them...



If there are many small fugitive sites

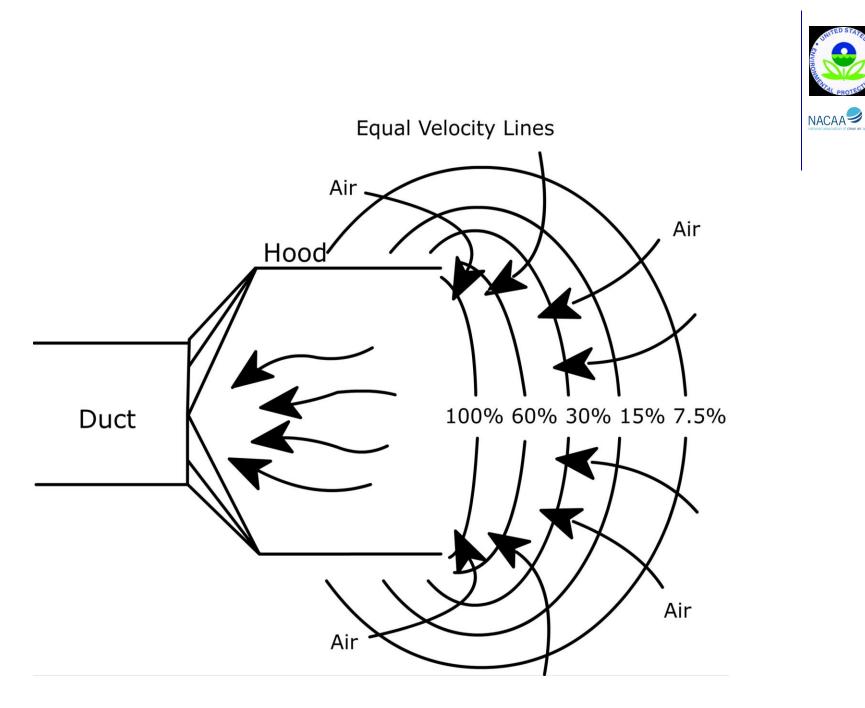
- If there is one major site that cannot be seen
- If the matter is not in the size range that causes light scattering

## **Hood Operating Principles**



Operate under negative pressure
 Hood must be close to emission source.

Capture Velocity: the air velocity at any point in front of the hood that will overcome opposing air currents and capture contaminated air.



# **Capture Velocities Considerations**

- •The surrounding air currents Minimal room air currents vs. disturbing room air currents
- •The level of toxicity of the pollutant to be captured
  - Nuisance value only vs. high toxicity
- •The amount of pollutant Intermittent (low production) vs. high production (heavy use)
- •Area of the hood opening
  - Large hood (large air mass in motion) vs. small hood (local control only)



## **Capture Velocities**



Type of Material Release	Capture Velocity (ft/min)
With no velocity into quiet air	50-100
At low velocity into moderately still air	100-200
Active generation into zone of rapid air motion	200-500
With high velocity into zone of very rapid air motion	500-2,000

## Example 10-3



The recommended capture velocity for a certain pollutant entering a 16-inch diameter hood is 300 ft/min.

- What is the required volumetric flow rate for the following distances from the hood face (X)?
- A. X = 12 in. (75% of hood diameter) B. X = 24 in. (150% of hood diameter)

$$Q = v_h (10X^2 + A_h)$$

## Example 10-3



The recommended capture velocity for a certain pollutant entering a 16-inch diameter hood is 300 ft/min.

- What is the required volumetric flow rate for the following distances from the hood face (X)?
- A. X = 12 in. (75% of hood diameter) B. X = 24 in. (150% of hood diameter)

$$Q = v_h (10X^2 + A_h)$$

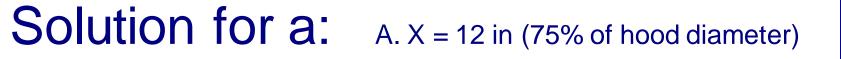
## **Solution for a:** A. X = 12 in (75% of hood diameter)



#### Calculate the area of the hood opening:

$$A_{h} = \frac{\pi D^{2}}{4} = \frac{\pi \left[16in\left(\frac{1ft}{12in}\right)\right]^{2}}{4} = 1.40ft^{2}$$

Calculate the volumetric flow rate, Q, required obtaining the recommended capture velocity of 300 fpm at a distance of 12 inches from the hood:



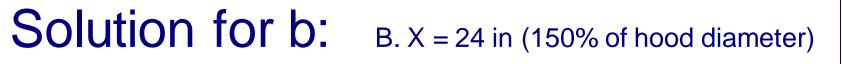


$$A_h = 1.40 \text{ ft}^2 \text{ and } X = 12 \text{ inches}$$

$$\mathbf{Q} = \mathbf{v}_{\mathrm{h}} (10\mathbf{X}^2 + \mathbf{A}_{\mathrm{h}})$$

$$= 300 \text{ ft} / \min \left[ 10(1 \text{ ft})^2 + 1.40 \text{ ft}^2 \right] = 3,420 \text{ ft}^3 / \min$$

The required volumetric flow rate for 300fpm at a distance of 12 inches is 3,420 ft<sup>3</sup>/min





The hood opening remains the same:

$$A_{h} = \frac{\pi D^{2}}{4} = \frac{\pi \left[16in\left(\frac{1ft}{12in}\right)\right]^{2}}{4} = 1.40ft^{2}$$

Calculate the volumetric flow rate, Q, required obtaining the recommended capture velocity of 300 fpm at a distance of 24 inches from the hood: Solution for B: B. X = 24 in (150% of hood diameter)



$$A_h = 1.40 \text{ ft}^2$$
 and  $X = 24 \text{ inches}$ 

$$\mathbf{Q} = \mathbf{v}_{\mathrm{h}} (10\mathbf{X}^2 + \mathbf{A}_{\mathrm{h}})$$

$$= 300 \, \text{ft} / \min \left[ 10(2 \, \text{ft})^2 + 1.40 \, \text{ft}^2 \right] = 3.420 \, \text{ft}^3 / \min$$

The volumetric flow rate requirements increased approximately 4 times when the X was doubled Hood Designs for Improved Performance



Considerations for hot gas streams
Use of Flanges
Use of Side Baffles
Other Designs

### Added Side Baffles





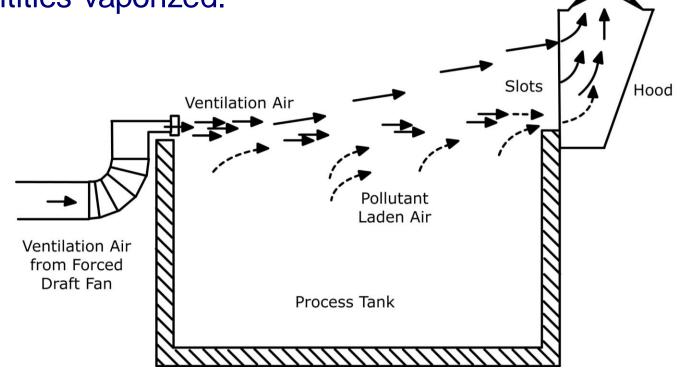




+ good for use in open tanks and where access from the top is necessary.

- Where cross drafts could increase quantities vaporized.

To Pollution Control Device and Induced Draft Fan



# Monitoring Hood Capture Effectiveness



# $SP_h = VP_d + h_e$

#### where $SP_h = hood static pressure$ $VP_d = velocity pressure in duct$ $h_e = hood entry loss$ $h_e = F_h VP_d$ $F_h = hood entry loss coefficient (dimensionless)$

# Duct shape affects airflow Plain duct end Vena contracta: where $h_{e} = 0.93$ air converges when it enters a duct Bell-mouth duct end Flanged duct end $h_{e} = 0.04$ $h_{e} = 0.49$

After the vena contract the airflow expands to fill the duct





 $VP_{d} = \rho_{g} \left( \frac{V_{d}}{1,096.7} \right)$ 

#### where $VP_d$ = duct velocity pressure (in WC) $v_d$ = duct gas velocity (ft/min) $\rho_g$ = gas density (lbm/ft<sup>3</sup>)

- As gas flow rate increases the static pressure increases
- A decrease in static pressure indicates the gas flow rate has decreased from previous levels.

## Example 10-4

A hood serving a paint dipping operation has a hood static pressure of 1.10 in WC. The baseline hood static pressure was 1.70 in WC.



- A. At present operating conditions
- B. At baseline levels

Use the data provided below: •F<sub>h</sub> = 0.93 •Temperature = 68°F •Duct diameter 2 ft (inside diameter)



Calculate the velocity pressure in the duct:



 $SP_{h} = (1+F_{h})VP_{d}$  $VP_{d} = \frac{SP_{h}}{1+F_{h}} = \frac{1.10 \text{ in WC}}{1+0.93} = 0.57 \text{ in WC}$  $F_{h} = 0.93$ 

Temperature = 68°F Duct diameter 2 ft (inside diameter)

#### Calculate the gas velocity in the duct:

$$VP_{d} = \rho_{g} \left(\frac{V_{d}}{1,096.7}\right)^{2}$$
  
$$v_{d} = 1,096.7 \sqrt{\frac{VP_{d}}{\rho_{g}}} = 1,096.7 \sqrt{\frac{0.57 \text{ in WC}}{0.0747 \text{ lb}_{m}/\text{ft}^{3}}} = 3,029.5 \text{ ft/min}$$

 $F_h = 0.93$ Temperature = 68°F Duct diameter 2 ft (inside diameter)



#### Calculate the gas flow rate:



$$Q = v_{d}A_{d} = v_{d}\left(\frac{\pi D^{2}}{4}\right)$$
$$= 3,029.5 \text{ ft/min}\left[\frac{\pi (2\text{ ft})^{2}}{4}\right] = 9,515.5 \text{ ft}^{3}/\text{min}$$
$$F_{h} = 0.93$$
Temperature = 68°F  
Duct diameter 2 ft (inside diameter)

The gas flow rate at present operating conditions is 9,515.5 ft<sup>3</sup>/min

## Example 10-4

A hood serving a paint dipping operation has a hood static pressure of 1.10 in WC. The baseline hood static pressure was 1.70 in WC.



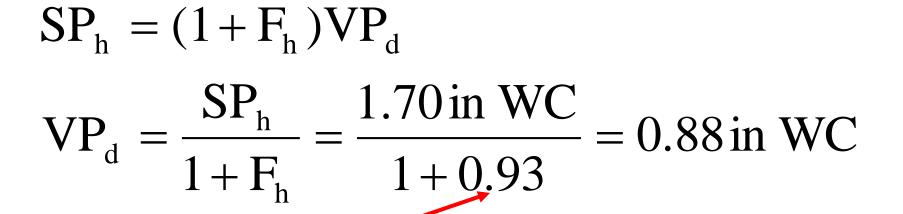
- A. At present operating conditions
- B. At baseline levels

Use the data provided below: •F<sub>h</sub> = 0.93 •Temperature = 68°F •Duct diameter 2 ft (inside diameter)



Example 10-4 solution (part b)

Calculate the velocity pressure in the duct:



 $F_h = 0.93$ Temperature = 68°F Duct diameter 2 ft (inside diameter)



Example 10-4 solution

#### Calculate the gas velocity in the duct:

$$VP_{d} = p_{g} \left(\frac{v_{d}}{1,096.7}\right)^{2}$$
  
$$v_{d} = 1,096.7 \sqrt{\frac{VP_{d}}{p_{g}}} = 1,096.7 \sqrt{\frac{0.88 \text{ in WC}}{0.0747 \text{ lb}_{m}/\text{ft}^{3}}} = 3,764.2 \text{ ft/min}$$

 $F_h = 0.93$ Temperature = 68°F Duct diameter 2 ft (inside diameter)



#### Calculate the gas flow rate:



$$Q = v_{d}A_{d} = v_{d}\left(\frac{\pi D^{2}}{4}\right) = 3,764.2 \text{ ft/min}\left[\frac{\pi (2\text{ft})^{2}}{4}\right] = 11,819.9 \text{ ft}^{3}/\text{min}$$

$$F_{h} = 0.93$$
Temperature = 68°F
Duct diameter 2 ft (inside diameter)

The decrease in WC from 1.7 in to 1.1 indicates a drop in the gas flow rate from 11,820 to 9.518 acfm. That's a 20% decrease.

## **Transport Velocities**



Contaminant Vapors, gasses, smoke **Fumes** Very fine, light dust Dry dust and powders Average industrial dust Heavy dusts Heavy or moist

Transport Velocity (ft/min) Any (usually 1000-2000) 1400-2000 2000-2500 2500-3500 3500-4000 4000-4500 4500 and up

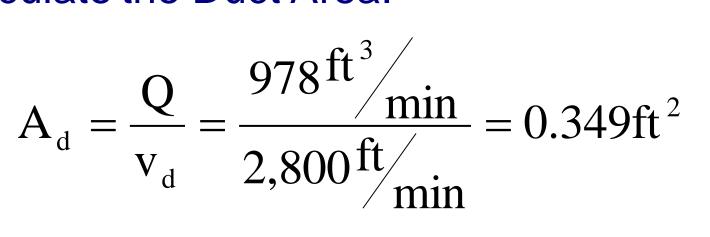
## **Calculating Duct Diameter**



- A duct system transporting a dry dust requires a minimum transport velocity of 2,800 ft/min. The volumetric flow rate for the system is 978 acfm.
- What is the necessary duct diameter in inches for this section of ductwork to maintain the minimum transport velocity?







Calculate the Duct Diameter:  $A_{d} = \frac{\pi D^{2}}{4}$  $D = \sqrt{\frac{4A_{d}}{\pi}} = \sqrt{\frac{4(0.349 \text{ft}^{2})}{\pi}} = 0.667 \text{ft} = 8 \text{in}$ 



#### Fans



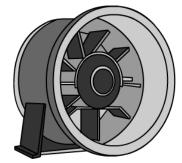


# Types of Fans



Figure 10-9. Axial fan

Axial
Centrifugal
Special



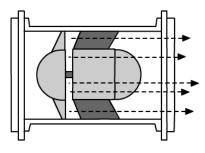
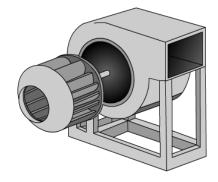


Figure 10-10. Centrifugal fan



# **Fan Components**



Diameter

#### Direct Drive Figure 10-11. Centrifual fan motor sheaves Belt Drive Belts Variable Drive Motor Fan Sheave

Sheave

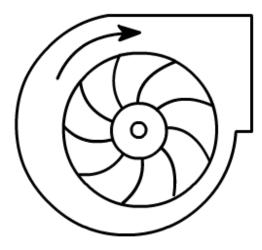
Diameter

# **Centrifugal Fan Wheels**



Forward curved
Radial
Backward curved
Standard blade
Airfoil blade





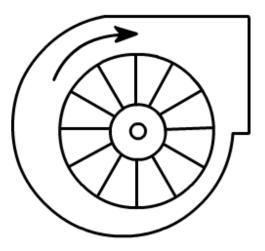
A. Forward curved

#### Has 24-64 shallow blades

Efficiency less than backward inclined

Operates at lowest speed





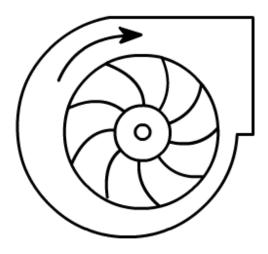
C. Radial

#### Has 6-10 blades

Efficiency less than backward inclined

Operates at low speed





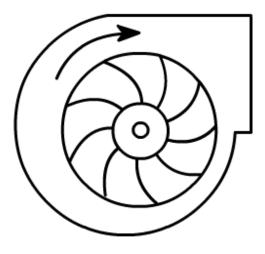
**B. Backward curved** 

#### Has 9-16 blades

Efficiency only slightly less than airfoil

Operates at high speed





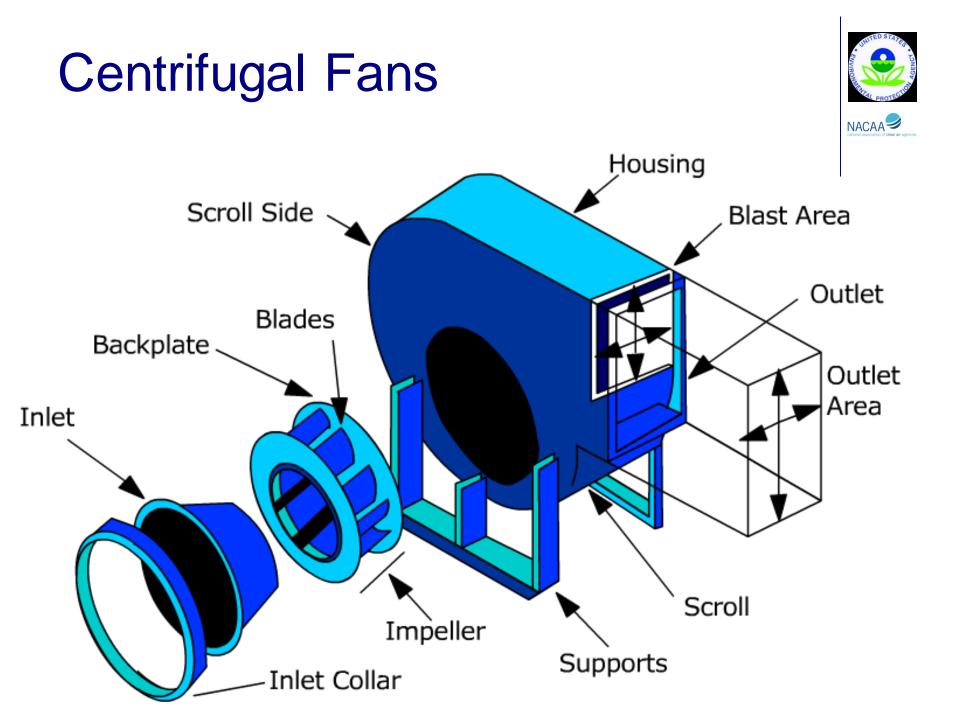
**B. Backward curved** 

#### Backward Curved – but with Airfoil blade

Has 9-16 blades

Most efficiency

Operates at highest speed





Fan Law #1:

the relationship of speed to gas flow rate

$$\mathbf{Q}_2 = \mathbf{Q}_1 \left( \frac{\mathbf{RPM}_2}{\mathbf{RPM}_1} \right)$$

Where

 $Q_1$ 

 $Q_2$ 

- =baseline gas flow rate (acfm)
  - = present gas flow rate (acfm)
- RPM<sub>1</sub> = baseline fan wheel rotational speed (revolutions per minute)
- RPM<sub>2</sub> = present fan wheel rotational speed (revolutions per minute)



Fan Laws:

Static pressure at the outlet is always higher than the SP at the inlet

Fan SP =  $Sp_{out} - Sp_{in} - VP_{in}$ 



#### Fan Law #2:

# Fan SP is related to the square of the fan speed

$$\operatorname{Fan} \operatorname{SP}_{2} = \operatorname{Fan} \operatorname{SP}_{1} \left( \frac{\operatorname{RPM}_{2}}{\operatorname{RPM}_{1}} \right)^{2}$$

#### Where

Fan  $SP_1$  = baseline fan static pressure (in WC) Fan  $SP_2$  = present fan static pressure (in WC) RPM<sub>1</sub> = baseline fan wheel rotational speed (revolutions per minute) RPM<sub>2</sub> = present fan wheel rotational speed (revolutions per minute)



Fan Law #3:

The brake horsepower is also related to the cube of the fan speed

$$BHP_2 = BHP_1 \left(\frac{RPM_2}{RPM_1}\right)^3$$

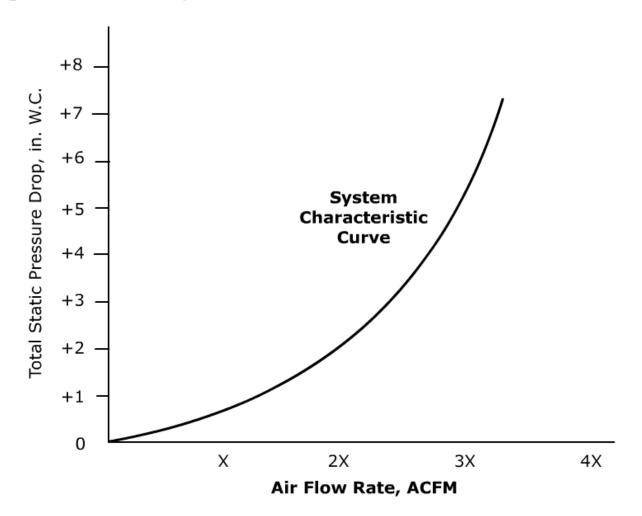
#### Where

- $BHP_1$  = baseline brake horsepower
- BHP<sub>2</sub> = present brake horsepower
- RPM<sub>1</sub> = baseline fan wheel rotational speed (revolutions per minute)
- RPM<sub>2</sub> = present fan wheel rotational speed (revolutions per minute)

#### System Characteristic Curve



Figure 10-14. System characteristic curve



#### Multi-Rating Table (sample)

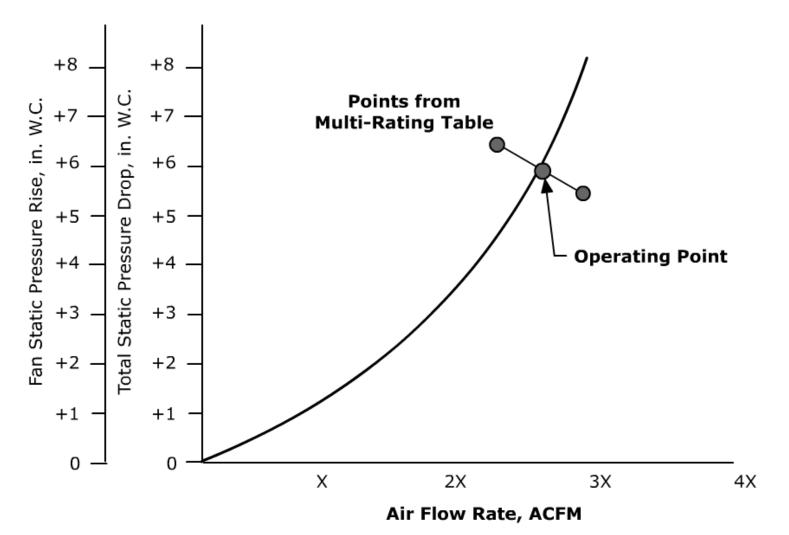


194 LS												heel diameter: 19¼" heel circumference: 5.01 fi								
		2'5		4"SP		6"SP		8*SP		10*SP		12"SP		14'SP		16*SP		18"SP		Τ
CFM	ov	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	RPM	BHP	R								
660 792 924 1056	1000 1200 1400 1600	995 1008 1023 1042	0.48 0.55 0.62 0.71	1392 1398 1405 1418	1.01 1.11 1.23 1.35	1698 1703 1708 1716	1.60 1.75 1.90 2.07	1960 1962 1965 1971	2.27 2.45 2.64 2.84	2191 2192 2194 2197	2.98 3.20 3.43 3.67	2399 2398 2401 2401	3.74 3.99 4.27 4.53	2592 2588 2589 2593	4.55 4.83 5.14 5.46	2769 2767 2766 2769	5.38 5.71 6.05 6.42	2938 2936 2932 2935	6.27 6.65 7.01 7.41	31.
1 188 1 320 1 452 1 584	1800 2000 2200 2400	1061 1084 1109 1136	0.80 0.90 1.01 1.13	1431 1447 1465 1485	1.49 1.64 1.80 1.98	1725 1739 1753 1759	274 2.441 2.65 2.87	1980 1967 1999 2012	3.96 3.29 3.541 3.80	2203 2209 7771 2229	3.92 4.19 4.49 4.78	2407 2414 2422 2431	4.83 5.15 5.47 5.82	2593 2600 2607 2612	5.78 6.13 6.50 6.87	2771 2773 2778 2785	6.79 7.16 7.55 7.98	2936 2940 2943 2949	ĩ	
1716 1980 2244 2508	2600 3000 3400 3800	1357 1223 1230 1361	1.91 1.91 2.33	1505 1554 1606 1661	7.16 2.58 3.04 3.56	1784 1824 1857 1917	110 3.62 4.19 4.84	2075 2059 2098 2141	4.03 4.70 5.38 6.12	7742 2272 2305 2345	5.11 5.82 6.59 7.44	2441 2464 2495 2531	6.18 6.95 7.83 8.78	2623 2644 2671 2703	7.71 8.14 9.09 10.1	279) 2815 2838 2866	9.340 9.34 10.4 11.5	2056 2011 2015 2015 31	S. In	
2772 3036 3300 3564 3828	4200 4600 5000 5400 5800	1439 1519 1603 1691 1781	2.83 3.40 4.07 4.84 5.73	1723 1788 1855 1929 2005	4.16 4.84 5.58 6.45 7.41	1968 2025 2066 2148 2214	5.54 6.32 7.20 8.14 9.18	2189 2239 2294 2350 2409	6.95 7.85 8.83 9.88 11.0	2387 2432 2483 2536 2591	8.37 9.36 10.5 11.6 12.9	2569 2611 2650 2708 2759	9.80 10.9 12.1 13.4 14.8	2740 2780 2825 2859 2917	11.3 12.5 13.8 15.2 16.7	2900 2937 2978 3024 3069	12.8 14.1 15.5 17.0 18'	:		

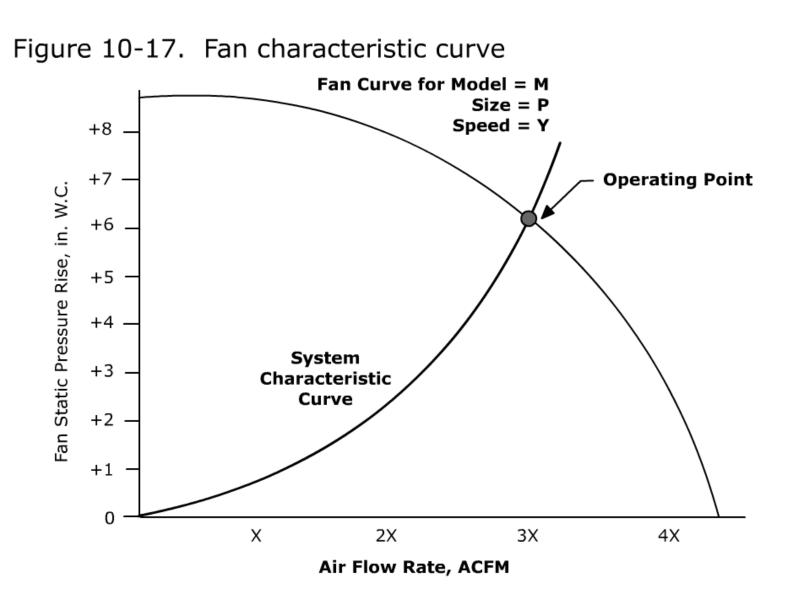
## **Operating Point**



Figure 10-16. Operating Point



#### Fan Curve

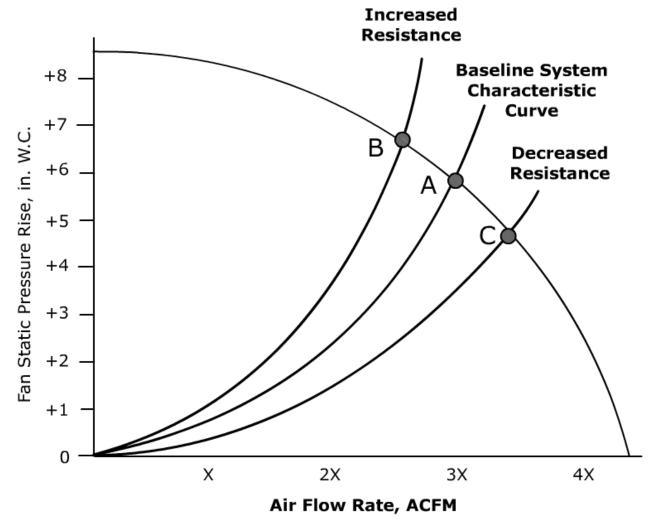


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## Changes in the System Resistance Curve

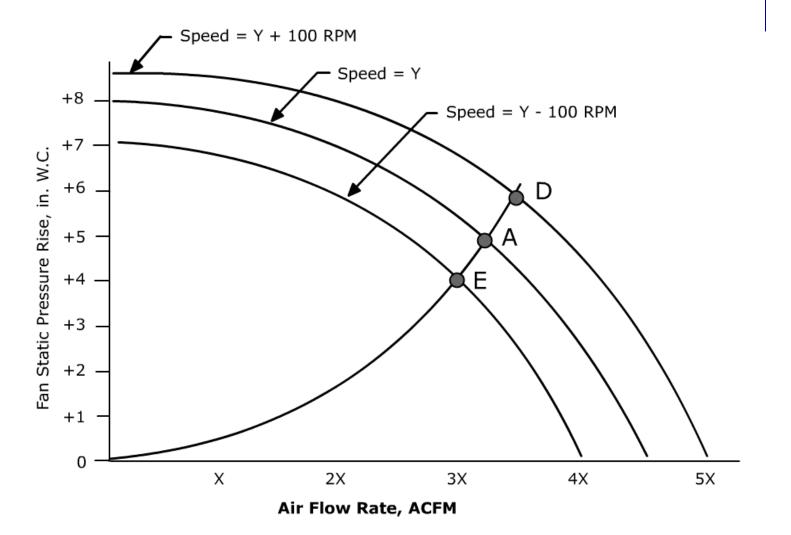


Figure 10-18. Changes in the system resistance curve



#### Changes in the Fan Speed

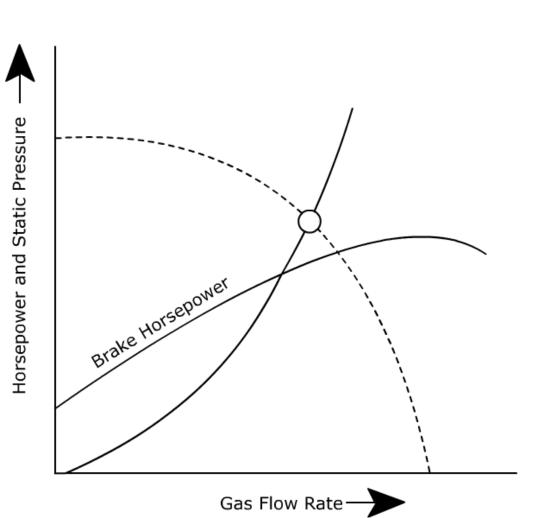
#### Figure 10-19. Changes in fan speed





#### Brake Horsepower Curve

Figure 10-20. Brake horsepower curve



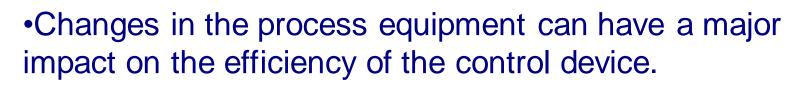
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Baseline System Characteristic

Evaluating the Entire Industrial Process

Why evaluate the whole process?

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•Changes in the air pollution control device can affect the ability of the process hoods to capture the pollutants at the point of generation.

•The operating data from one unit in the system can be valuable in evaluating the operating conditions in another unit in the system.

•Hoods and fans can influence the efficiency of the air pollution control equipment and the release of fugitive emissions from the process equipment.



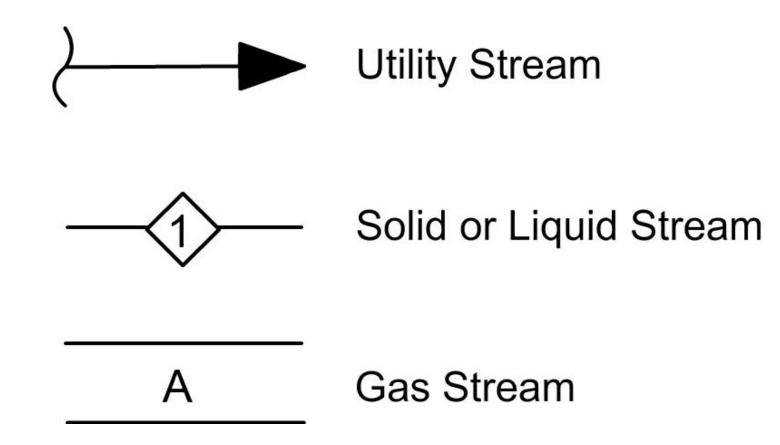


#### How are Flowcharts Useful?

- •Evaluating process operating changes that are affecting control device performance
- Identifying instruments that are not working properly
- Identifying health and safety problems
- Communicating effectively







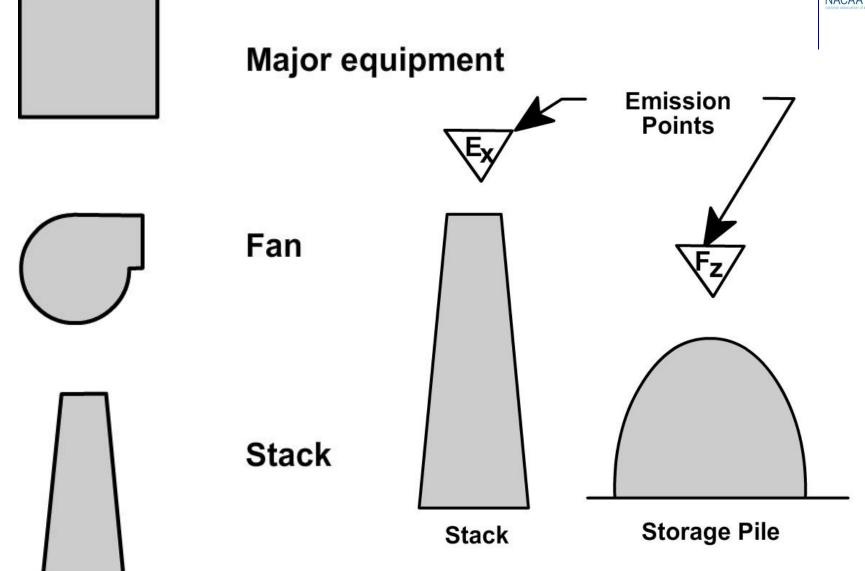
#### **Codes for Utility Streams**



			1
Cal	-compressed calibration gas	HS	-high pressure stream
CA	-compressed air	IA	-instrument air
CD	-condensate	LS	-low pressure steam
CW	-city (or plant) fresh water	Oil	-No. 2 or No. 6 oil
Gas	-natural gas		

# Major Equipment & Emission Point Symbols



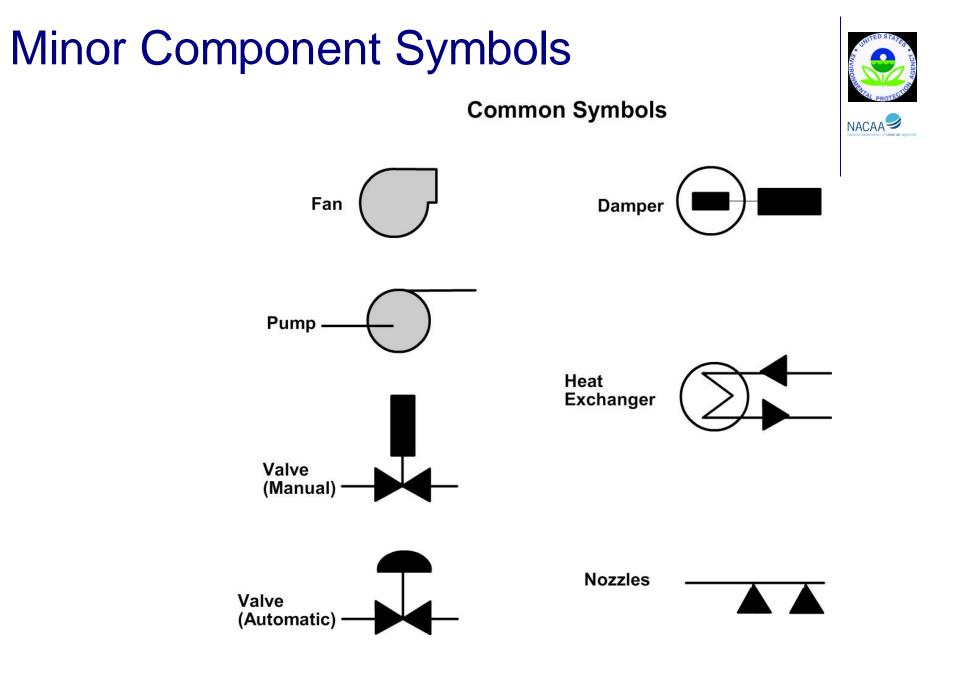


## Minor Components of Systems



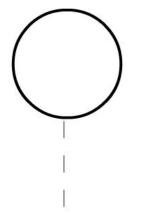
NACAA

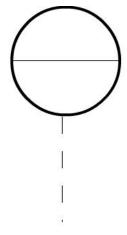
Fabric Filters			Wet Scrubbers					
	Bypass dampers		Pumps					
	Relief dampers		Nozzles					
	Outlet dampers		Manual valves					
	Reverse air fans		Automatic valves					
Carbon Adsorbers and Oxidizers								
	Indirect heat exchangers							
	Fans							

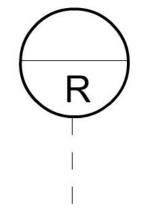


#### Instruments









Direct Reading Instrument Panel Mounted Instrument

Panel Mounted Instrument with Continuous Recorder

#### Instrument Codes



А	Motor current	рН	Liquid or slurry pH
CEM	Continuous emission monitor	Δp	Static pressure drop
Den	Density	SP	Gas static pressure
F	Flow	SSP	Stack sampling port
L	Liquid level	Т	Temperature
LEL	Lower explosive limit	V	Vacuum gauge
MP	Measurement port	VOC	Low concentration VOC monitor
Op	Opacity	W	Weight
Р	Gas or liquid pressure		

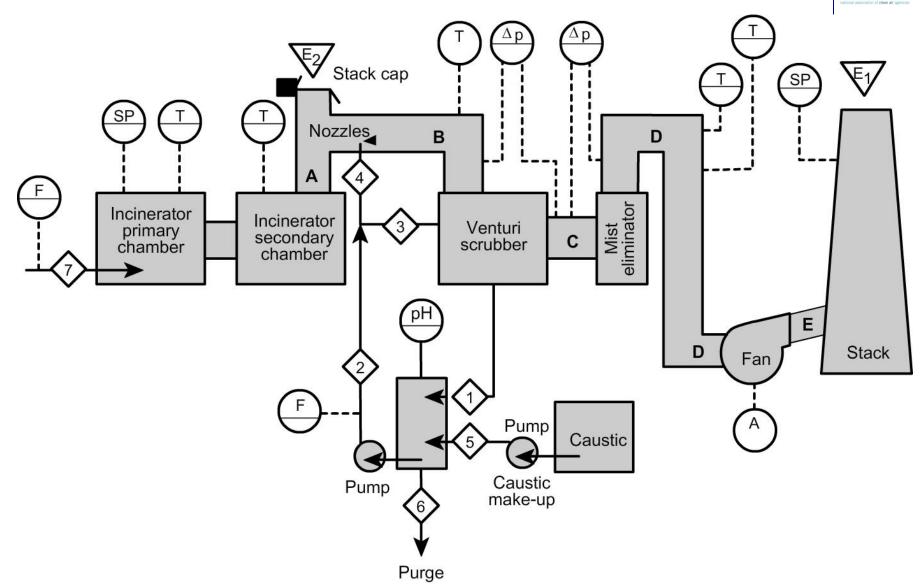
#### Materials of Construction



CS	Carbon Steel	RL	Rubber lined
FR	Fiberglass reinforced	SS	Stainless steel
Р	plastic		
N	Nickel alloy	W	Wood
		D	

#### Diagrams





### How diagrams help



- 1.Determine whether or not the operating data is consistent and logical.
- 2.Compare current data against sitespecific baseline data.
- 3.Determine specific areas that may need emphasis during the inspection.
- 4.Determine potential health and safety problems that may be encountered during the inspection.

#### Examples 10-8 and 10-9



#### Please review in your text

## **Flowcharts Summary**



- Identify changes in control device performance due to process changes
- Identify instruments that are not consistent with other similar instruments in the system
- Communicate effectively with other personnel
- Avoid potential health and safety hazards